

d (including $d = 2$), and that every solution has the form $\pm(x_n, y_n)$ where $x_n + \sqrt{d}y_n = (x_1 + \sqrt{d}y_1)^n$ for some solution (x_1, y_1) and $n \in \mathbb{Z}$.

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