Carnegie Mellon University

Vatabase Systems Index Concurrency Control



ADMINISTRIVIA

Homework #3 is due Sunday Sept 6th @ 11:59pm

Project #2 is due Sunday Sept 29th @ 11:59pm

→ Recitation next week

Mid-term Exam on Wednesday Oct 9th @ 2:00pm

 \rightarrow In-class in this room.



UPCOMING DATABASE TALKS

DataFusion Comet (DB Seminar)

- → Monday Sept 30th @ 4:30pm ET
- \rightarrow Zoom



Oracle Talk (DB Group)

- → Tuesday Oct 1st @ 12:00pm ET
- → GHC 8115

ORACLE

ParadeDB (DB Seminar)

- → Monday Oct 7th @ 4:30pm ET
- \rightarrow Zoom





OBSERVATION

We (mostly) assumed all the data structures that we have discussed so far are single-threaded.

A modern DBMS needs to allow multiple threads to safely access data structures to take advantage of additional CPU cores and hide disk I/O stalls.





CONCURRENCY CONTROL

A <u>concurrency control</u> protocol is the method that the DBMS uses to ensure "correct" results for concurrent operations on a shared object.

- A protocol's correctness criteria can vary:
- → **Logical Correctness:** Can a thread see the data that it is supposed to see?
- → **Physical Correctness:** Is the internal representation of the object sound?



TODAY'S AGENDA

Latches Overview

Hash Table Latching

B+Tree Latching

Leaf Node Scans

Project #2 Announcement



LOCKS VS. LATCHES

Locks (Transactions)

- → Protect the database's logical contents from other transactions.
- → Held for transaction's duration.
- \rightarrow Need to be able to rollback changes.

Latches (Workers)

- → Protect the critical sections of the DBMS's internal data structure from other workers (e.g., threads).
- \rightarrow Held for operation duration.
- \rightarrow Do <u>not</u> need to be able to rollback changes.



LOCKS VS. LATCHES

Lecture #15



Locks

Separate... Transactions

Protect... Database Contents

During... Entire Transactions

Modes... Shared, Exclusive, Update,

Intention

Deadlock Detection & Resolution

...by... Waits-for, Timeout, Aborts

Kept in... Lock Manager

Latches

Workers (threads, processes)

In-Memory Data Structures

Critical Sections

Read, Write

Avoidance

Coding Discipline

Protected Data Structure

Source: Goetz Graefe

ECMU-DB 15-445/645 (Fall 2024)

LATCH MODES

Read Mode

- → Multiple threads can read the same object at the same time.
- → A thread can acquire the read latch if another thread has it in read mode.

Write Mode

- → Only one thread can access the object.
- → A thread cannot acquire a write latch if another thread has it in any mode.

Compatibility Matrix

| | Read | Write |
|-------|----------|-------|
| Read | / | X |
| Write | X | X |



LATCH IMPLEMENTATION GOALS

Small memory footprint. 闩锁需要内联到数据结构中, 因此尽可能占据小的内存空间.

Fast execution path when no contention.

Decentralized management of latches.

Avoid expensive system calls.

Room: Moderated Discussions

By: Linus Torvalds (torvalds.delete@this.linux-foundation.org), January 3, 2020 6:05 pm

Beastian (no.email.delete@this.aol.com) on January 3, 2020 11:46 am wrote:

> I'm usually on the other side of these primitives when I write code as a consumer of them, > but it's very interesting to read about the nuances related to their implementations:

The whole post seems to be just wrong, and is measuring something completely different than what the author thinks and claims it is

Small memory

First off, spinlocks can only be used if you actually know you're not being scheduled while using them. But the blog post author seems to be implementing his own spinlocks in user space with no regard for whether the lock user might be scheduled or not. And the code used for the

It basically reads the time before releasing the lock, and then it reads it after acquiring the lock again, and claims that the time difference is the time when no lock was held. Which is just inane and pointless and completely wrong. That's pure garbage. What happens is that

Fast execution

- (a) since you're spinning, you're using CPU time
- (b) at a random time, the scheduler will schedule you out

Decentralized

(c) that random time might ne just after you read the "current time", but before you actually released the spinlock.

So now you still hold the lock, but you got scheduled away from the CPU, because you had used up your time slice. The "current time" you read is basically now stale, and has nothing to do with the (future) time when you are actually going to release the lock.

Avoid expensi

Somebody else comes in and wants that "spinlock", and that somebody will now spin for a long while, since nobody is releasing it - it's still held by that other thread entirely that was just scheduled out. At some point, the scheduler says "ok, now you've used your time slice", and schedules the original thread, and now the lock is actually released. Then another thread comes in, gets the lock again, and then it looks at the time and says "oh, a long time passed without the lock being held at all".

And notice how the above is the good schenario. If you have more threads than CPU's (maybe because of other processes unrelated to your own test load), maybe the next thread that gets sheeduled isn't the one that is going to release the lock. No, that one already got its timeslice, so the next thread scheduled might be another thread that wants that lock that is still being held by the thread that isn't even

So the code in question is pure garbage. You can't do spinlocks like that. Or rather, you very much can do them like that, and when you do that you are measuring random latencies and getting nonsensical values, because what you are measuring is "I have a lot of busywork, where all the processes are CPU-bound, and I'm measuring random points of how long the scheduler kept the process in place".

And then you write a blog-post blamings others, not understanding that it's your incorrect code that is garbage, and is giving random garbage

SECMU•DB 15-445/645 (Fall 2024)

Source: Filip Pizlo

Small memory

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避免在用户空间使用自旋锁.

自旋锁是一种锁, 当线程尝试获取它时, 会在一

个循环中简单地等待("自旋"), 反复检查该锁

I repeat: do not use spinlocks in user space, unless you actually know what you're doing. And be aware that the likelihood that you know what you are doing is basically nil.

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Room: Moderated Discussions

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是否可用。

Test-and-Set Spinlock

Blocking OS Mutex

Reader-Writer Locks

Advanced approaches:

- → Adaptive Spinlock (<u>Apple ParkingLot</u>)
- → Queue-based Spinlock (<u>MCS Locks</u>)
- → Optimistic Lock Coupling (<u>The Germans</u>)



LATCH I

Test-and-Set Spinlo
Blocking OS Mutex
Reader-Writer Loc

Advanced approach

- → Adaptive Spinlock (
- → Queue-based Spinle
- → Optimistic Lock Co



Locking in WebKit

May 6, 2016 by Filip Pizlo @filpizlo

Back in August 2015 we replaced all spinlocks and OS-provided mutexes in WebKit with the new WTF::Lock (WTF stands for Web Template Framework). We also replaced all OS-provided condition variables with WTF::Condition. These new primitives have some cool properties:

- 1. WTF::Lock and WTF::Condition only require one byte of storage each. WTF::Lock only needs two bits in that byte. The small size encourages using huge numbers of very fine-grained locks. OS mutexes often require 64 bytes or more. The small size of WTF::Lock means that there's rarely an excuse for not having one, or even multiple, fine-grained locks in any object that has things that need to be synchronized.
- 2. WTF::Lock is super fast in the case that matters most: uncontended lock acquisition. Parallel algorithms tend to avoid contention by having many fine-grained locks. This means that a mature parallel algorithm will have many uncontended lock acquisitions that is, calls to lock() when the lock is not held, and calls to unlock() when nobody is waiting in line. Similarly, waiting.
- 3. WTF::Lock is fast under microcontention. A microcontended lock is one that is contended and the critical section is short. This means that shortly after any failing lock attempt, the lock will become available again since no thread will hold the lock for long. This is the most common kind of contention in parallel code, since it's common to go to great pains to do very little work while
- 4. WTF::Lock doesn't waste CPU cycles when a lock is held for a long time. WTF::Lock is adaptive: it changes its strategy for how to wait for the lock to become available based on how long it has been trying. If the lock doesn't become available promptly, WTF::Lock will suspend the calling thread until the lock becomes available.

LATCH I

WebKit

Test-and-Set Spinlo
Blocking OS Mutex
Reader-Writer Loc

避免依赖 OS 提供的 pthread 实现.

Advanced approach

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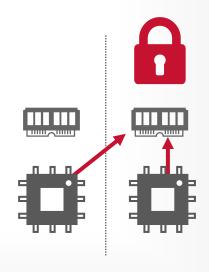
Compared to OS-provided locks like pthread_mutex, WTF::Lock is 64 times smaller and up to 180 times faster. Compared to OS-provided condition variables like pthread_cond, WTF::Condition is 64 times smaller. Using WTF::Lock instead of pthread_mutex means that WebKit is 10% faster on JetStream, 5% faster on Speedometer, and 5% faster on our page loading test.

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Approach #1: Test-and-Set Spin Latch (TAS)

- → Very efficient (single instruction to latch/unlatch)
- → Non-scalable, not cache friendly, not OS friendly.
- → Example: std::atomic<T>



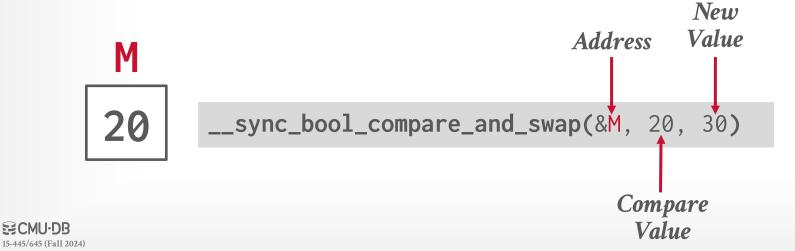


COMPARE-AND-SWAP

Atomic instruction that compares contents of a memory location M to a given value V

- → If values are equal, installs new given value V' in M
- \rightarrow Otherwise, operation fails

See C++11 Atomics

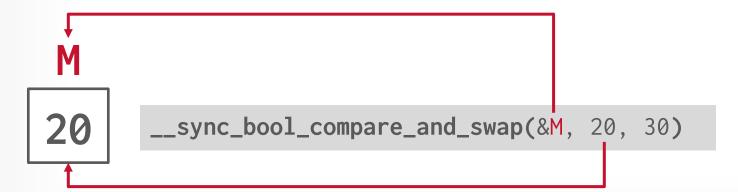


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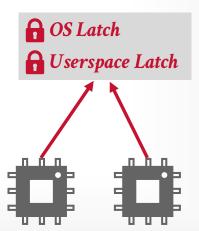




Approach #2: Blocking OS Mutex

- \rightarrow Simple to use
- → Non-scalable (about 25ns per lock/unlock invocation)
- → Example: std::mutex —→pthread_mutex_t —→ futex

```
std::mutex m;
:
m.lock();
// Do something special...
m.unlock();
```

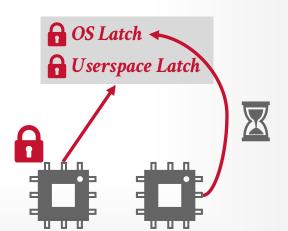




Approach #2: Blocking OS Mutex

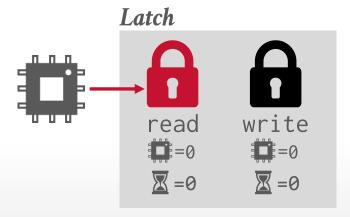
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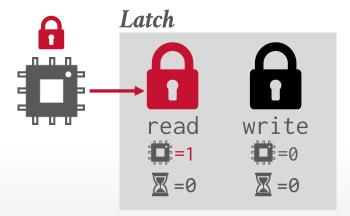


- → Allows for concurrent readers. Must manage read/write → pthread_mutex_t queues to avoid starvation. → pthread_cond_t
- \rightarrow Can be implemented on top of spinlocks.
- → Example: std::shared_mutex → pthread_rwlock_t



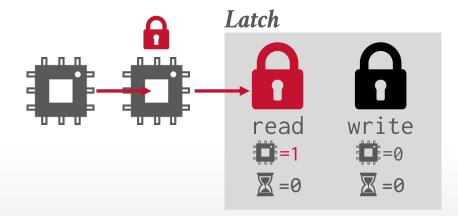


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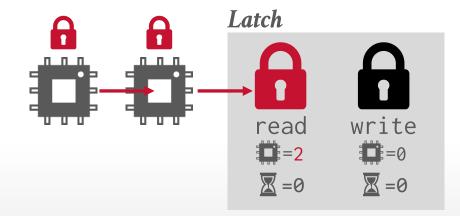


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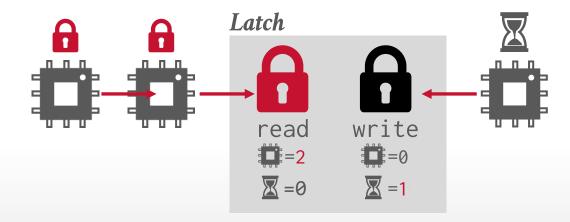


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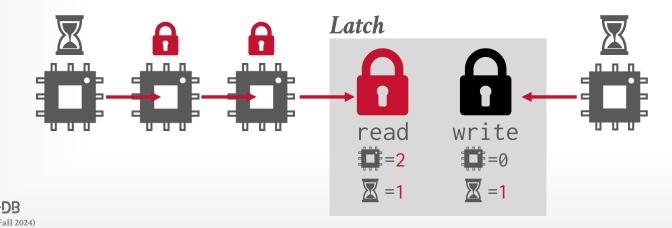


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HASH TABLE LATCHING

Easy to support concurrent access due to the limited ways threads access the data structure.

