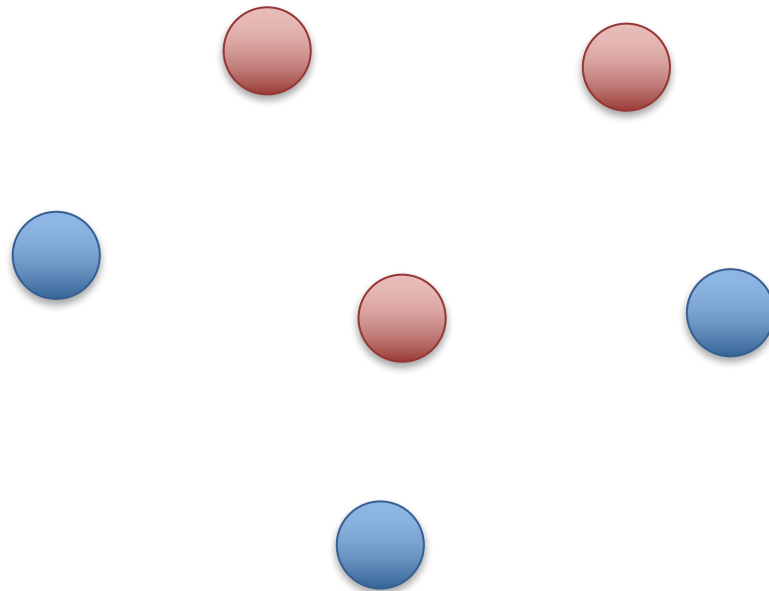
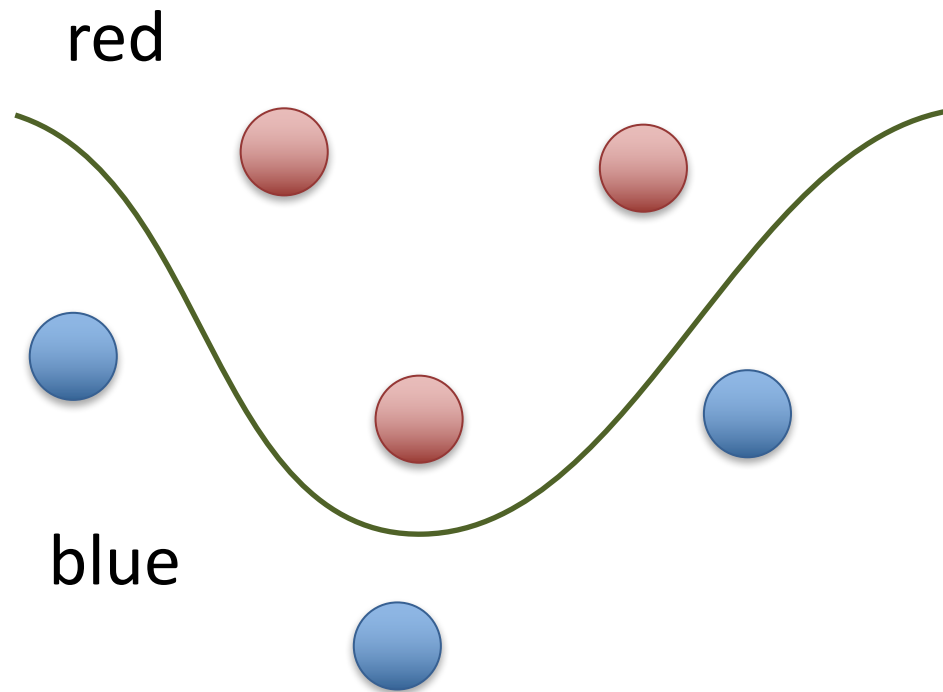


