

Homework #2 – Due Thursday, Jul. 19
STAT-UB.0001 – Statistics for Business Control

Problem 1

The U.S. Census Bureau reports the percentage of mothers in the workforce who have infant children. The following table gives a breakdown of the marital status and working status of the 1.8 million mothers with infant children in the year 2010. (The numbers in the table are in thousands.) A mother with infant children is to be selected randomly.

	Working	Not Working
Married and living with husband	1174	89
All other arrangements	416	121

Let A be the event “Mom with infant works”, and let B be the event “Mom with infant is married and living with husband”.

- (a) Find $P(A)$, $P(B)$, and $P(A | B)$.
- (b) Are the events A and B independent?
- (c) Find $P(B | A)$ and $P(B | A^c)$. Are they equal?

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Problem 2

The local area network (LAN) at Stern is temporarily shut down. Previous shutdowns have been due to hardware failure, software failure, or power failure. Maintenance engineers have determined that the probabilities of hardware, software, and power failures are 0.01, 0.05 and 0.02, respectively. They have also determined that if the system experiences hardware problems, LAN shuts down 73% of the time. Similarly, if software problems occur, LAN shuts down 12% of the time; and if power problems occur, LAN shuts down 88% of the time.

- (a) Express the information given in the problem statement as probabilities or conditional probabilities. Example: $P(\text{Hardware})=0.01$.
- (b) What is the probability that LAN will shutdown (in the future)?
- (c) Given the fact that LAN is shut down, what is the probability that the current shutdown is due to hardware failure? Software failure? Power failure?

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Problem 3

- (a) There are 3 male and 3 female students sitting in a row, and they chose their seats randomly. What is the probability of the event "No two males sit together and no two females sit together"? (Hint: The gender of the seated students can only be FMFMFM or MFMFMF.)
- (b) Compute the probability of randomly drawing five cards from a deck, and getting two Aces. (Hint: A deck has 52 cards, and 4 of them are Aces.)

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Problem 4

Consider the probability distribution function for the random variable X shown here:

x	10	20	30	40	50	60
$p(x)$	0.05	0.20	0.30	0.25	0.10	0.10

- (a) Find μ , σ^2 , and σ . Write down the formulas showing how do you get these numbers.
- (b) Use empirical rules with μ and σ to find the approximate 95% interval of the probability.
- (c) What is the probability that X will fall within the interval you just computed in (b)? (Hint: Use the PDF table.)

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