- → All threads move in the same direction and only access a single page/slot at a time.
- \rightarrow Deadlocks are not possible.

To resize the table, take a global write latch on the entire table (e.g., in the header page).



HASH TABLE LATCHING

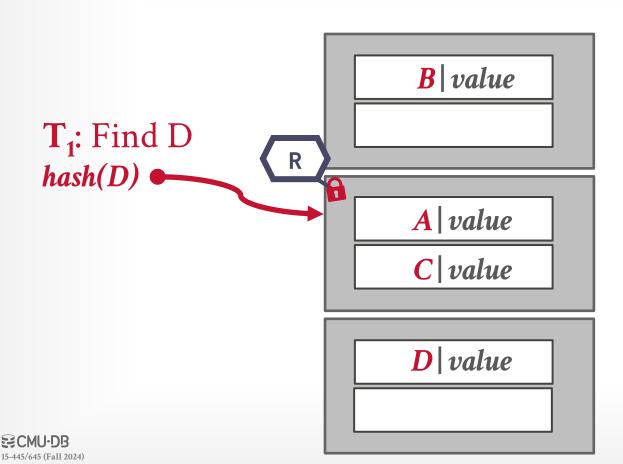
Approach #1: Page/Block Latches

- → Each page/block has its own reader-writer latch that protects its entire contents.
- → Threads acquire either a read or write latch before they access a page/block.

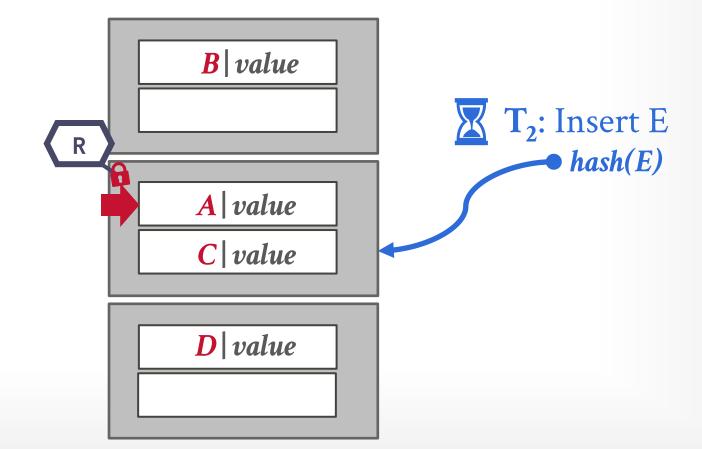
Approach #2: Slot Latches

- \rightarrow Each slot has its own latch.
- → Can use a single-mode latch to reduce meta-data and computational overhead.



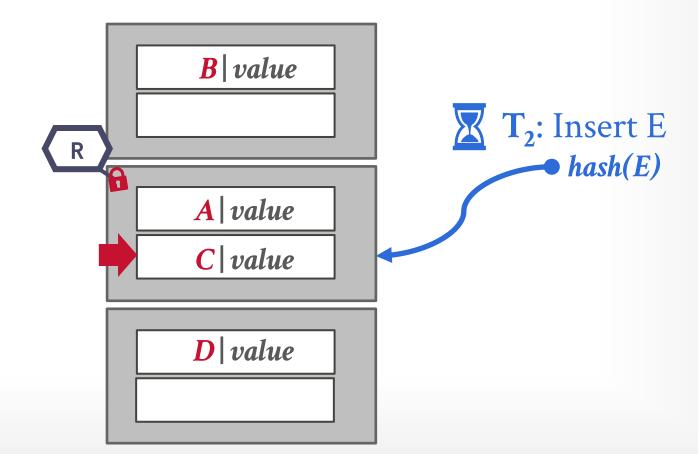


T₁: Find D hash(D)

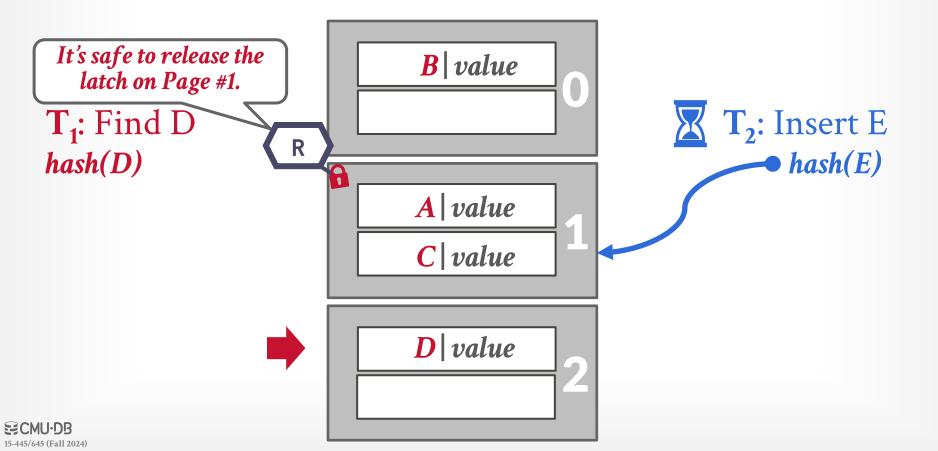




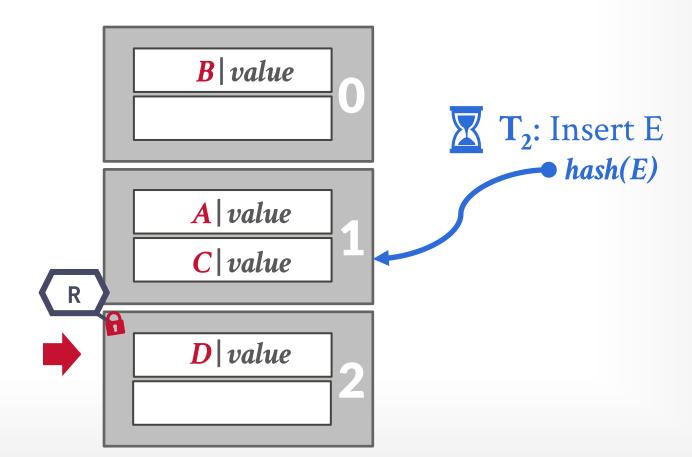
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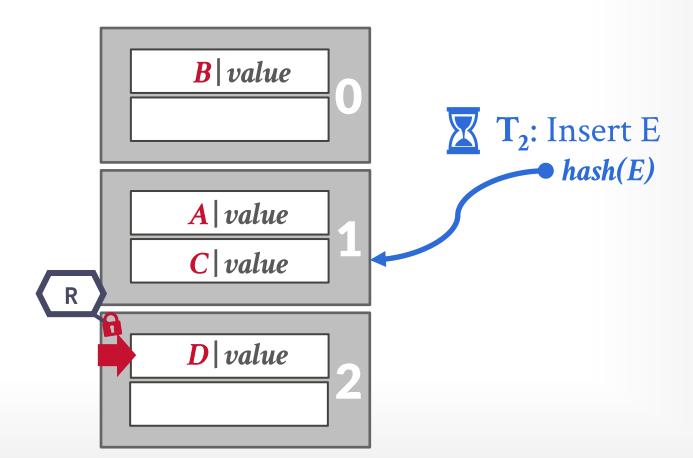


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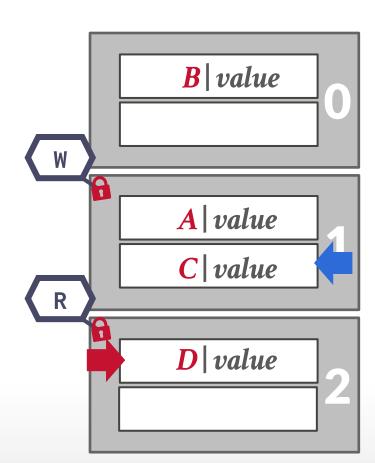


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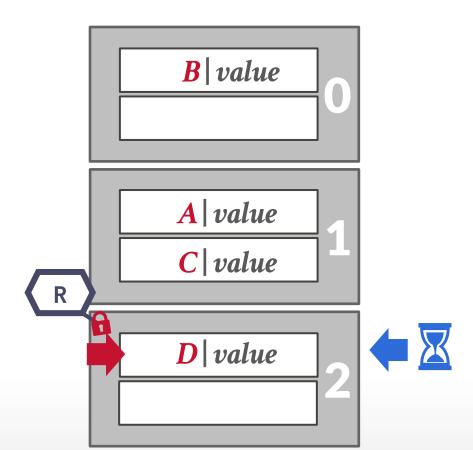
T₁: Find D hash(D)



T₂: Insert E hash(E)



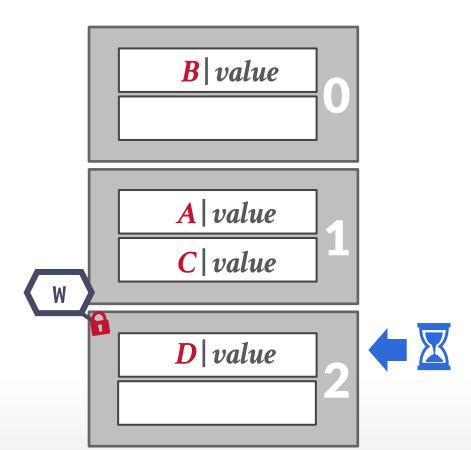
T₁: Find D hash(D)



 T_2 : Insert E hash(E)



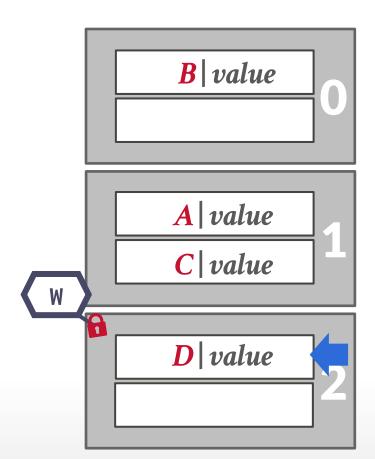
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 T_2 : Insert E hash(E)

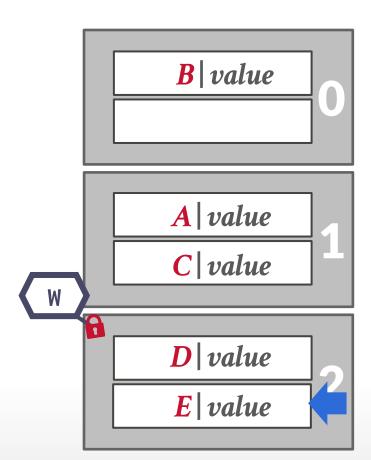


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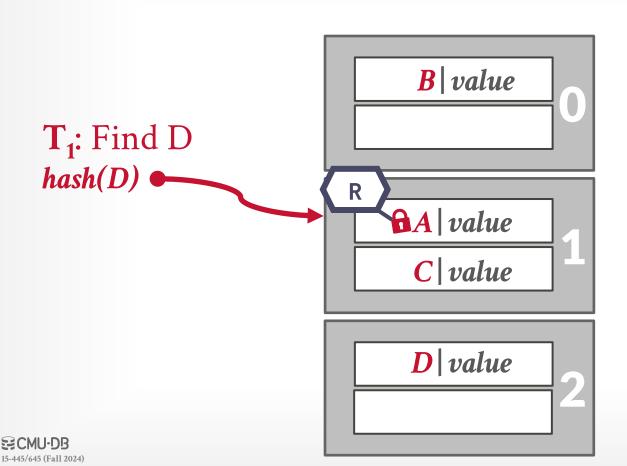




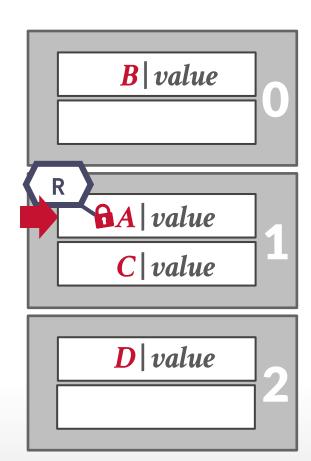
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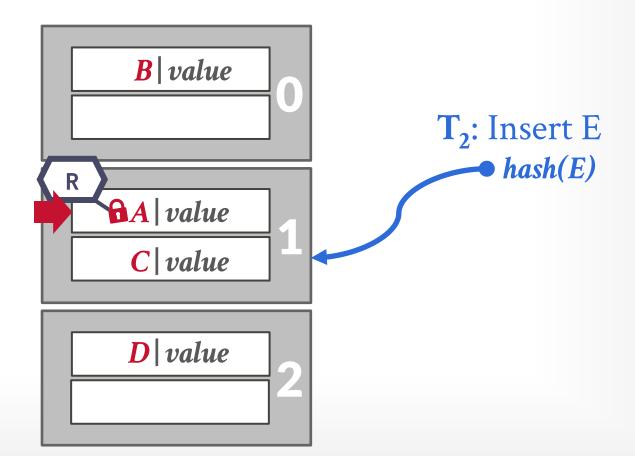