A major risk in classification: overfitting

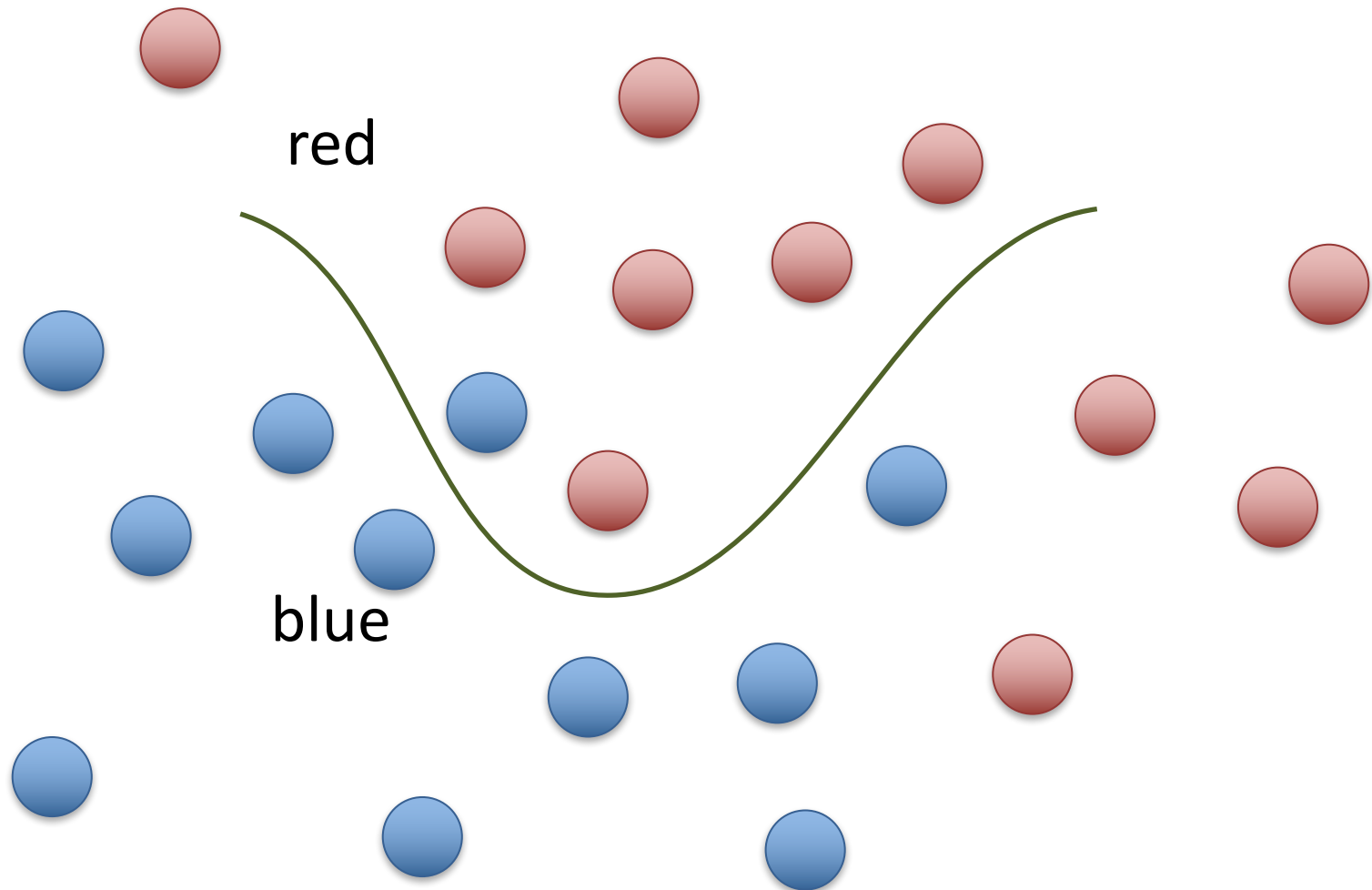
Assume we have a