Title: "Elementary and high school students performance and relation to the district education finance " -GA Final Project Research proposal Author: Yu Zhang output:

1. Introduction

In the discussion of K-12 students' success, the issue of financing is prominent from the perspective of various stakeholders. Policymakers are engaged in asking how much public purse should be devoted to elementary and high school students related to competing demands on tuition, expenditure, and transportation. Federal education and census are concerned about the financial capacity to provide quality education and sustain the living hood. Besides, the family and students concerned about how they pay for education can guarantee the students' success beyond elementary and high school.

In observing the NAEP (National Assessment of Educational Progress) data and Educational financing data from the National Finance Census (National Center for Educational Statistics), we have been known the educational finance can be characterized by the goals of students' academic success, and by a strong influence by the financial capacity, by and large, we might predict the elementary and high school students academic success on mathematics and literacy to be influenced by the features of family and federal educational financing, this is for example, highly praise by educational scholar and researcher Joan Herman'description: "the keys resources, educational financing have been imposed the role to expand the enrollment and institutes. On the performance standards, the evaluation can be introduced to predict the student's performance" (2011).

```
In [1]:
    import pandas as pd
    import numpy as np
    import seaborn as sns
    import matplotlib.pyplot as plt
    from sklearn.metrics import r2_score
    import statsmodels.api as sm
    %matplotlib inline

    from sklearn.linear_model import Ridge, Lasso, ElasticNet, LinearRegression
    from sklearn.model_selection import cross_val_score

plt.rcParams['figure.figsize'] = (8, 6)
    plt.rcParams['font.size'] = 14
    plt.style.use("fivethirtyeight")

from sklearn.linear_model import LinearRegression
```

```
In [3]: districts.head()
```

Out[3]:

	STATE	ENROLL	NAME	YRDATA	TOTALREV	TFEDREV	TSTREV	TLOCREV	TOTALEXP
() Alabama	9609.0	AUTAUGA COUNTY SCHOOL DISTRICT	2016	80867	7447	53842	19578	76672
1	I Alabama	30931.0	BALDWIN COUNTY SCHOOL DISTRICT	2016	338236	23710	145180	169346	299880
2	2 Alabama	912.0	BARBOUR COUNTY SCHOOL DISTRICT	2016	10116	2342	5434	2340	10070
3	3 Alabama	2842.0	EUFAULA CITY SCHOOL DISTRICT	2016	26182	3558	15900	6724	29843
4	I Alabama	3322.0	BIBB COUNTY SCHOOL DISTRICT	2016	32486	3664	21846	6976	31662

In [10]: districts_new2.head()

Out[10]:		year	state	name	enrollment	total_revenue	federal_revenue	state_revenue	local_rev
					mean	mean	mean	mean	1
	0	1993	Alabama	ALBERTVILLE CITY SCH DIST	3011.0	11101.0	879.0	7403.0	2
	1	1993	Alabama	ALEXANDER CITY SCH DIST	3748.0	14406.0	982.0	8949.0	4
	2	1993	Alabama	ANDALUSIA CTY SCH DIST	2136.0	7749.0	949.0	5023.0	1
	3	1993	Alabama	ANNISTON CTY SCH DST	4164.0	17714.0	3084.0	10615.0	4
	4	1993	Alabama	ARAB CIT SCHOOL DIST	2485.0	8296.0	492.0	5834.0	1

```
In [11]: districts_new2.columns = ('year', 'state', 'name', 'enrollment', 'total_revenu
In [12]: districts_new2.shape
Out[12]: (356945, 13)
In [13]: districts_new3 = districts_new2[districts_new2.federal_revenue > 50000]
In [14]: districts_new3.shape
Out[14]: (2123, 13)
In [15]: districts_new3.dtypes
Out[15]: year
                                            int64
                                           object
         state
         name
                                           object
         enrollment
                                          float64
         total revenue
                                          float64
         federal_revenue
                                          float64
         state_revenue
                                          float64
         local revenue
                                          float64
         expenditure
                                          float64
         current_spending_instruction
                                          float64
         current_spending
                                          float64
         other_spending
                                          float64
         total_capital
                                          float64
         dtype: object
```