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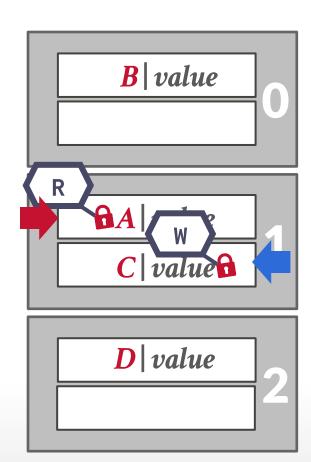


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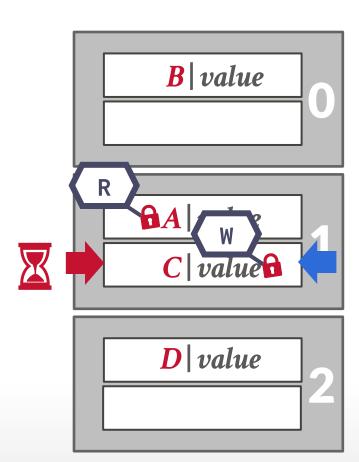


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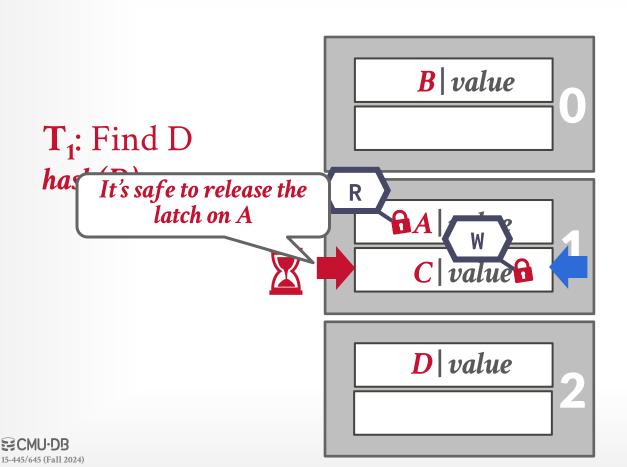




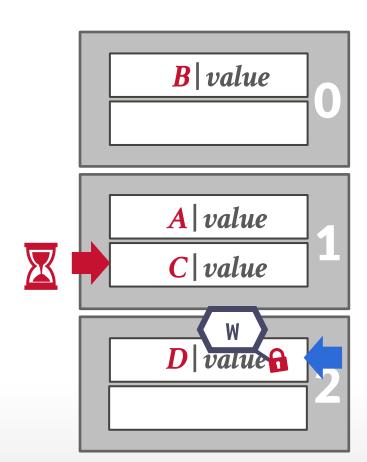
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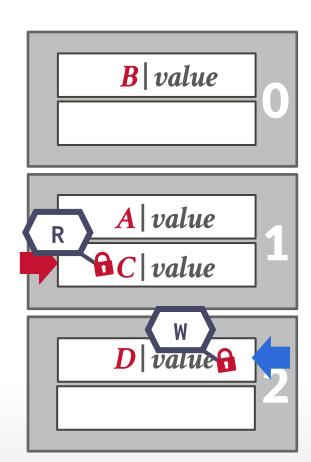


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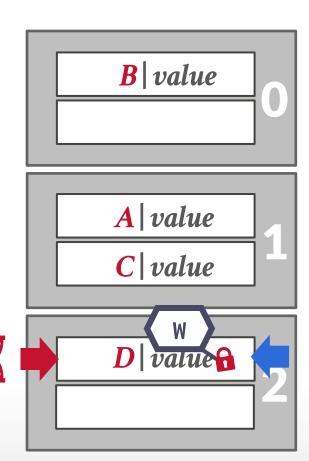


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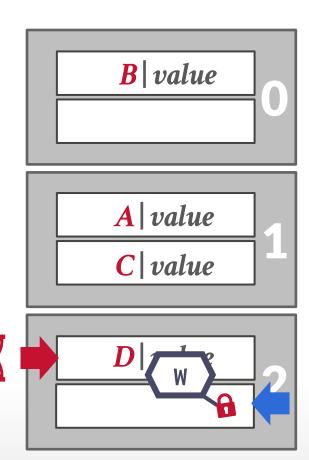


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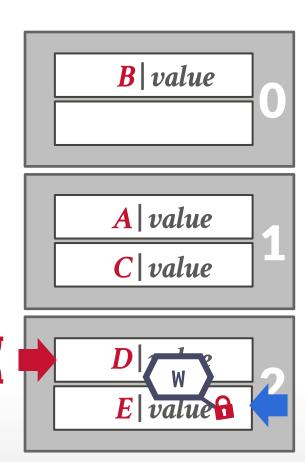


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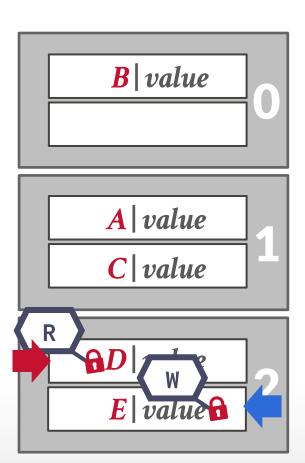


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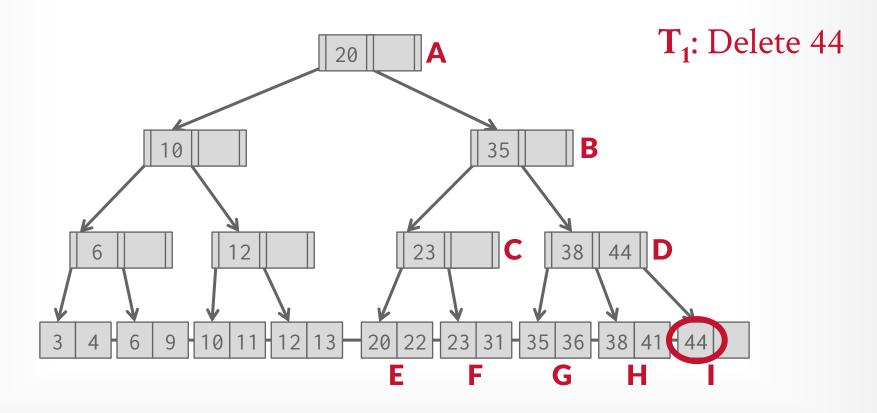
B+TREE CONCURRENCY CONTROL

We want to allow multiple threads to read and update a B+Tree at the same time.

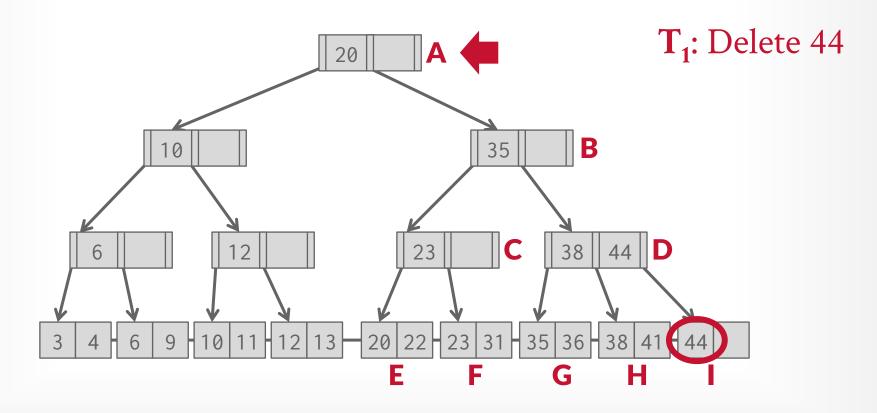
We need to protect against two types of problems:

- → Threads trying to modify the contents of a node at the same time.
- → One thread traversing the tree while another thread splits/merges nodes.