small data set



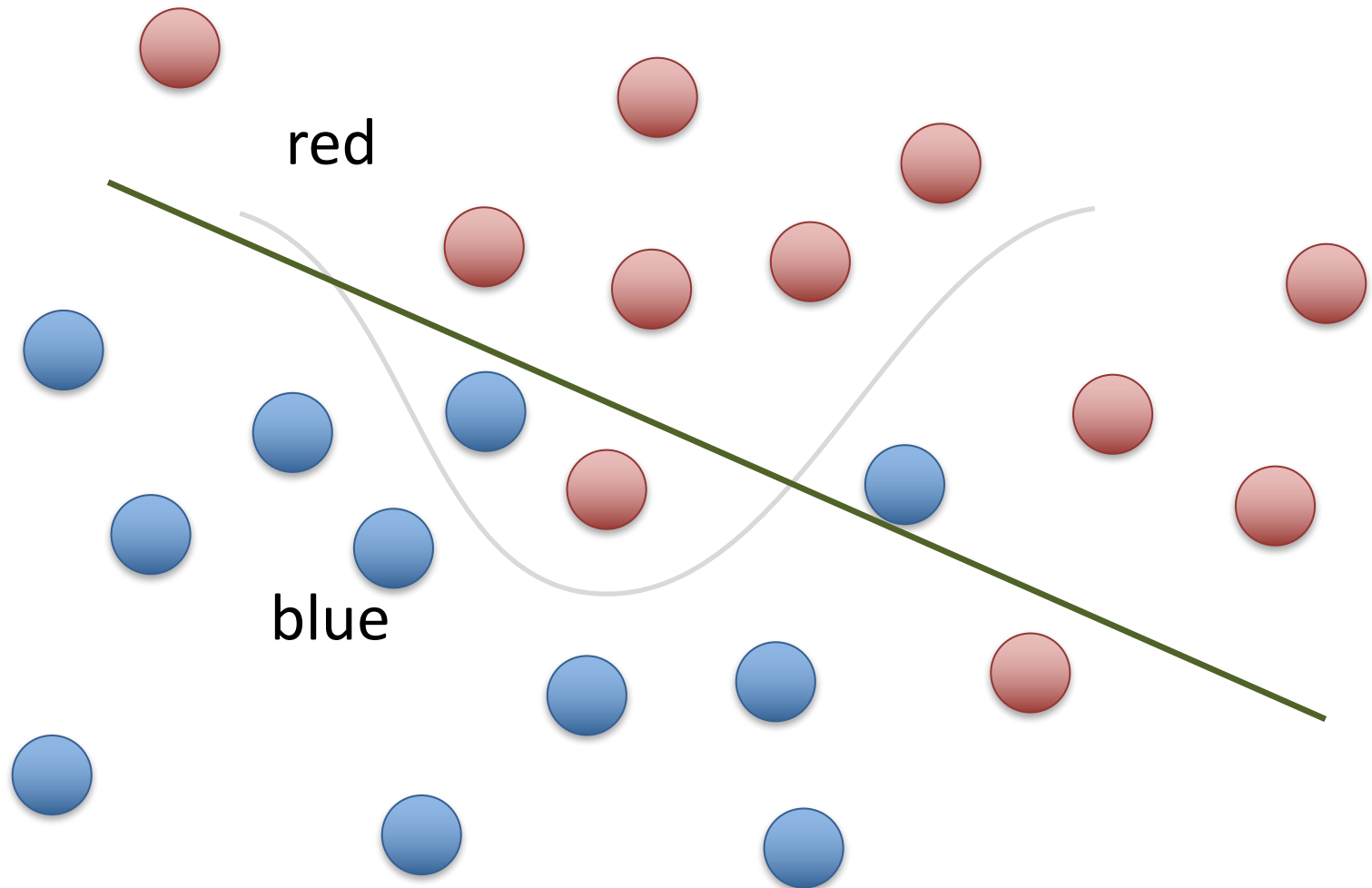
# We fit a model that separates red and blue