In [16]: districts_new3.info()

<class 'pandas.core.frame.DataFrame'>
Int64Index: 2123 entries, 1059 to 356696
Data columns (total 13 columns):

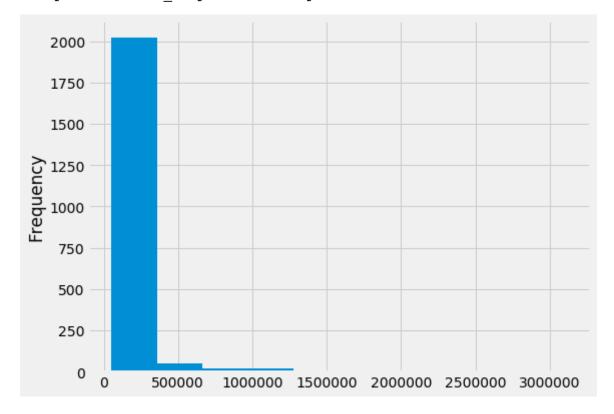
#	Column	Non-Null Count	Dtype
0	year	2123 non-null	int64
1	state	2123 non-null	object
2	name	2123 non-null	object
3	enrollment	2123 non-null	float64
4	total_revenue	2123 non-null	float64
5	federal_revenue	2123 non-null	float64
6	state_revenue	2123 non-null	float64
7	local_revenue	2123 non-null	float64
8	expenditure	2123 non-null	float64
9	current_spending_instruction	2123 non-null	float64
10	current_spending	2123 non-null	float64
11	other_spending	2123 non-null	float64
12	total_capital	2123 non-null	float64
-1 L	floot(1/10) int(1/1)	a = + (2)	

dtypes: float64(10), int64(1), object(2)

memory usage: 232.2+ KB

In [17]: districts_new3.federal_revenue.plot(kind = 'hist')

Out[17]: <matplotlib.axes._subplots.AxesSubplot at 0x1f7508f9248>

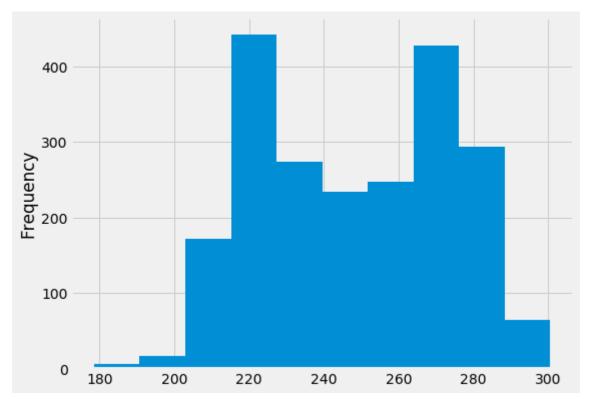


The featueres are extremely right skewed; majority fundings are densed on small amount range, set up the data range

```
In [18]: districts_f = districts_new3[districts_new3.year > 1995 ]
```

```
In [19]: districts_f.shape
Out[19]: (2057, 13)
In [20]: naep.columns=('year', 'state', 'score', 'test_subject', 'grade')
In [21]: naep.score = pd.to_numeric(naep['score'],errors='coerce')
In [22]: naep.score.plot(kind = 'hist') ##NAEP data are normaly distributed
```

Out[22]: <matplotlib.axes._subplots.AxesSubplot at 0x1f7509fdfc8>



In [23]:
 naep.head()

Out[23]:

	year	state	score	test_subject	grade
0	2017	Alabama	232.170688	Mathematics	4
1	2017	Alaska	230.456278	Mathematics	4
2	2017	Arizona	234.435788	Mathematics	4
3	2017	Arkansas	233.848144	Mathematics	4
4	2017	California	232.262941	Mathematics	4

```
In [24]: eduf = pd.merge(districts_new3, naep, on = ['year','state'])
eduf.head()
```

