移动通信第三次作业

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1. 由题可知

$$(d')^2 = d^2 + (h_t - h_r)^2 \tag{1}$$

得

$$d' = \sqrt{d^2 + (h_t - h_r)^2} \tag{2}$$

$$(d'')^2 = d^2 + (h_t + h_r)^2 (3)$$

得

$$d'' = \sqrt{d^2 + (h_t + h_r)^2} \tag{4}$$

得

$$\Delta = d'' - d' \tag{5}$$

$$= \sqrt{d^2 + (h_t + h_r)^2} - \sqrt{d^2 + (h_t - h_r)^2}$$
 (6)

$$= d * (\sqrt{1 + (\frac{h_t + h_r}{d})^2} - 1) - d * (\sqrt{1 + (\frac{h_t - h_r}{d})^2} - 1)$$
 (7)

(8)

又因为

$$(1+x)^a - 1 \sim ax \tag{9}$$

当且仅当 $x \to 0$ 时成立所以 $d \gg (h_t + h_r)$

$$\Delta = d'' - d' \tag{10}$$

$$=\frac{2h_t h_r}{d} \tag{11}$$

当且仅当 $d \gg (h_t + h_r)$ 时成立

2. 因为

$$p_r(d) \propto d^{-3.5} \tag{12}$$

且

$$pr(1) = 1mw (13)$$

所以

$$p_r(d) = d^{-3.5}mw (14)$$

所以

$$p_r(10) = 0.316mw (15)$$

$$p_r(10)[db] = -35db (16)$$

$$\tilde{p_r}(10) = p_r(10) + x_\sigma(db)$$
 (17)

所以

$$\sigma = 7.75db \tag{18}$$

3. (a) 设 p_i 为在 d_i 处的接受功率, $\hat{p_i}$ 为估计值

$$\hat{p}_i(d) = p(d_0) - 10n \log(\frac{d_i}{d_0}) \tag{19}$$

$$\hat{p_1} = 0dbm \tag{20}$$

$$\hat{p_2} = -3n \tag{21}$$

$$\hat{p}_3 = -10n \tag{22}$$

$$\hat{p_4} = -13n \tag{23}$$

$$T(n) = \sum_{i=1}^{4} (p_i - \hat{p}_i)^2$$
 (24)

$$=278n^2 - 1838n + 3294\tag{25}$$

(26)

解得

$$n = 3.3 \tag{27}$$