When more data becomes available, we see that the model is poor

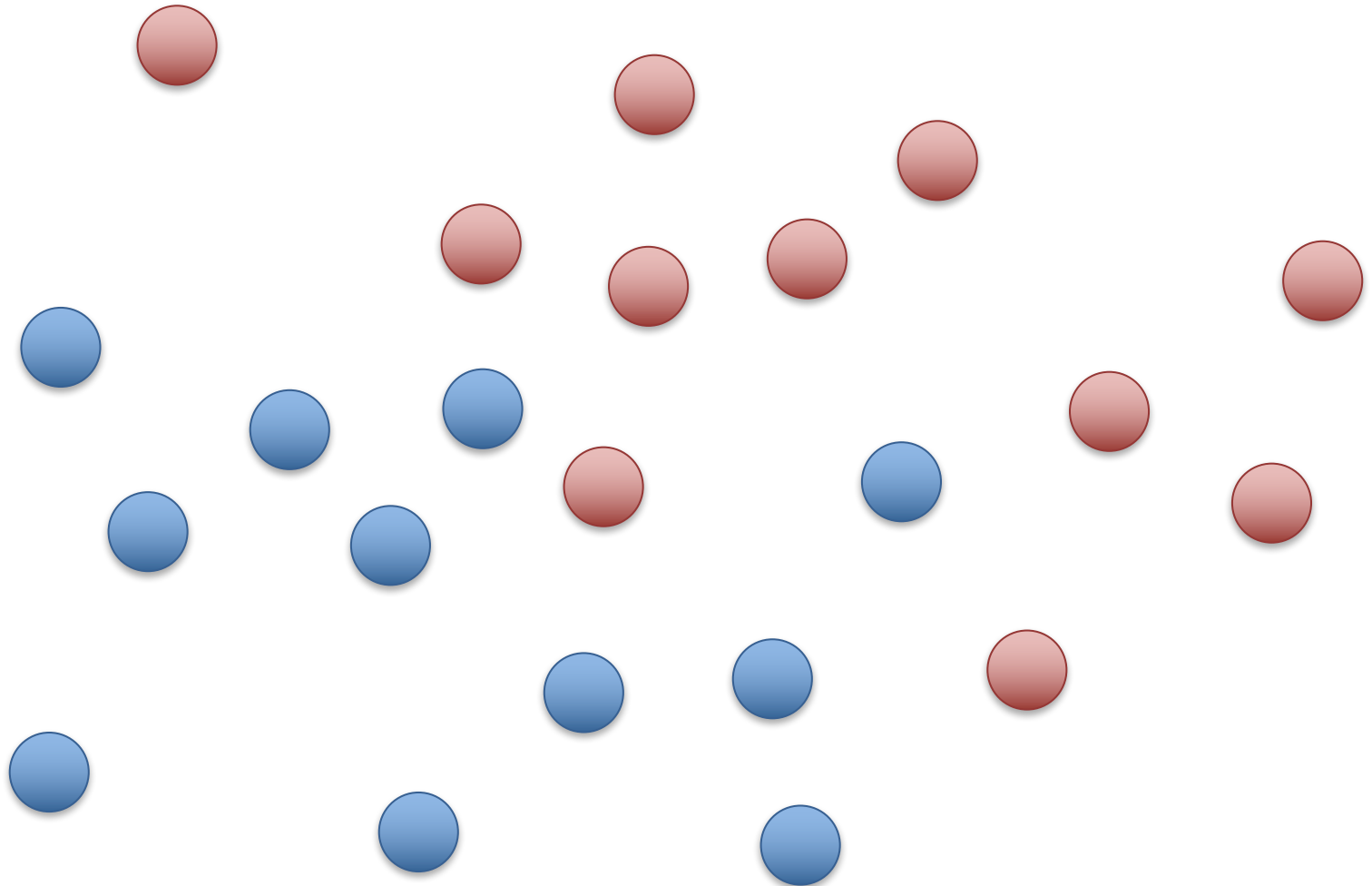


# A simpler model might