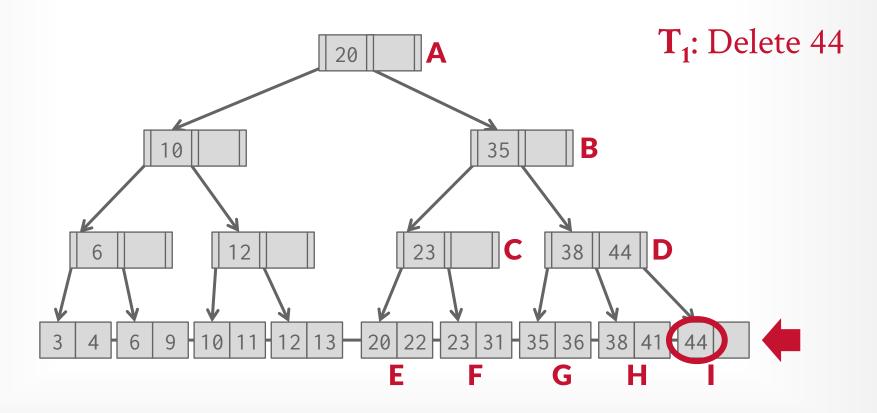




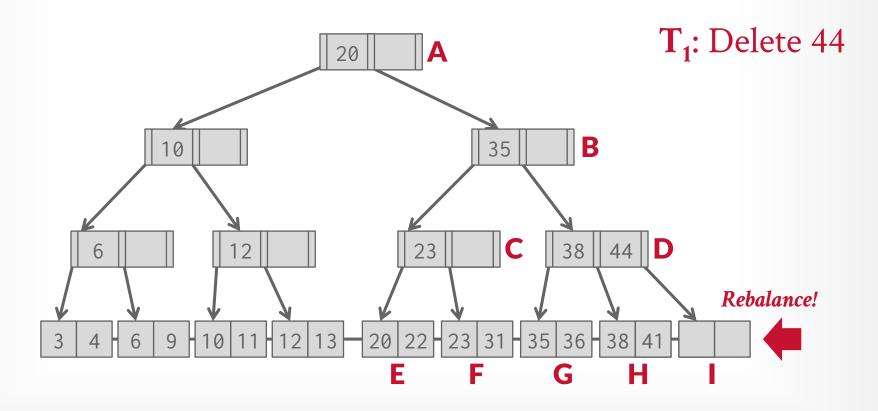




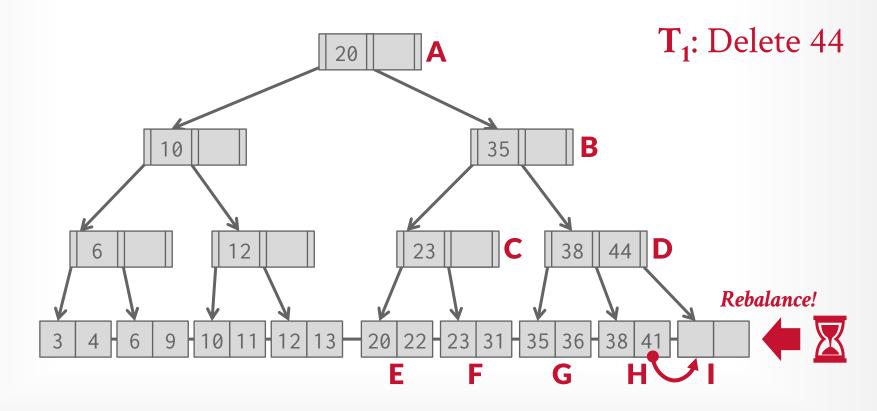




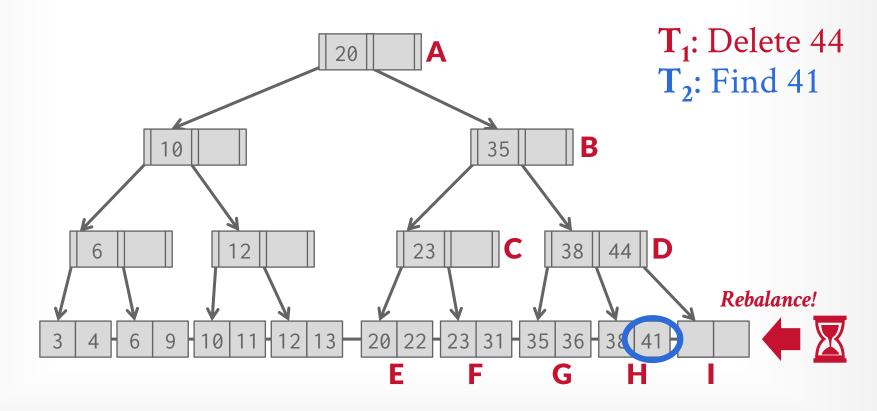




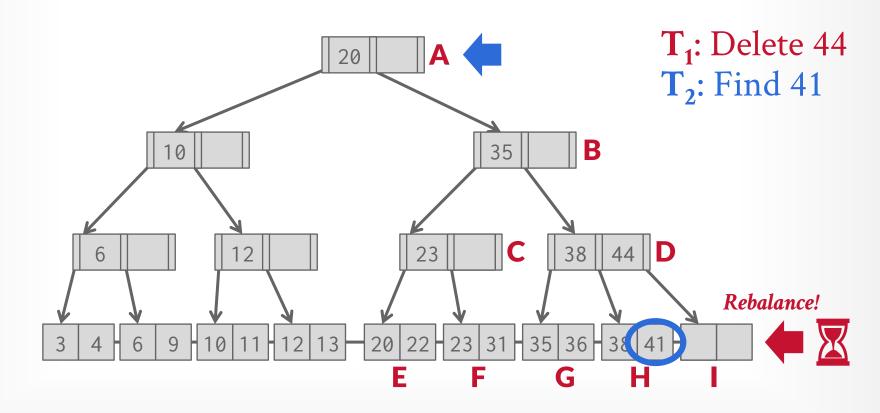




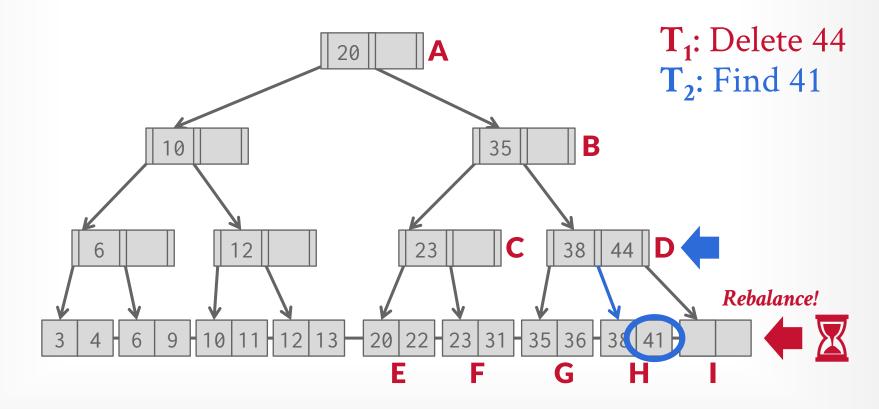




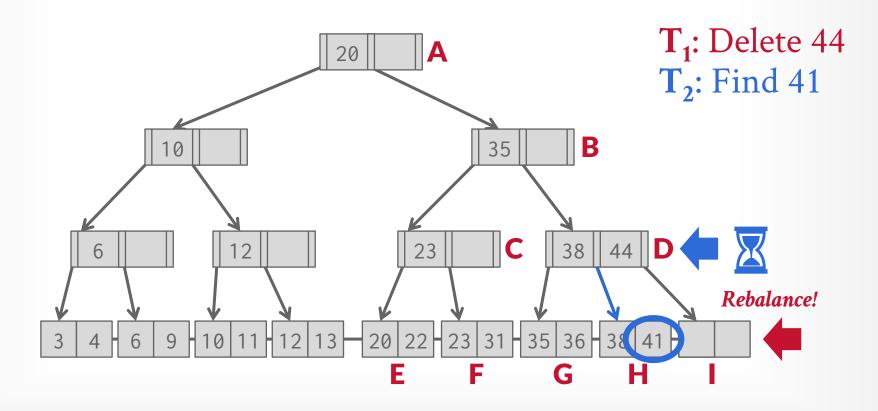




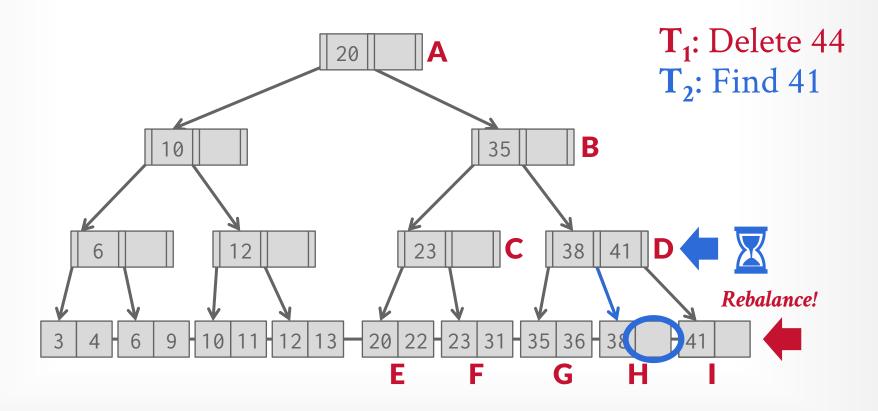




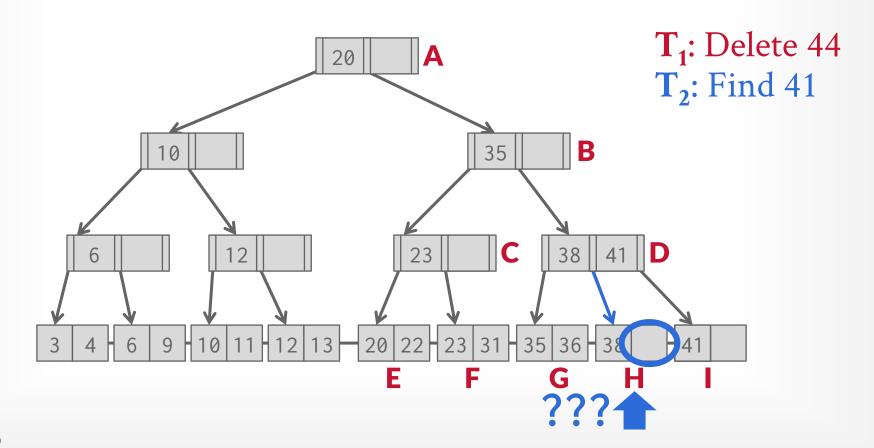














LATCH CRABBING/COUPLING

Protocol to allow multiple threads to access/modify B+Tree at the same time.

- → Get latch for parent
- → Get latch for child
- → Release latch for parent if "safe"

A <u>safe node</u> is one that will not split or merge when updated.

- → Not full (on insertion)
- → More than half-full (on deletion)



LATCH CRABBING/COUPLING

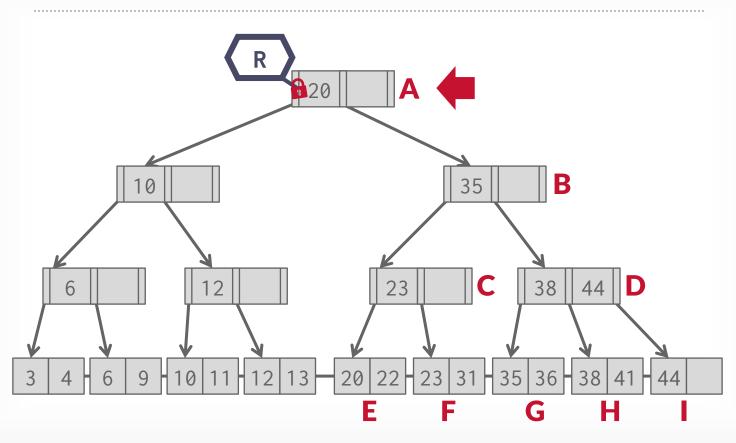
Find: Start at root and traverse down the tree:

- \rightarrow Acquire **R** latch on child,
- \rightarrow Then unlatch parent.
- \rightarrow Repeat until we reach the leaf node.

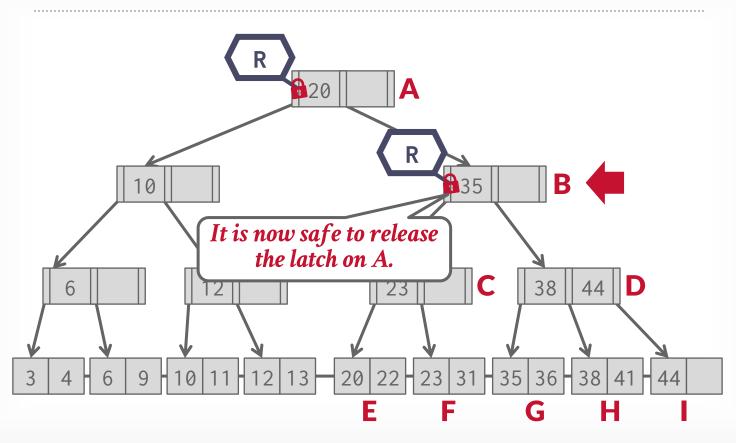
Insert/Delete: Start at root and go down, obtaining **W** latches as needed. Once child is latched, check if it is safe:

