(1a)

That X is a vector space is easily seen by its definition $\alpha \left(x_j\right)_{j=1}^{\infty} + \beta \left(y_j\right)_{j=1}^{\infty} = \left(\alpha x_j + \beta y_j\right)_{j=1}^{\infty}$

Reference