have worked better

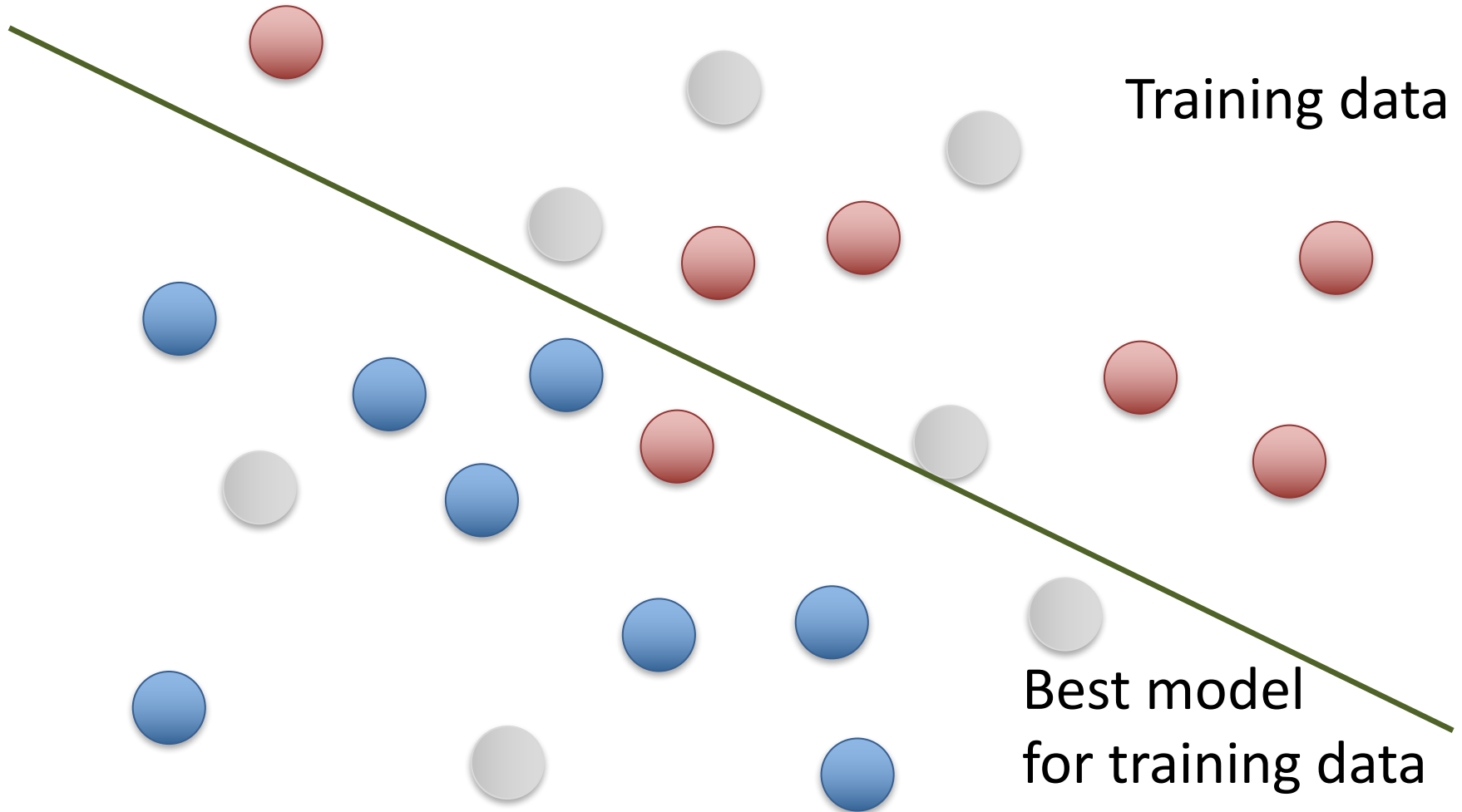


A predictor always works best on the data set on which it was trained!