→ If child is safe, release all latches on ancestors

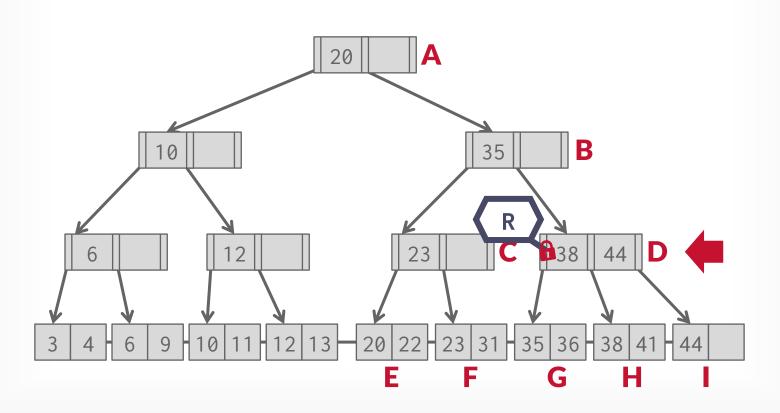




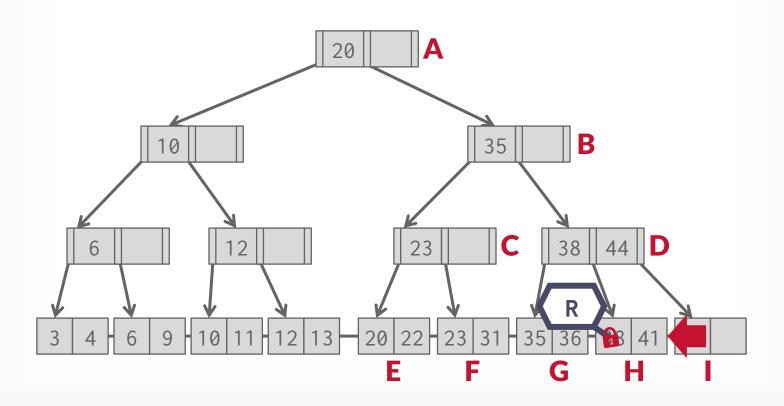




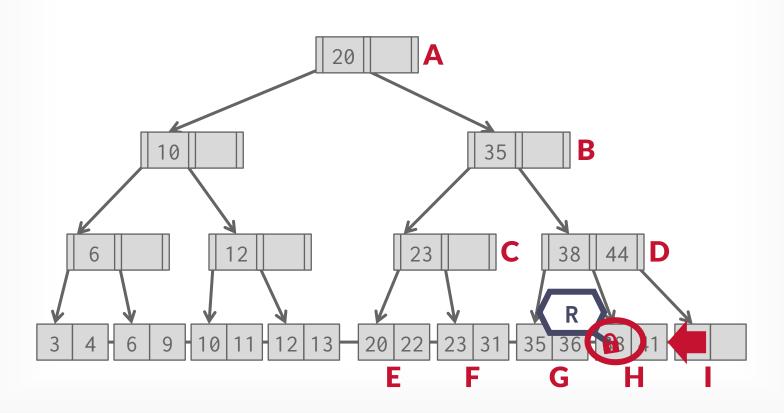




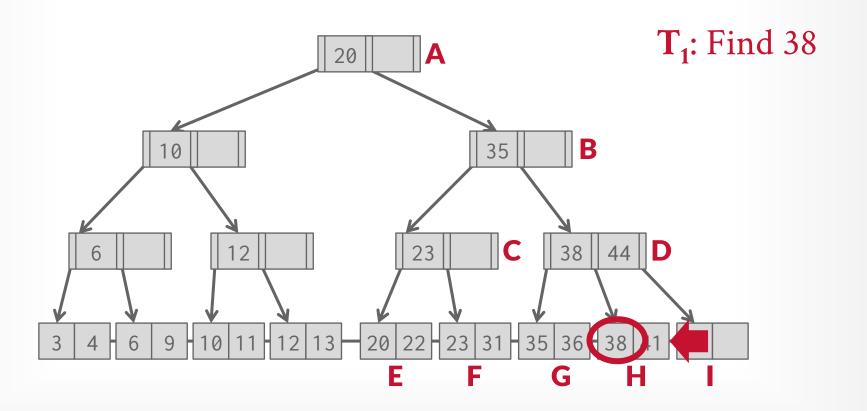




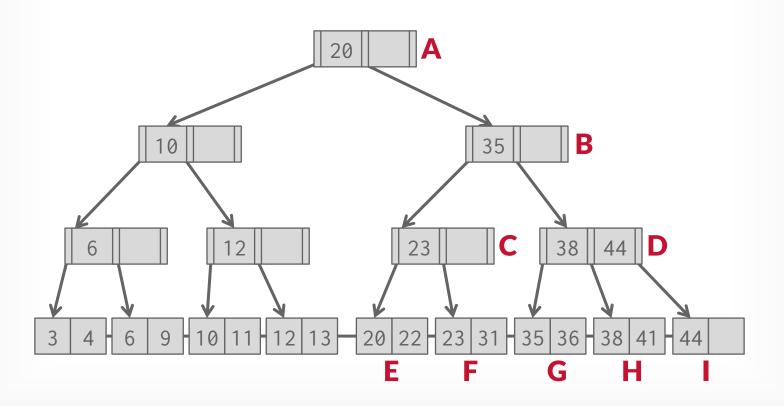




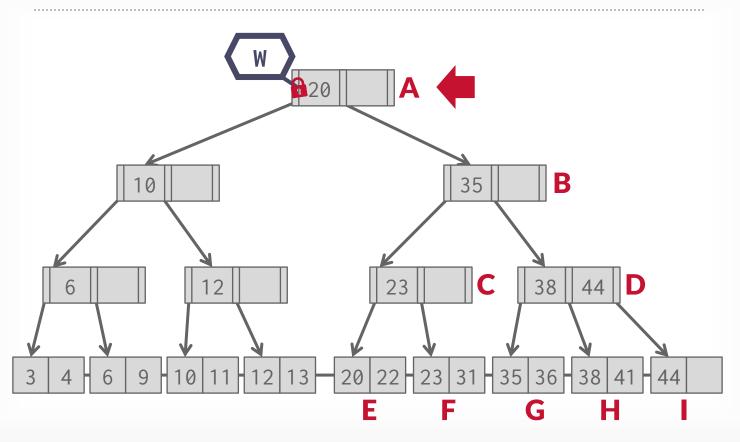




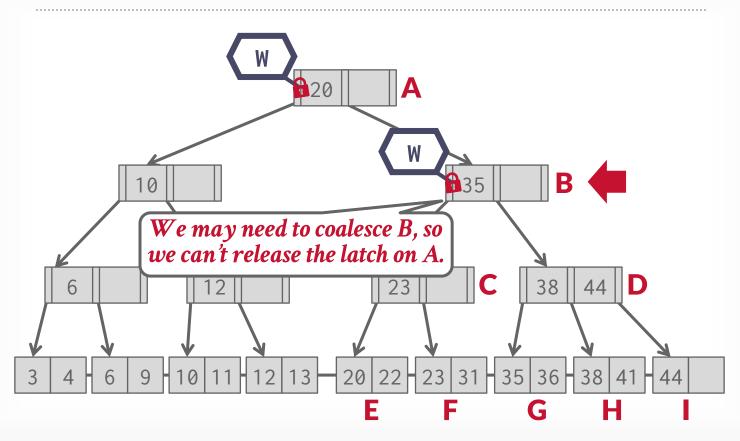




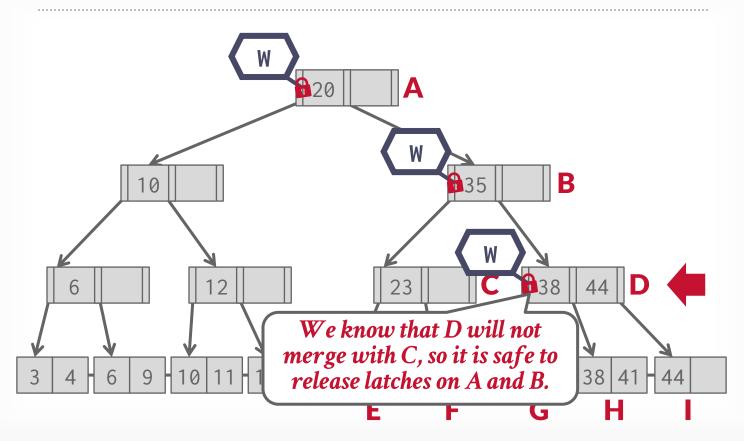




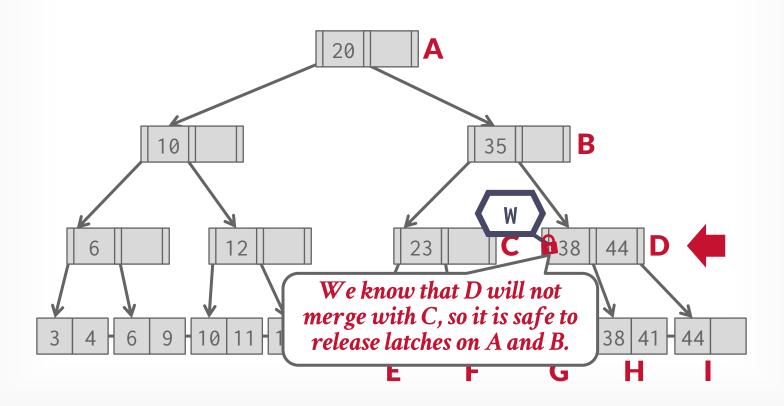




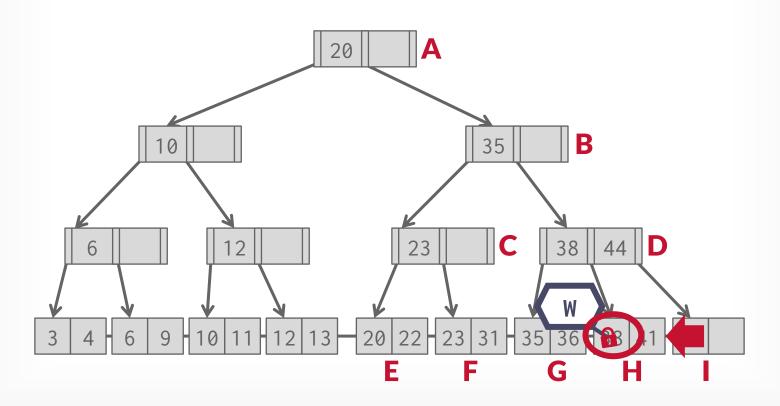




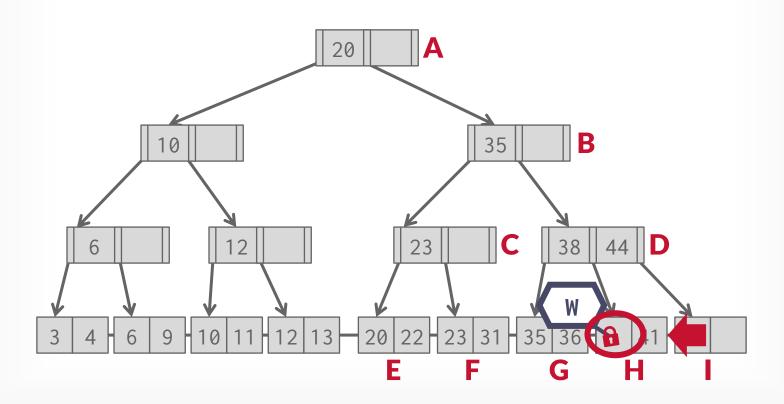




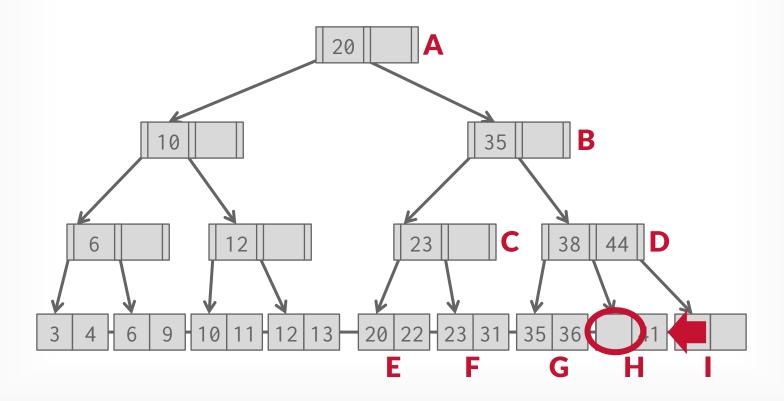




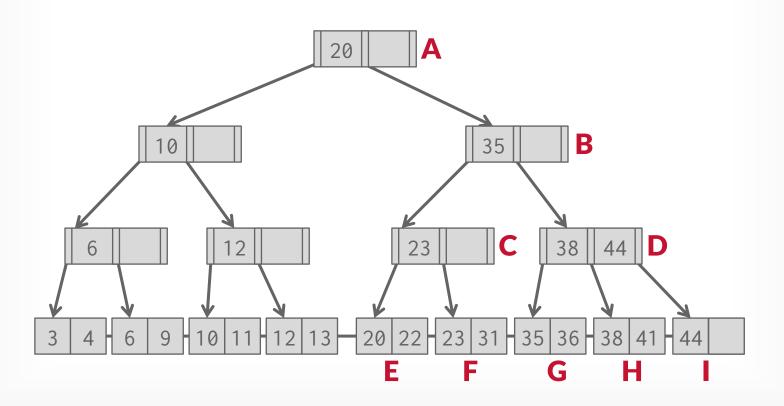




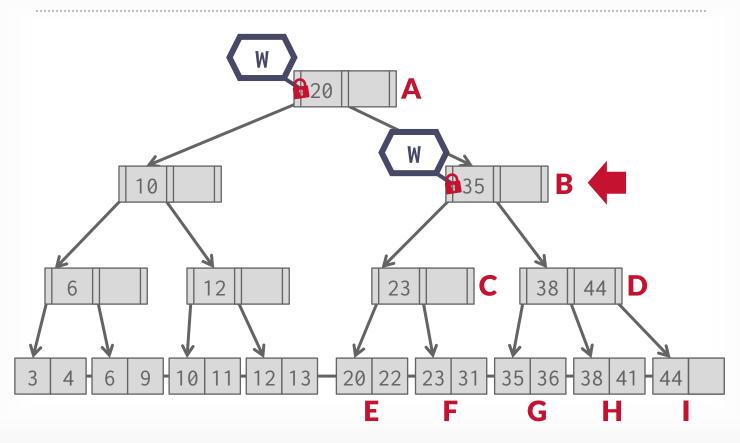




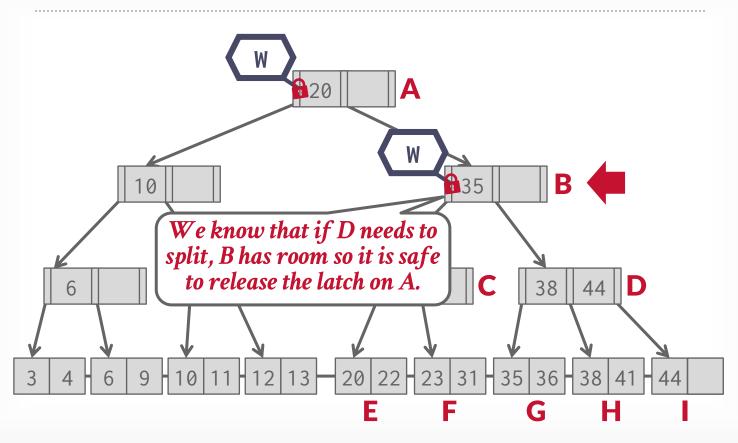




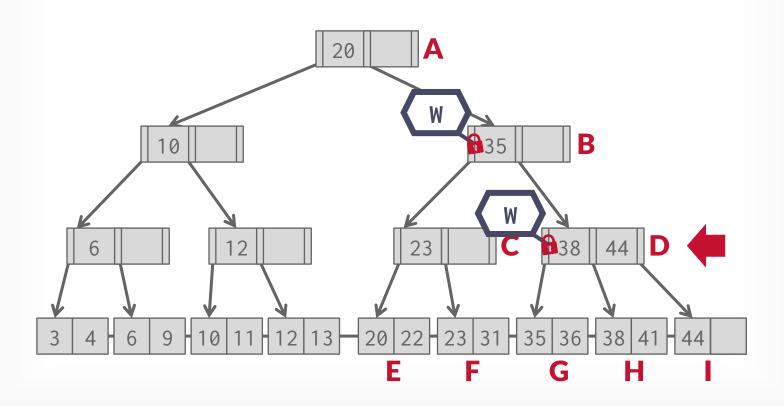