Out[24]:

	year	state	name	enrollment	total_revenue	federal_revenue	state_revenue	local_reve
c	1994	California	LOS ANGELES CO OFF OF EDUCATION	0.0	329287.0	114874.0	124991.0	894
1	1994	California	LOS ANGELES UNIF SCH DIST	639129.0	3813590.0	475847.0	2428837.0	9089
2	1994	California	SAN DIEGO CITY UNIF SCH DIST	127258.0	735898.0	59809.0	297470.0	3786
3	1994	District of Columbia	DC PUBLIC SCHOOLS	80678.0	735720.0	79432.0	0.0	6562
4	1994	Florida	BROWARD CO SCHOOL DIST	189862.0	1217958.0	73252.0	617046.0	5276

```
In [25]: eduf.to_csv(r'data/edu_data.csv')
```

In [26]: ## total revenue, state revenue, adn expenditure are on odd range
missing the unit information to transform the data
suggest drop

In [361]: eduf.head()

Out[361]:

	year	state	name	enrollment	total_revenue	federal_revenue	state_revenue	local_reve
0	1994	California	LOS ANGELES CO OFF OF EDUCATION	0.0	329287.0	114874.0	124991.0	894
1	1994	California	LOS ANGELES UNIF SCH DIST	639129.0	3813590.0	475847.0	2428837.0	9089
2	1994	California	SAN DIEGO CITY UNIF SCH DIST	127258.0	735898.0	59809.0	297470.0	3786
3	1994	District of Columbia	DC PUBLIC SCHOOLS	80678.0	735720.0	79432.0	0.0	6562
4	1994	Florida	BROWARD CO SCHOOL DIST	189862.0	1217958.0	73252.0	617046.0	5276

##education EDA visualization

In [362]: eduf.corr()

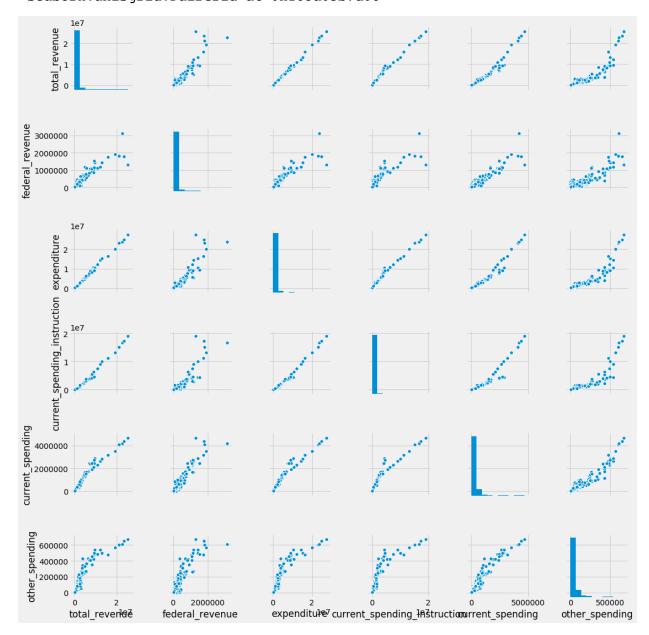
Out[362]:

	year	enrollment	total_revenue	federal_revenue	state_revenue lo
year	1.000000	-0.176945	-0.039407	-0.024318	-0.058719
enrollment	-0.176945	1.000000	0.902879	0.868165	0.902086
total_revenue	-0.039407	0.902879	1.000000	0.917869	0.958876
federal_revenue	-0.024318	0.868165	0.917869	1.000000	0.903667
state_revenue	-0.058719	0.902086	0.958876	0.903667	1.000000
local_revenue	-0.019887	0.815687	0.952118	0.816075	0.829721
expenditure	-0.042459	0.904216	0.998196	0.914874	0.954947
current_spending_instruction	-0.027907	0.860274	0.988210	0.884147	0.928328
current_spending	-0.057108	0.941326	0.971238	0.925755	0.955879
other_spending	-0.091002	0.951188	0.911038	0.898340	0.918368
total_capital	-0.079319	0.863639	0.919154	0.853129	0.903232
score	0.155699	-0.018320	0.007067	-0.002246	-0.002641
grade	0.019577	-0.005029	-0.000797	-0.000416	-0.000915