# Solution: divide data into training and test sets

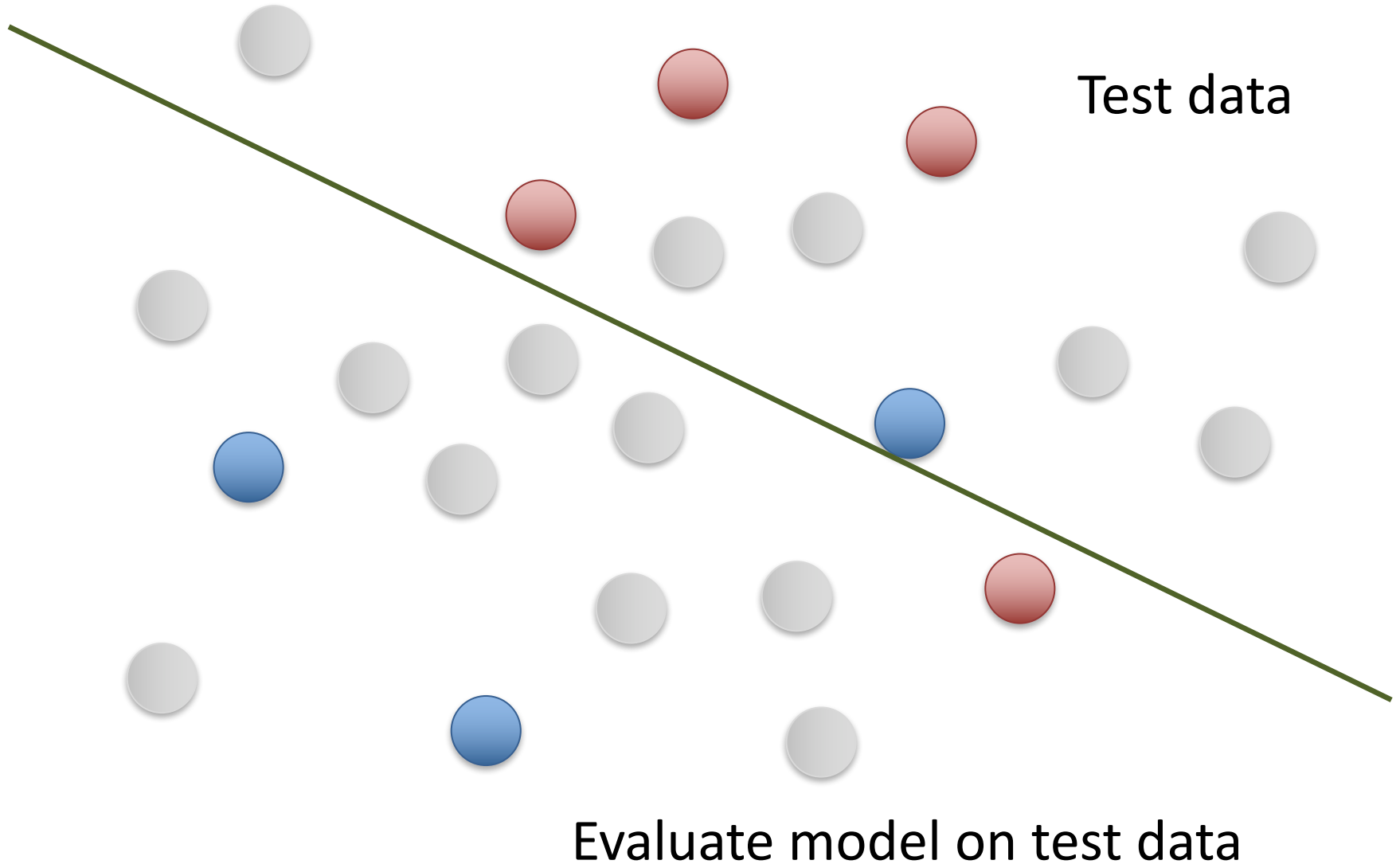


# Solution: divide data into training and test sets





# Solution: divide data into training and test sets



# Frequently used approach: $k$ -fold cross-validation

- Divide data into  $k$  equal parts
- Use  $k-1$  parts as training set, 1 as test set
- Repeat  $k$  times, so each part has been used once as test set

## Also: Leave-one-out cross-validation

- Fit model on  $n-1$  data points
- Evaluate on remaining data point
- Repeat  $n$  times, so each point has been left out once

# And: Repeated random sub-sampling validation

- Randomly split data into training and test data sets
- Train model on training set, evaluate on test set
- Repeat multiple times, average over result

# Random sub-sampling in R

```
# We assume our data are stored in data table called `data`.
```

# Random sub-sampling in R

```
# We assume our data are stored in data table called `data`.  
  
# Fraction of data used for training purposes (here: 40%)  
train_fraction <- 0.4
```

# Random sub-sampling in R

```
# We assume our data are stored in data table called `data`.  
  
# Fraction of data used for training purposes (here: 40%)  
train_fraction <- 0.4  
# Number of observations in training set  
train_size <- floor(train_fraction * nrow(data))
```

# Random sub-sampling in R

```
# We assume our data are stored in data table called `data`.

# Fraction of data used for training purposes (here: 40%)
train_fraction <- 0.4
# Number of observations in training set
train_size <- floor(train_fraction * nrow(data))
# Indices of observations to be used for training
train_indices <- sample(1:nrow(data), size = train_size)
```



# Random sub-sampling in R

```
# We assume our data are stored in data table called `data`.

# Fraction of data used for training purposes (here: 40%)
train_fraction <- 0.4
# Number of observations in training set
train_size <- floor(train_fraction * nrow(data))
# Indices of observations to be used for training
train_indices <- sample(1:nrow(data), size = train_size)

# Extract training and test data
train_data <- data[train_indices, ] # get training data
test_data <- data[-train_indices, ] # get test data
```