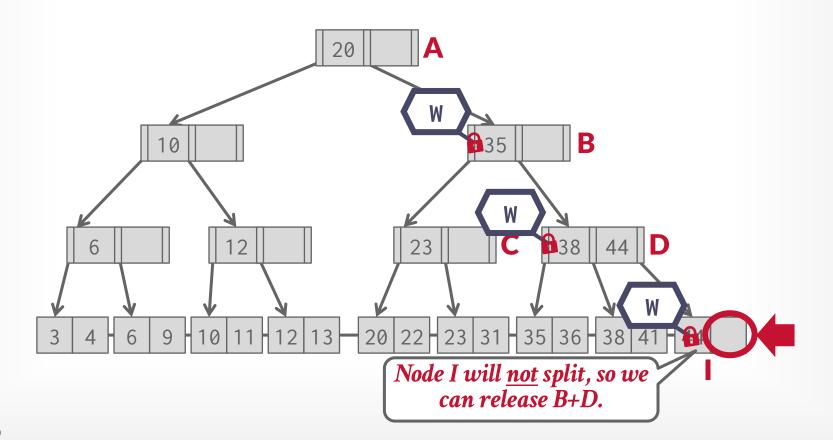




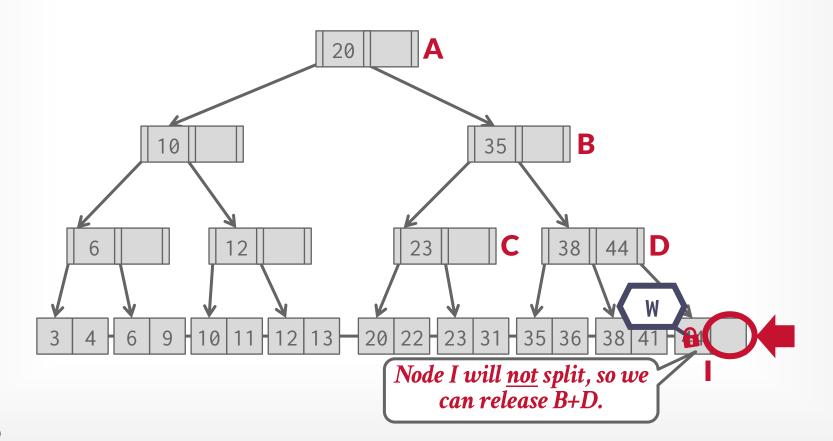




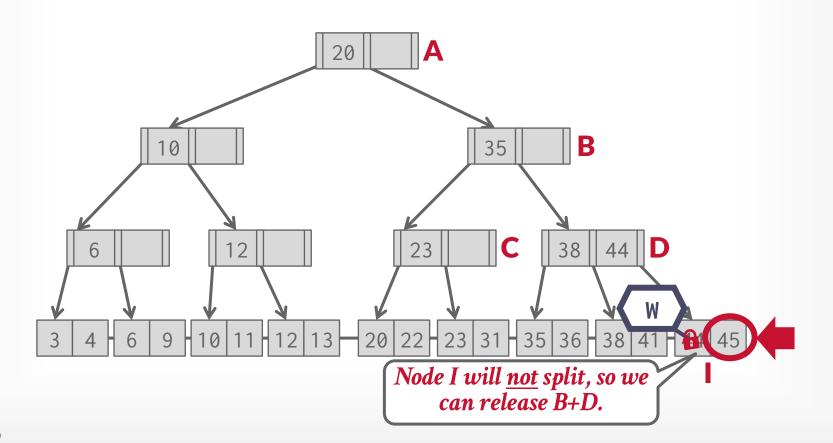




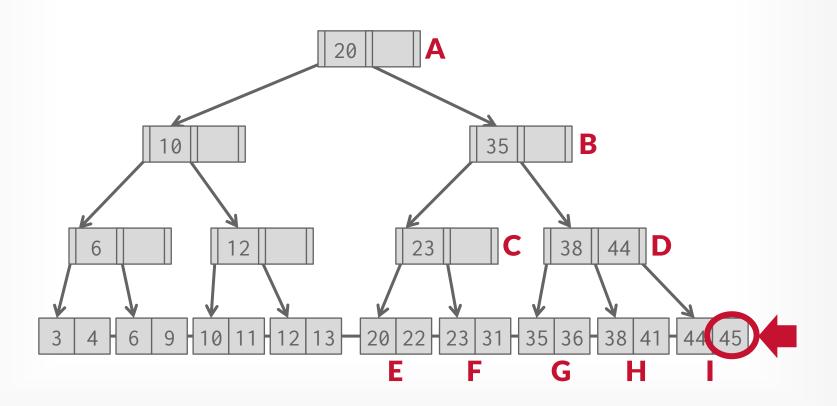




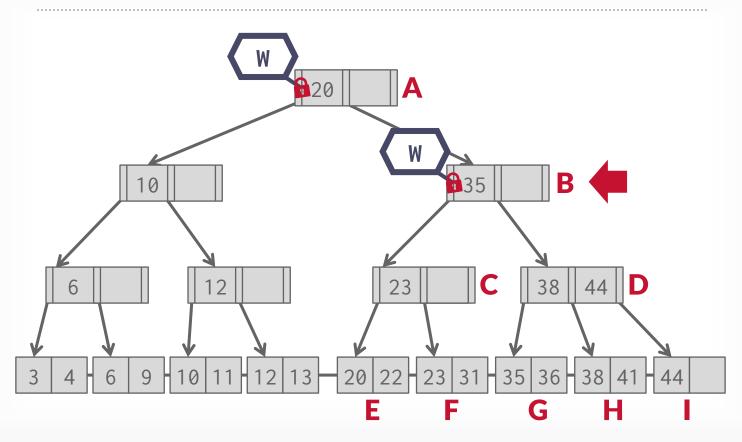




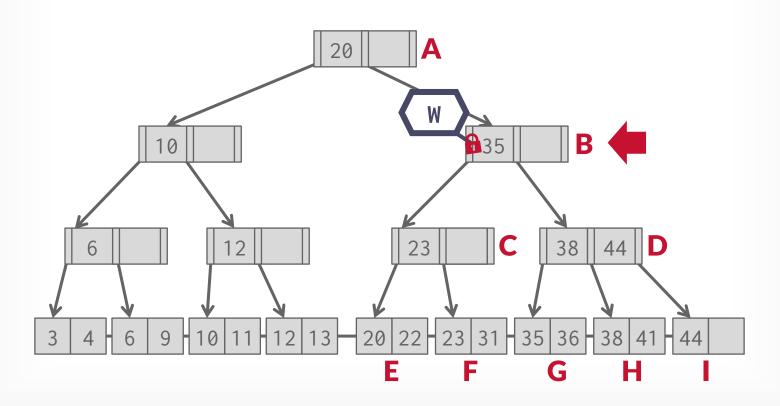




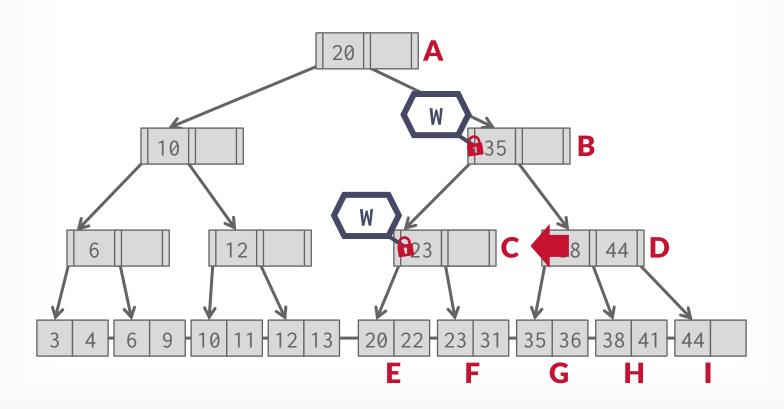




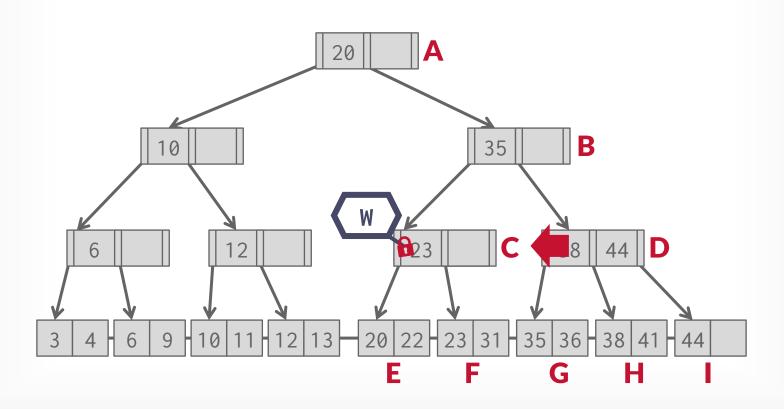




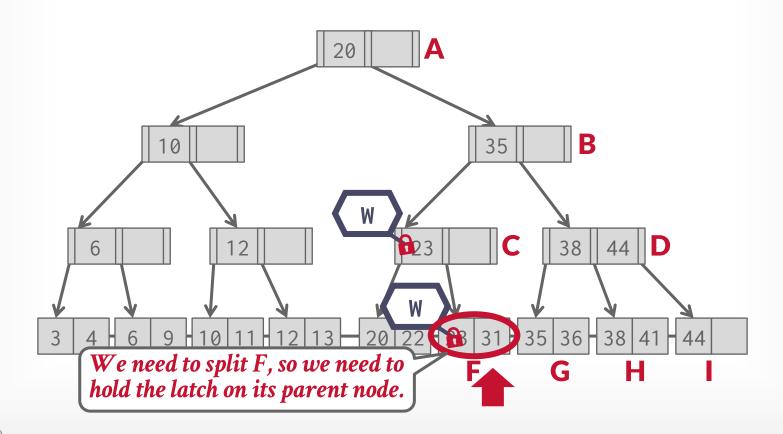




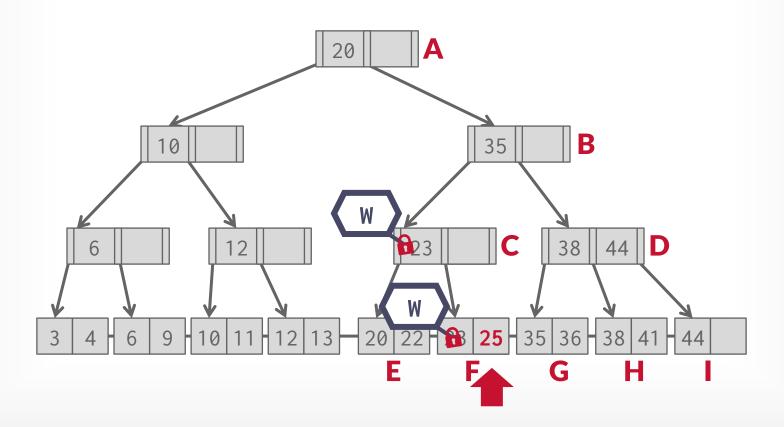




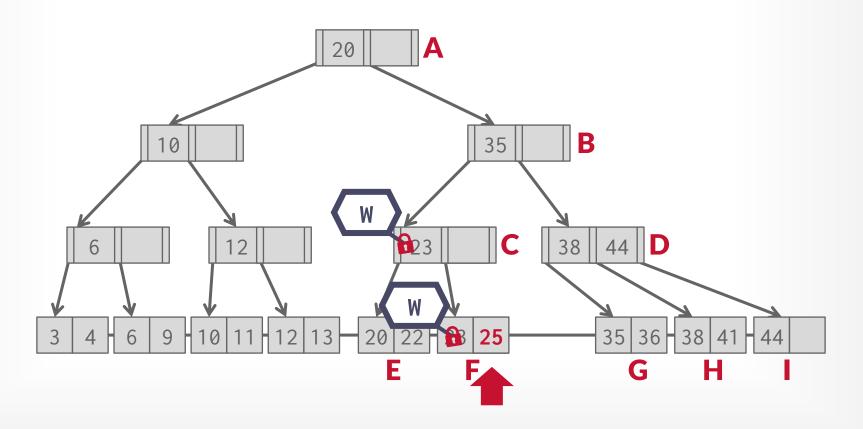




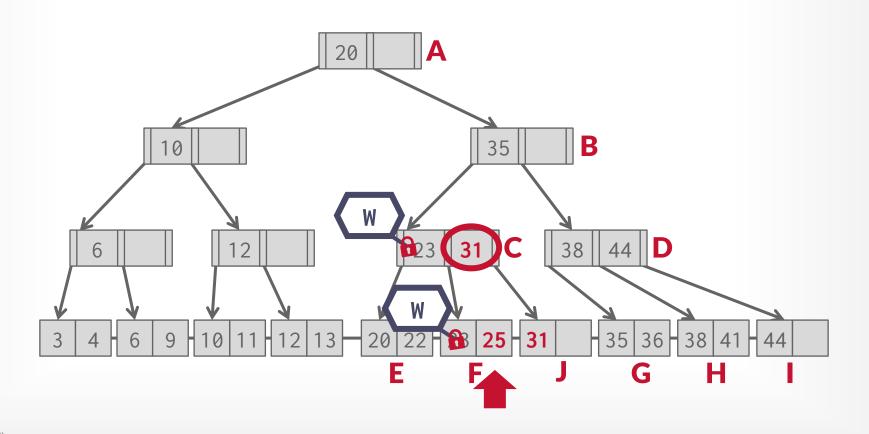




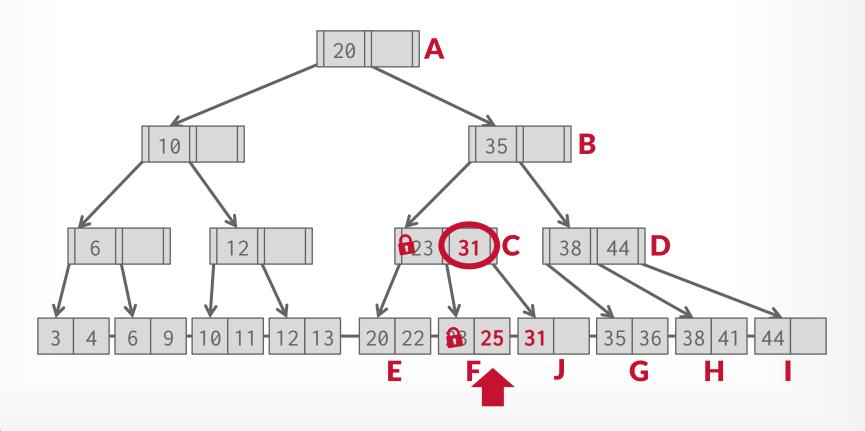








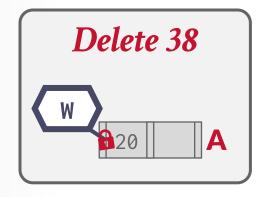


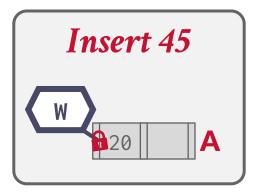


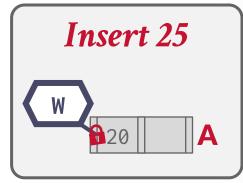


OBSERVATION

What was the first step that all the update examples did on the B+Tree?







