

Algorithm: CGSL-ECM One-Time TTE Simulation (Gillespie + ODE)

Input: $\theta \sim$ (from Model II's control parameters), Q_{base} , $y(\cdot)$,
 $(\mu_I(s), \sigma_I(s))$, t_start , $x \theta$, $s\theta$, V_cutoff , I_min

Output: TTE

Initialization: $t \leftarrow \theta$, $X \leftarrow s\theta$, $x \leftarrow x\theta$

for $k = 1$ to 10000 **do**

- 1) Initialization: $t \leftarrow 0$, $X \leftarrow s0$, $x \leftarrow x0$
- 2) Main loop: while $V_{term}(t) > V_{cutoff}$ do
 - a) Calculate $t_day = (t_start + t) \bmod 24$, and update gate $\gamma = \text{clip}(v(t_day), 0, 1)$
 - b) Construct the adaptive generation matrix (only gating $\{S1, S2\} \rightarrow \{S3, S4\}$, and calculate the diagonal terms)
 - c) Gillespie: sample time interval $\Delta t \sim \text{Exp}(\mu_I(X))$, and sample the next state X_{new}
 - d) Sample the interval current $I \sim \max(1, \mu_I(X), N(\mu_I(X), \sigma_I^2(X)))$
 - e) Use constant 1 to advance Model I and its ODE by Δt ; if an event is triggered within the interval, return TTE
 - f) Update: $t \leftarrow t + \Delta t$, $X \leftarrow X_{new}$
- 3) End: return TTE = t

end