##heat map indicated poor correlation between score and enrollment and features

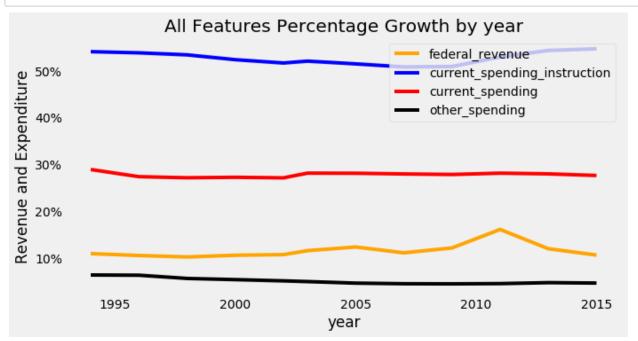
In [381]: sns.pairplot(eduf[['total_revenue','federal_revenue','expenditure','current

Out[381]: <seaborn.axisgrid.PairGrid at 0x183a05b7d08>



```
In [202]: ##feature EDA
In [33]: by_year = eduf.groupby('year')['total_revenue','federal_revenue','expenditu
          C:\Users\zhang\anaconda3\lib\site-packages\ipykernel launcher.py:1: Futur
          eWarning: Indexing with multiple keys (implicitly converted to a tuple of
          keys) will be deprecated, use a list instead.
            """Entry point for launching an IPython kernel.
 In [27]: plt.plot(by year['total_revenue'], color='red')
          plt.plot(by_year['federal_revenue'], color='orange', label='federal revenue
          plt.plot(by_year['expenditure'], color='green')
          plt.plot(by year['current spending instruction'], color='blue')
          plt.plot(by year['current spending'], color='grey')
          plt.plot(by_year['other_spending'], color='black')
          plt.legend(['total revenue', 'federal revenue', 'expenditure', 'current spendi
          plt.grid(b=None)
          plt.xlabel('year')
          plt.ylabel('Revenue')
          plt.title('All Features Growth by year')
          plt.savefig('data/features by year.png', transparent=True,dpi=300, bbox inc
          plt.show()
          NameError
                                                    Traceback (most recent call las
          <ipython-input-27-4862f67c1388> in <module>
          ---> 1 plt.plot(by year['total revenue'], color='red')
                2 plt.plot(by_year['federal_revenue'], color='orange', label='feder
          al revenue')
                3 plt.plot(by year['expenditure'], color='green')
                4 plt.plot(by year['current spending instruction'], color='blue')
                5 plt.plot(by year['current spending'], color='grey')
          NameError: name 'by_year' is not defined
 In [44]: import matplotlib.ticker as mtick
```

