

**Tenth-order lepton  $g-2$ :  
Contribution from diagrams containing a sixth-order  
light-by-light-scattering subdiagram internally**

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### Abstract

This paper reports the result of our evaluation of the tenth-order QED correction to the lepton  $g-2$  from Feynman diagrams which have sixth-order light-by-light-scattering subdiagrams, none of whose vertices couple to the external magnetic field. The gauge-invariant set of these diagrams, called Set II(e), consists of 180 vertex diagrams. In the case of the electron  $g-2$  ( $a_e$ ), where the light-by-light subdiagram consists of the electron loop, the contribution to  $a_e$  is found to be  $-1.344\,9\,(10)(\alpha/\pi)^5$ . The contribution of the muon loop to  $a_e$  is  $-0.000\,465\,(4)(\alpha/\pi)^5$ . The contribution of the tau-lepton loop is about two orders of magnitudes smaller than that of the muon loop and hence negligible. The sum of all of these contributions to  $a_e$  is  $-1.345\,(1)(\alpha/\pi)^5$ . We have also evaluated the contribution of Set II(e) to the muon  $g-2$  ( $a_\mu$ ). The contribution to  $a_\mu$  from the electron loop is  $3.265\,(12)(\alpha/\pi)^5$ , while the contribution of the tau-lepton loop is  $-0.038\,06\,(13)(\alpha/\pi)^5$ . The total contribution to  $a_\mu$ , which is the sum of these two contributions and the mass-independent part of  $a_e$ , is  $1.882\,(13)(\alpha/\pi)^5$ .

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