Taking a write latch on the root every time becomes a bottleneck with higher concurrency.



BETTER LATCHING ALGORITHM

Most modifications to a B+Tree will not require a split or merge.

Instead of assuming there will be a split/merge, optimistically traverse the tree using read latches.

If a worker guesses wrong, repeat traversal with pessimistic algorithm.

Acta Informatica 9, 1-21 (1977)



Concurrency of Operations on B-Trees

R. Bayer* and M. Schkolnick

IBM Research Laboratory, San José, CA 95193, USA

Summary. Concurrent operations on B-trees pose the problem of insuring in that each operation can be carried out without interfering with other operations that each operation can be carried to subject the step performed simultaneously by other users. This problem can be become critical if these structures are being used to support access paths, like indexes, to data base systems. In this case, serializing access to one store these indexes can create an unacceptable bottlem for the cancerpath of the control of t

Recently, there has been some questioning on whether B-tree structures can support concurrent operations. In this paper, we examine the problem of concurrent access to B-trees. We present a deadlock free solution which can be tuned to specific requirements. An analysis is presented which allows the selection of parameters so as to satisfy these requirements.

The solution presented here uses simple locking protocols. Thus, we conclude that B-trees can be used advantageously in a multi-user environment.

1. Introduction

In this paper, we examine the problem of concurrent access to indexes which are maintained as B-trees. This type of organization was introduced by Bayer and McCreight [2] and some variants of it appear in Knuth [10] and Wedekind [13]. Performance studies of it were restricted to the single user environment. Recently, these structures have been examined for possible use in a multi-user (concurrent) environment. Some initial studies have been made about the feasibility of their use in this type of situation [1, 6], and [11].

An accessing schema which achieves a high degree of concurrency in using the index will be presented. The schema allows dynamic tuning to adapt its performance to the profile of the current set of users. Another property of the

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ünchen 2, Germany (Fed. Rep.)



BETTER LATCHING ALGORITHM

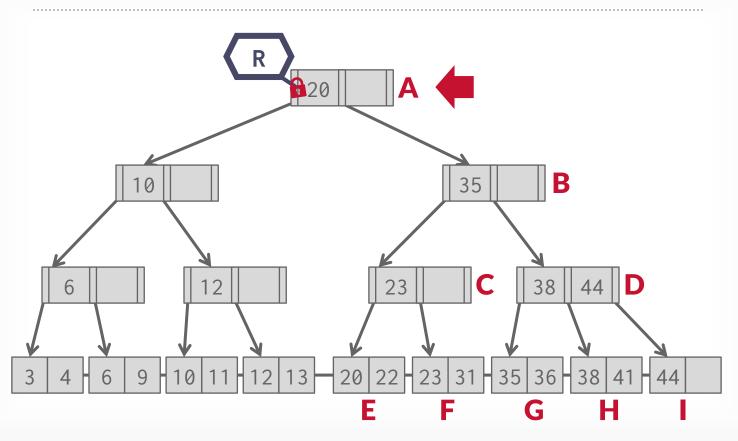
Search: Same as before.

Insert/Delete:

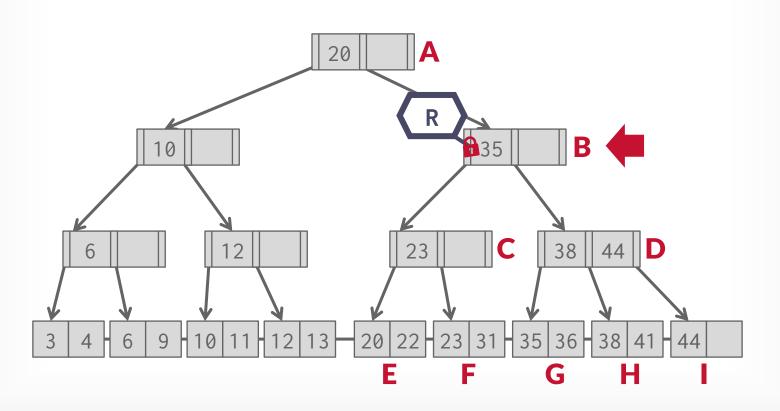
- → Set latches as if for search, get to leaf, and set W latch on leaf.
- → If leaf is not safe, release all latches, and restart thread using previous insert/delete protocol with write latches.

This approach optimistically assumes that only leaf node will be modified; if not, **R** latches set on the first pass to leaf are wasteful.

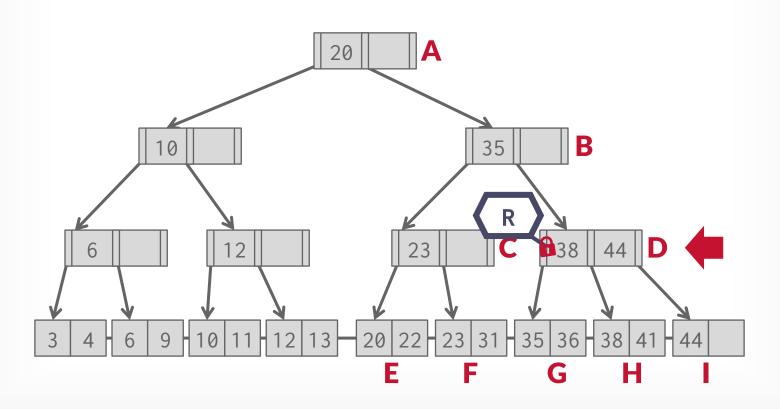




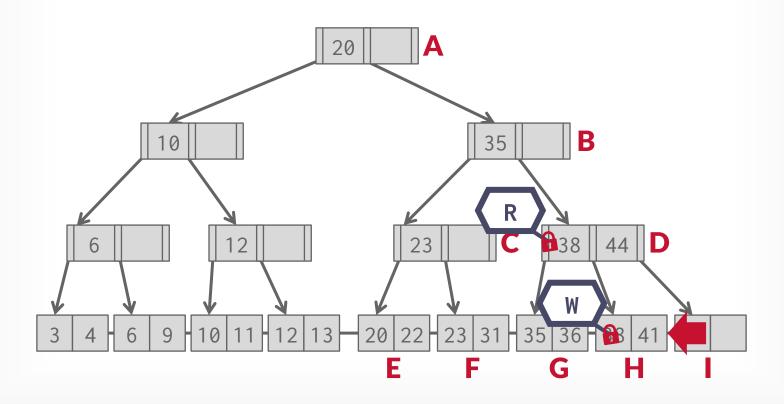




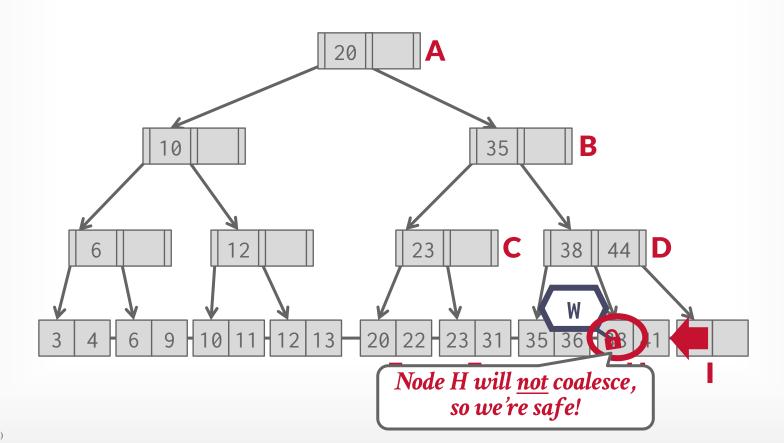




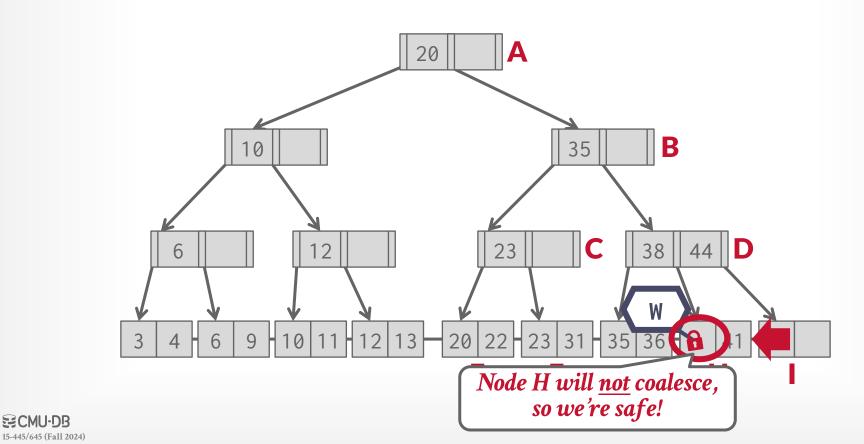


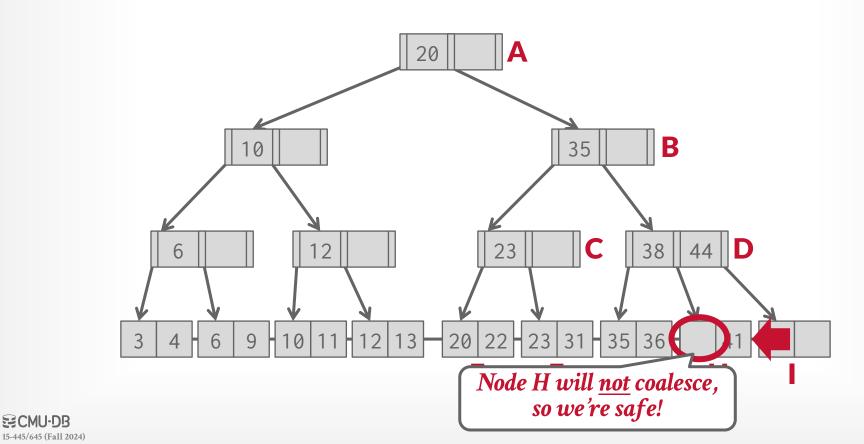


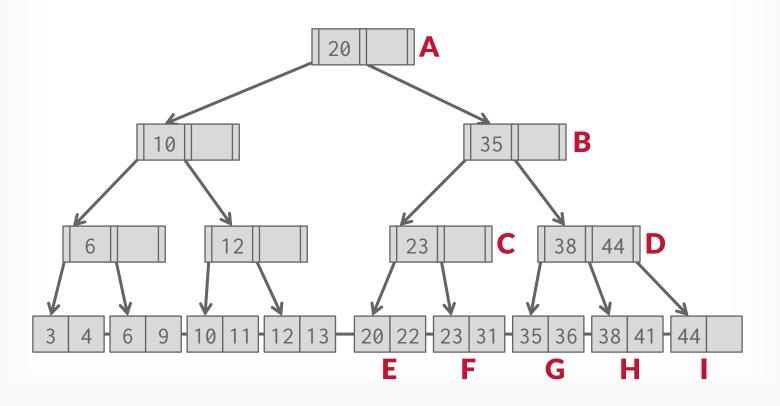






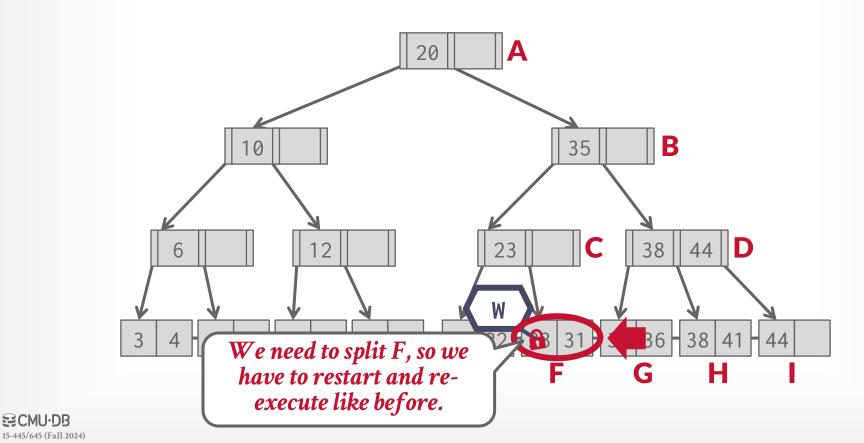








EXAMPLE #4 - INSERT 25



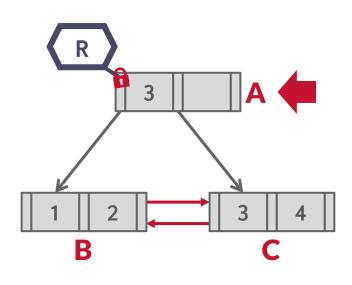
OBSERVATION

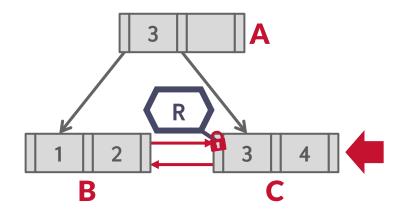
The threads in all the examples so far have acquired latches in a "top-down" manner.