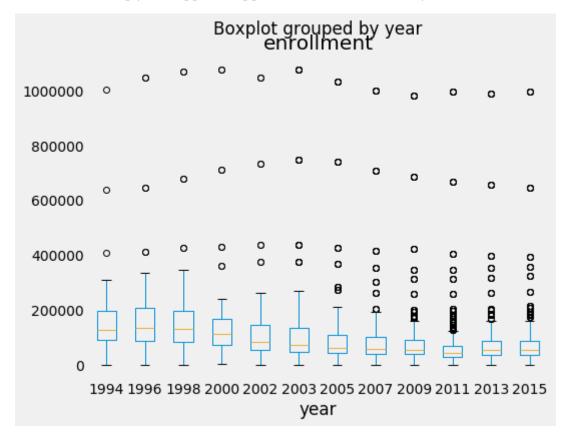
```
In [48]:
         ##percentage break down
         by_year['current_spending_percentage'] = by_year['current_spending'] / by_y
         by year['federal revenue percentage'] = by year['federal revenue'] / by yea
         by year['current spending instruction percentage'] = by year['current spend
         by year['other spending percentage'] = by year['other spending'] / by year[
         ax = plt.subplots(1, 1, figsize=(10,5))
         p1 = plt.plot(by_year['federal_revenue_percentage'], color='orange', label=
         p2 = plt.plot(by year['current spending instruction percentage'], color='bl
         p3 = plt.plot(by_year['current_spending_percentage'], color='red')
         p4 = plt.plot(by year['other spending percentage'], color='black')
         plt.legend(['federal revenue','current spending instruction','current spend
         plt.grid(b=None)
         plt.gca().yaxis.set_major_formatter(mtick.PercentFormatter(1.0))
         plt.xlabel('year')
         plt.ylabel('Revenue and Expenditure')
         plt.title('All Features Percentage Growth by year')
         plt.savefig('data/feature_pct.png', dpi=300, bbox_inches='tight')
         plt.show()
```

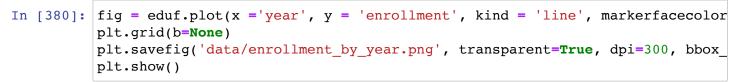


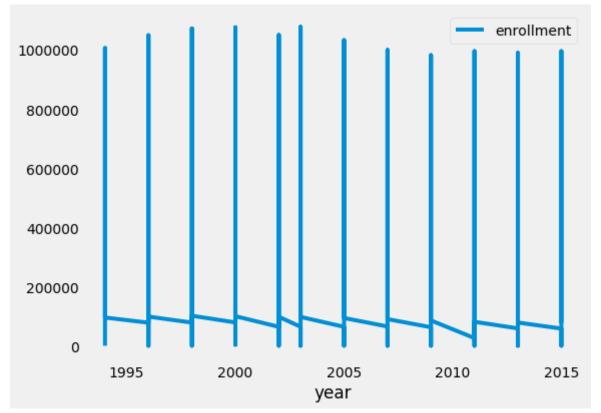
```
In [30]: # Box plot of score, grouped by season
    eduf.boxplot(column='enrollment', by='year')
    plt.grid(b=None)
    plt.savefig('data/enrollment_box.png', transparent=True,dpi=300, bbox_inche
    plt.show()
```

C:\Users\zhang\anaconda3\lib\site-packages\numpy\core_asarray.py:83: Vis ibleDeprecationWarning: Creating an ndarray from ragged nested sequences (which is a list-or-tuple of lists-or-tuples-or ndarrays with different l engths or shapes) is deprecated. If you meant to do this, you must specify 'dtype=object' when creating the ndarray

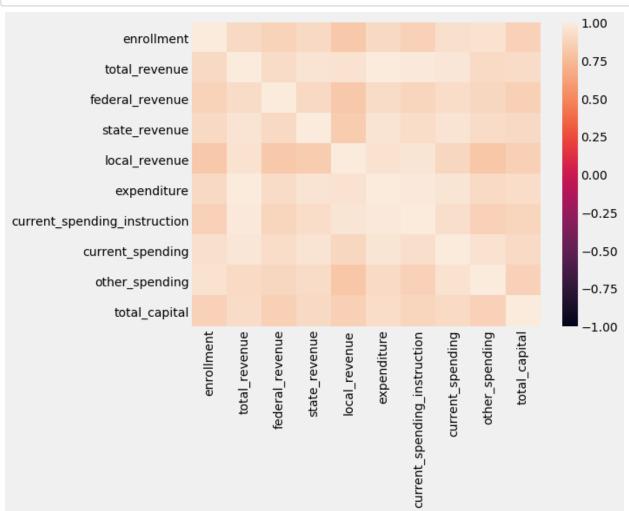
return array(a, dtype, copy=False, order=order)







```
In [372]: sns.heatmap(eduf.drop(['year', 'score', 'grade'], axis = 1).corr(), vmin=-1,
    plt.savefig('data/heatmap.png', transparent=True, dpi=300, bbox_inches='tigh
    plt.grid(b=None)
    plt.show()
```



```
In [75]: # Create X and y.
X = eduf[feature_cols]
y = eduf.enrollment
```

```
In [390]: X2 = sm.add_constant(X)
    est = sm.OLS(y, X2)
    est2 = est.fit()
    print(est2.summary())
    pdf.output("data/regression.pdf")
```

