Indefinite integral & substitution method

1. Find the indefinite integral.

(a)
$$\int \left(\frac{x+1}{x}\right)^2 dx$$

(b)
$$\int \frac{x^2}{x^2 + 1} dx$$

2. Use substitution method to find the integral.

(a)
$$\int \cot(x) dx$$

(b)
$$\int \frac{x}{x^4 + 1} \, dx$$

(c)
$$\int x^2 \sqrt{x+1} \ dx$$

(d)
$$\int \frac{e^x + 1}{e^x + x} \, dx$$

3. Substitution for definite integrals.

(a)
$$\int_0^1 \frac{e^x + 1}{e^x + x} \, dx$$

(b)
$$\int_0^2 x\sqrt{4-x^2} \, dx$$

(c)
$$\int_{1}^{2} \frac{e^{1/x}}{x^2} dx$$

(d)
$$\int_0^1 \frac{1}{(1+\sqrt{x})^2} dx$$