- → A thread can only acquire a latch from a node that is below its current node.
- → If the desired latch is unavailable, the thread must wait until it becomes available.

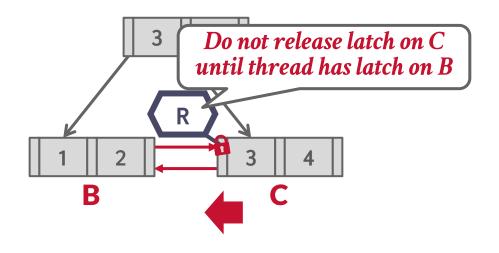
But what if threads want to move from one leaf node to another leaf node?



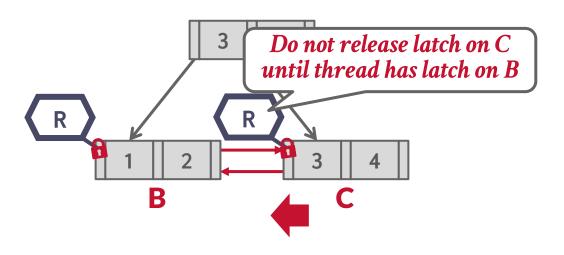




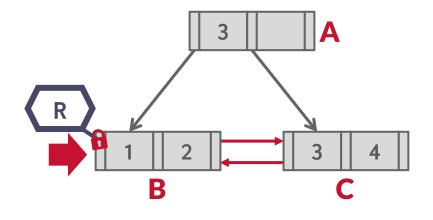




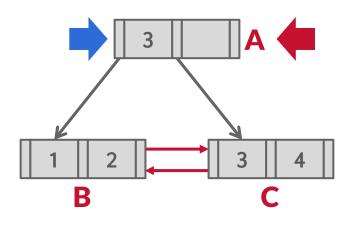






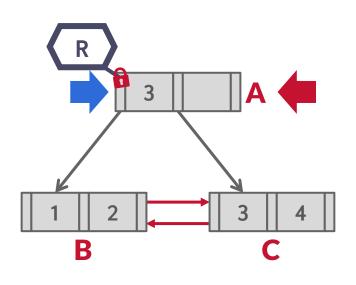




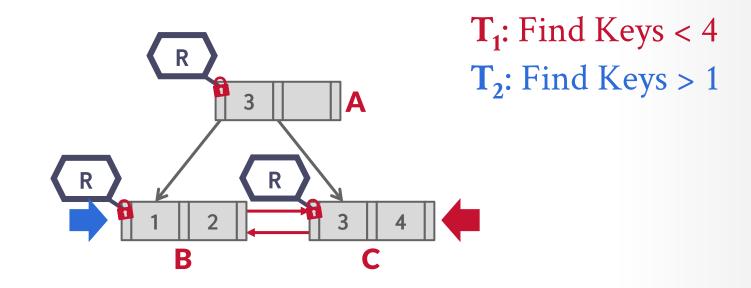


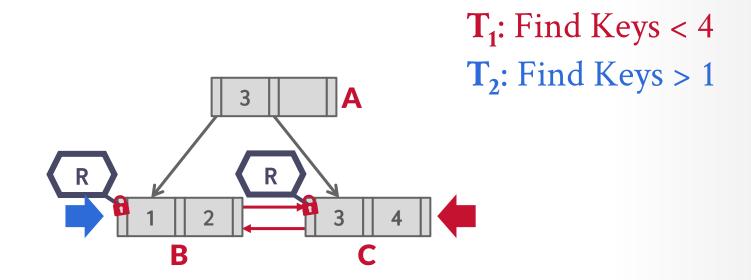
 T_1 : Find Keys < 4

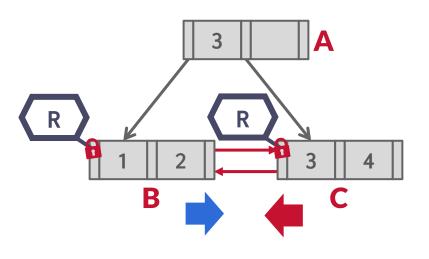
 T_2 : Find Keys > 1



 T_1 : Find Keys < 4 T_2 : Find Keys > 1







 T_1 : Find Keys < 4

 T_2 : Find Keys > 1

 T_1 : Find Keys < 4

Both T_1 and T_2 now hold this read latch.

Both T_1 and T_2 now hold this read latch.

R

Both T_1 and T_2 now hold this read latch.

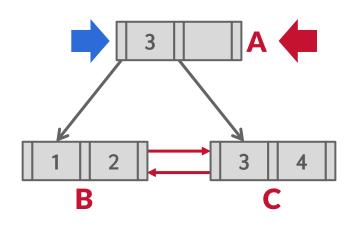
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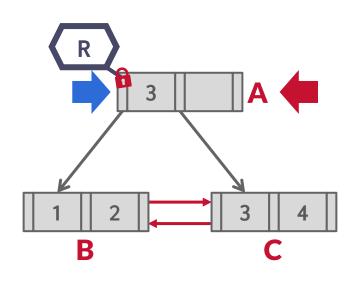


 T_1 : Find Keys < 4 T_2 : Find Keys > 1 T_1 : Find Keys > 1 T_2 : Find Keys > 1 T_3 : Find Keys > 1

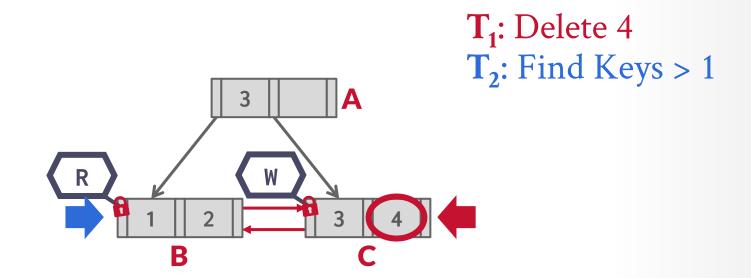


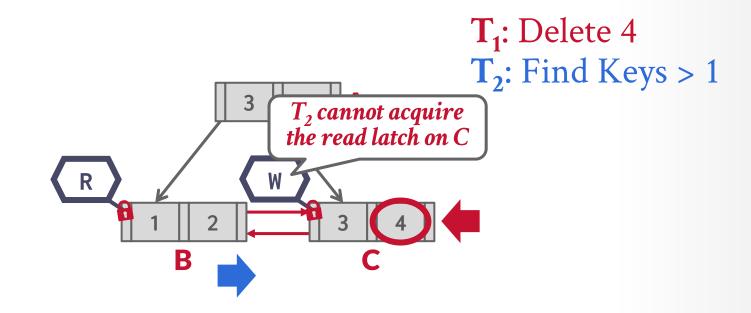


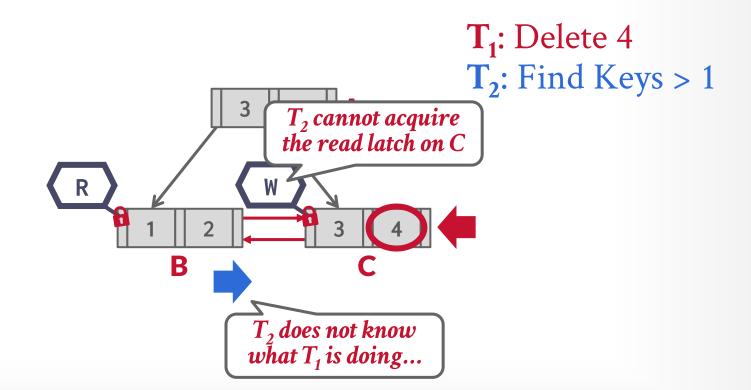
T₁: Delete 4
T₂: Find Keys > 1



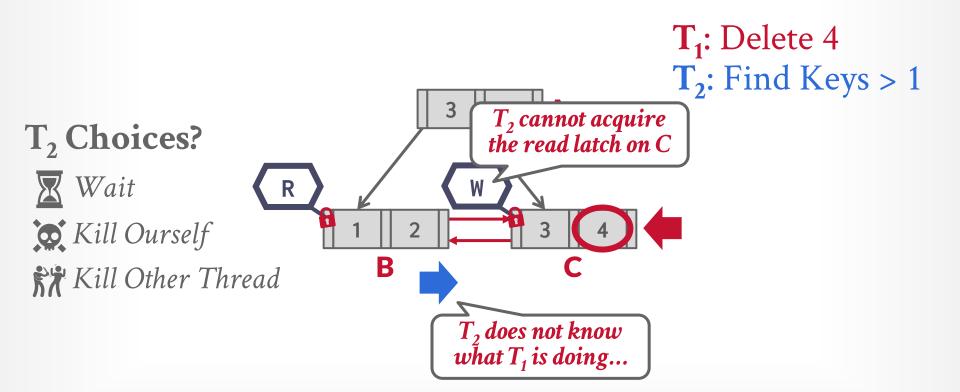
T₁: Delete 4
T₂: Find Keys > 1



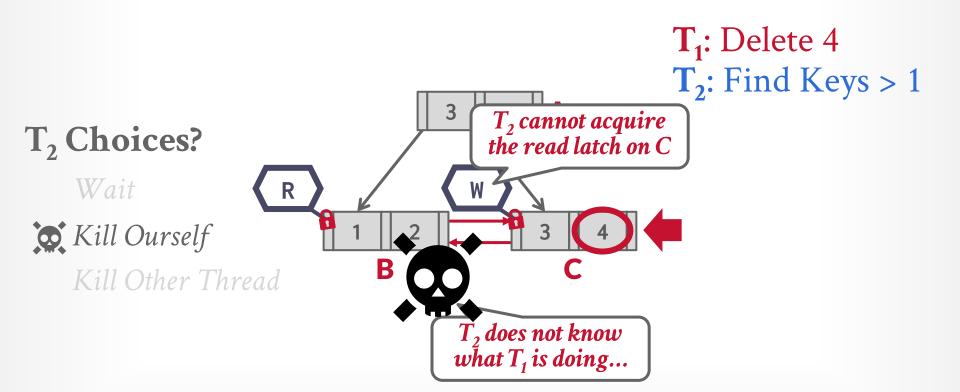














LEAF NODE SCANS

Latches do <u>not</u> support deadlock detection or avoidance. The only way we can deal with this problem is through coding discipline.

The leaf node sibling latch acquisition protocol must support a "no-wait" mode.

The DBMS's data structures must cope with failed latch acquisitions.

→ Usually transparent to end-user / application.



CONCLUSION

Making a data structure thread-safe is notoriously difficult in practice.

We focused on B+Trees, but the same high-level techniques are applicable to other data structures.



NEXT CLASS

We are finally going to discuss how to execute some queries...



PROJECT #2

You will build a thread-safe B+tree backed by your buffer pool manager.

- → Page Layout
- → Insert/Delete/Find Operations
- → Iterator
- → Latch Crabbing

We define the API for you. You need to provide the method implementations.



This is more difficult than Project #1.
Start immediately!



https://15445.courses.cs.cmu.edu/fall2024/project2

TASKS

Task #1: Page Layouts

- → How each node will store its key/values in a page.
- \rightarrow You only need to support unique keys.

Task #2: Operations

- → Support point queries (single key).
- → Support inserts with node splitting.
- → Support removal of keys with sibling stealing + merging.
- \rightarrow Does <u>not</u> need to be thread-safe.



TASKS

Task #3: Index Iterator

- → Create a STL iterator for range scans on leaf nodes.
- → You only need to support ascending scans.

Task #4: Concurrent Index

- → Introduce latch crabbing/coupling protocol to support safe concurrent operations.
- → Make sure you have splits / merges working correctly before proceeding with this task.



DEVELOPMENT HINTS

Follow the textbook semantics and algorithms.

Set the page size to be small (e.g., 512B) when you first start so that you can see more splits/merges.

Make sure that you protect the internal B+Tree root_page_id member.



EXTRA CREDIT

Gradescope Leaderboard runs your code with a specialized in-memory version of BusTub.

The top 20 fastest implementations in the class will receive extra credit for this assignment.

- \rightarrow #1: 50% bonus points
- \rightarrow #2–10: 25% bonus points
- \rightarrow #11–20: 10% bonus points

You must pass all the test cases to qualify!





PLAGIARISM WARNING



The homework and projects must be your own original work. They are <u>not</u> group assignments. You may <u>not</u> copy source code from other people or the web.

Plagiarism is <u>not</u> tolerated. You will get lit up.

→ Please ask me if you are unsure.

See <u>CMU's Policy on Academic Integrity</u> for additional information.