OLS Regression Results ______ enrollment R-squared: Dep. Variable: 0.924 Model: OLS Adj. R-squared: 0.924 Method: Least Squares F-statistic: 7784. Date: Sat, 13 Feb 2021 Prob (F-statistic): 0.00 Time: 18:41:33 Log-Likelihood: -45890. No. Observations: 9.17 3855 AIC: 9e+04 Df Residuals: 3848 BIC: 9.18 4e+04 Df Model: Covariance Type: nonrobust ______ coef std err t P>|t| [0.025 0.975] 4230.3263 814.701 5.192 0.000 const 2633.039 5827.613 -0.0724 0.005 -13.166 0.000 total revenue -0.062 -0.083 0.000 federal revenue -0.0502 0.008 -6.654-0.065 -0.035 expenditure 0.0493 0.006 8.693 0.000 0.038 0.060 current_spending_instruction 0.0159 0.006 2.781 0.005 0.005 0.027 0.1727 current spending 0.010 16.700 0.000 0.152 0.193 other spending 1.0255 0.027 38.685 0.000 0.974 1.077 ===== 2230.006 Omnibus: Durbin-Watson: 0.582 0.000 Prob(Omnibus): Jarque-Bera (JB): 13607 1.575 Skew: 1.988 Prob(JB): 0.00 31.833 Cond. No. 5.1 Kurtosis: 7e+06 ______

```
Warnings:
```

- [1] Standard Errors assume that the covariance matrix of the errors is correctly specified.
- [2] The condition number is large, 5.17e+06. This might indicate that the re are

