



FIG. 3: The ratio of linear density perturbations  $\delta_{\text{fRG}}/\delta_{\Lambda\text{CDM}}(k = 0.174h\text{Mpc}^{-1})$  as a function of redshift for three different values of  $\lambda$  with  $n = 2$ .

$(\delta_{\text{fRG}}/\delta_{\Lambda\text{CDM}})^2(k = 0.174h\text{Mpc}^{-1}) \lesssim 1.1$ . Although we neglect non-linear effects here, the difference between linear calculation and non-linear N-body simulation remained smaller than 5% at the wavenumber  $0.174h\text{Mpc}^{-1}$ [32].

Figures 4 represent  $(\delta_{\text{fRG}}/\delta_{\Lambda\text{CDM}})^2(k = 0.174h\text{Mpc}^{-1})$  as a function of  $\lambda$  for  $n = 2, 3$ , and 4. From the analytic formula (19), this  $\lambda$  dependence would have the form  $(\delta_{\text{fRG}}/\delta_{\Lambda\text{CDM}})^2 \propto C^2(k) \propto \lambda^{-\frac{(2n-p_n+1)(\sqrt{33}-5)}{4(3n+2)}}$  which is depicted by a broken line in each figure. This curve, however, does not match the asymptotic behaviour  $(\delta_{\text{fRG}}/\delta_{\Lambda\text{CDM}})^2 \rightarrow 1$  for large  $\lambda$ . We find that an exponential function

$$(\delta_{\text{fRG}}/\delta_{\Lambda\text{CDM}})^2 = 1 + b_n e^{-q_n \lambda} \quad (29)$$

fits the numerical calculation very well with  $(n, b_n, q_n) = (2, 0.47, 0.19)$ ,  $(3, 0.43, 0.49)$ , and  $(4, 0.39, 0.70)$ , respectively. From these figures, in order to keep deviation from  $\Lambda\text{CDM}$  model smaller than 10% at  $k = 0.174h\text{Mpc}^{-1}$ , we find  $\lambda$  should be larger than 8.2, 3.0, and 1.9 for  $n = 2, 3$ , and 4, respectively.

From these analysis, we can constrain the parameter space as Fig. 5. The region which