

Enzymatic reaction rate:  $r_p = k_3[KS]$  (I)

Since the initial concentration of E is the sum of the concentration of free E and the concentration of ES, that is:  $[E_0] = [E] + [ES]$  (II)

If the catalytic rate  $k_3$  is large, the ES complex will convert very quickly once it has been generated. At this point, it can be approximated that the ES is maintained at a lower concentration and remains essentially constant. Therefore, using the classical steady-state assumption in physicochemical kinetics, i.e. the ES production and elimination reach a dynamic equilibrium equation, therefore:

$$k_1[E][S] = k_2[ES] + k_3[ES] \quad \text{(III)}$$

It can be seen from (III):  $[E] = \frac{k_2+k_3}{k_1[S]} * [ES]$  (IV)

It can be seen from (II) and (IV):  $[E_0] = \frac{k_2+k_3+k_1[S]}{k_1[S]} * [ES]$

Therefore:  $[ES] = \frac{k_1[E_0][S]}{k_2+k_3+k_1[S]}$  (V)

It can be seen from (I) and (V):  $r_p = \frac{k_1k_3[E_0][S]}{k_2+k_3+k_1[S]}$