strong multicollinearity or other numerical problems.

```
NameError
                                                             Traceback (most recent call las
            t)
            <ipython-input-390-c8bad0a8b594> in <module>
                   3 \text{ est2} = \text{est.fit()}
                   4 print(est2.summary())
            ---> 5 pdf.output("data/regression.pdf")
            NameError: name 'pdf' is not defined
 In [77]:
           ##scatter plots of all correlation
            feature cols1 = ['total revenue', 'federal revenue', 'expenditure', 'current sp
 In [78]: ##build linear regression for prediction
 In [79]: X = eduf[feature cols1]
           y = eduf.enrollment
In [268]: X.describe()
Out[268]:
                   total_revenue federal_revenue
                                               expenditure current_spending_instruction current_spending
            count 3.855000e+03
                                 3.855000e+03 3.855000e+03
                                                                       3.855000e+03
                                                                                       3.855000e+03
             mean 1.079346e+06
                                 1.325096e+05 1.107774e+06
                                                                       5.827077e+05
                                                                                       3.089959e+05
              std 1.989207e+06
                                 2.122858e+05 2.131881e+06
                                                                       1.375229e+06
                                                                                       4.353089e+05
                                                                                       1.801900e+04
              min
                  7.708900e+04
                                 5.001900e+04 3.525100e+04
                                                                       8.220000e+02
                                                                                       1.318020e+05
                  4.392340e+05
                                 6.074900e+04 4.355470e+05
                                                                       2.242330e+05
              25%
                                                                       3.122830e+05
                                                                                       1.921970e+05
              50% 6.131440e+05
                                 7.725900e+04 6.211730e+05
              75% 1.065630e+06
                                 1.138840e+05 1.062236e+06
                                                                       5.418120e+05
                                                                                       3.224060e+05
              max 2.543738e+07
                                 3.120314e+06 2.747789e+07
                                                                       1.903582e+07
                                                                                       4.694906e+06
In [269]: |y.isnull().sum()
Out[269]: 0
In [270]: y.fillna(0, inplace=True)
```

```
In [271]: X.isnull().sum()
                                                0
Out[271]: total revenue
           federal_revenue
                                                0
           expenditure
                                                0
           current_spending_instruction
                                                0
                                                0
           current_spending
           other_spending
                                                0
           dtype: int64
In [272]: print((X.dtypes))
                                                float64
           total revenue
           federal_revenue
                                                float64
           expenditure
                                                float64
           current spending instruction
                                                float64
           current_spending
                                                float64
                                                float64
           other_spending
           dtype: object
In [273]: print((X.shape))
           (3855, 6)
In [274]: y.describe
Out[274]: <bound method NDFrame.describe of 0
                                                                 0.0
                    639129.0
           1
           2
                    127258.0
           3
                      80678.0
                    189862.0
                       . . .
           3850
                      12650.0
           3851
                      77316.0
           3852
                      77316.0
           3853
                      77316.0
           3854
                      77316.0
           Name: enrollment, Length: 3855, dtype: float64>
In [275]: X.corr()
Out[275]:
                                    total_revenue federal_revenue expenditure current_spending_instruction
                        total_revenue
                                        1.000000
                                                      0.917869
                                                                 0.998196
                                                                                          0.988210
                                        0.917869
                                                      1.000000
                                                                 0.914874
                                                                                          0.88414
                       federal_revenue
                                        0.998196
                                                      0.914874
                                                                 1.000000
                                                                                          0.99015
                          expenditure
                                                      0.884147
                                                                 0.990151
                                                                                          1.00000
            current_spending_instruction
                                        0.988210
```

0.971238

0.911038

current_spending

other_spending

0.925755

0.898340

0.968666

0.909028

0.93129;

 0.86000^{4}

```
In [276]: # Check y's type.
          print(type(y))
          <class 'pandas.core.series.Series'>
In [277]: print((y.shape))
           (3855,)
In [278]: ## 4 steps
          ## initiate
          ## training
          ## predict
          ## evaluate
 In [93]: Xs = eduf[['total_revenue', 'federal_revenue', 'expenditure', 'current_spendin
          y = eduf['enrollment']
          lr = LinearRegression()
          lr.fit(Xs, y)
 Out[93]: LinearRegression(copy X=True, fit_intercept=True, n_jobs=None, normalize=
          False)
In [279]: from sklearn.linear model import LinearRegression
 In [92]: print(lr.intercept )
          print(lr.coef )
          4230.326308517164
          [-0.07238651 - 0.0502455 \quad 0.04932558 \quad 0.01592084 \quad 0.17267962 \quad 1.02548782]
In [125]: x_train, x_test,y_train,y_test = train_test_split(X,y,random_state = 123)
          y pred = lr.predict(X)
          X_pred = lr.predict(X)
In [109]: |lr.fit(x_train,y_train)
Out[109]: LinearRegression(copy X=True, fit intercept=True, n jobs=None, normalize=
          False)
In [133]: ## calcuate the accuracy
          lr.score(x_test,y_test)
Out[133]: 0.900831053664841
```

```
In [141]: from sklearn.model_selection import train_test_split
          # Define a function that accepts a list of features and returns testing RMS
          def train_test_rmse(eduf, feature_cols1):
              X = gpa1[feature_cols]
              y = gpal.gpa
              X train, X test, y train, y test = train test split(X, y, random state=
              linreg = LinearRegression()
              linreg.fit(X_train, y_train)
              y_pred = linreg.predict(X_test)
              return np.sqrt(metrics.mean squared error(true, pred))
  In [ ]: | from sklearn.model_selection import train test split
          # Define a function that accepts a list of features and returns testing RMS
          def train test mae(eduf, feature cols1):
              X = gpa1[feature_cols]
              y = gpal.gpa
              X train, X test, y train, y test = train test split(X, y, random state=
              linreg = LinearRegression()
              linreg.fit(X_train, y_train)
              y pred = linreg.predict(X test)
              return metrics.mean absolute error(y test, y pred)
In [140]: # Compare different sets of features.
          print(train test rmse(eduf, ['total revenue', 'federal revenue', 'expenditure
          print(train_test_rmse(eduf, ['total_revenue', 'federal_revenue','current_sp
          print(train test rmse(eduf, ['total revenue', 'current spending', 'expendit
          30726.187375168993
          30554.656132892174
          34903.17143826005
In [150]: print(train test mae(eduf, ['total revenue', 'federal revenue', 'expenditure'
          print(train_test_mae(eduf, ['total_revenue', 'federal_revenue', 'current_spe
          print(train test mae(eduf, ['total revenue', 'current spending', 'expenditu
          19979.203553974072
          20158.043316193853
          22607.78278364976
In [305]: ## RMSEA reduced wtih more features
```

```
In [114]: X train, X test, y train, y test = train_test_split(X, y, random_state=123)
          y null = np.zeros_like(y test, dtype=float)
          y_null.fill(y_test.mean())
          y_null
Out[114]: array([83227.40975104, 83227.40975104, 83227.40975104, 83227.40975104,
                 83227.40975104, 83227.40975104, 83227.40975104, 83227.40975104,
                 83227.40975104, 83227.40975104, 83227.40975104, 83227.40975104,
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In [115]: np.sqrt(metrics.mean squared error(y test, y null))
Out[115]: 97571.0155302958
          Ridge Regression
In [423]: revenue_dummies = pd.get_dummies(districts_f.total_revenue)
In [424]: districts_dummies = pd.concat([districts_f, revenue_dummies], axis=1)
In [425]: | X = districts dummies[feature cols]
          y = districts dummies.enrollment
          linreg = LinearRegression()
          linreg.fit(X, y)
          X train, X test, y train, y test = train test split(X, y, random state=1)
```

ridge regression

```
In [ ]: from sklearn.linear_model import Ridge
          ridgereg = Ridge(alpha=0, normalize=True)
          ridgereg.fit(X_train, y_train)
          y_pred = ridgereg.predict(X_test)
          print(np.sqrt(metrics.mean squared error(y test, y pred)))
In [430]: y pred = ridgereg.predict(X)
In [435]: print(ridgereg.intercept_)
          10886.08329776775
In [298]: |list(zip(feature_cols, ridgereg.coef_))
Out[298]: [('total_revenue', -0.07844183321424758),
           ('federal_revenue', -0.06983128027489204),
           ('expenditure', 0.074294423126399),
           ('current_spending_instruction', -0.0047588651012720655),
           ('current_spending', 0.14513856086261095),
           ('other_spending', 1.0430108861542022)]
In [433]: ridgereg = Ridge(alpha=0.1, normalize=True)
          ridgereg.fit(X_train, y_train)
          y pred = ridgereg.predict(X test)
          print(np.sqrt(metrics.mean squared error(y test, y pred)))
          41640.4232288643
In [126]: list(zip(feature cols, ridgereg.coef ))
Out[126]: [('total revenue', 0.002614288254853433),
           ('federal_revenue', 0.0172038925711048),
           ('state_revenue', 0.014514305171092002),
           ('expenditure', 0.004149895352522794),
           ('current spending instruction', -0.0017976188683634198),
           ('current_spending', 0.06633619271346432),
           ('other spending', 0.6739851697829419),
           ('total capital', 0.06761253149194939)]
```

Conclusion The total revenue, state_revenue, federal_revenue, enrollment, current_spending, and expenditure are the strong predictors for enrollments. The multicolinearity are also detected on the heatmap. Tuning the KNN model help improve the model evaluation and reduce the testing error. By scale the training and testing data, the testing error reduced although the overall model fits not actually improved.