

# Homework 10

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## 1

### (a)

Shape is (1000, 3, 256, 256). Each dim means: images number, color(R, G, B), image width, image height.

### (b)

Shape is (40, 80, 2400). Each dim means: recording number, channels, samples.

### (c)

Shape is (32, 300, 3, 512, 512). Each dim means: video number, frame number, color(R, G, B), image width, image height.

## 2

### (a)

$i + k_i$  and  $i + k_2$  should within the boundary of the  $X$ .

### (b)

The size of  $Z$  will be  $[5 \times 4]$ .

### (c)

The largest positive values will be 6, the position is (1,3), (2,3), (3,3).

### (d)

The largest negative values will be -2, the position is (3, 4).

### (e)

0 will appears on position (1, 1), (1, 2)

## 3

### (a)

Shapes of  $Z$  and  $U$  is  $[i - k_1 + 1 \times j - k_2 + 1 \times n] = [46 \times 62 \times 10]$

**(b)**

Number of input channel is  $48 \times 64 \times 10 = 30720$

Number of input channel is  $46 \times 62 \times 10 = 28520$

**(c)**

Multiplications will be performed  $46 \times 62 \times 10 = 28520$  times.

**(d)**

Trainable parameters will be  $3 \times 3 \times 10 \times 20 + 10 = 1810$

**4**

**(a)**

$$\frac{\partial J}{\partial Z[i, j_1, j_2, m]} = \frac{\partial J}{\partial U} \cdot \frac{\partial U}{\partial Z[i, j_1, j_2, m]} = \frac{\partial J}{\partial U} \cdot \frac{e^{-Z[i, j_1, j_2, m]}}{(1 + e^{-Z[i, j_1, j_2, m]})^2}$$

**(b)**

$$\begin{aligned} \frac{\partial J}{\partial W[k_1, k_2, n, m]} &= \frac{\partial J}{\partial Z[i, j_1, j_2, m]} \cdot \frac{Z[i, j_1, j_2, m]}{W[k_1, k_2, n, m]} \\ &= \frac{\partial J}{\partial Z[i, j_1, j_2, m]} \cdot X[i, j + k_1, j_2 + k_2, n] \end{aligned}$$

**(c)**

$$\begin{aligned} \frac{\partial J}{\partial X[i, j_i, j_2, n]} &= \frac{\partial J}{\partial Z[i, j_1, j_2, m]} \cdot \frac{Z[i, j_1, j_2, m]}{X[i, j_i, j_2, n]} \\ &= \frac{\partial J}{\partial Z[i, j_1, j_2, m]} \cdot W[k_1, k_2, n, m] \end{aligned}$$

**5**

**(a)**

$$\mathbf{y} = [2, 2, 10, 0]$$

**(b)**

$$\mathbf{y} = [2, 3, 10, 1]$$

**(c)**

If using sub-sampling with stride = s, shape will be (B, N, Ceil(C/s)).

if using max pooling with size= $p$  and stride= $s$ , shape will be  $(B, N, \text{Ceil}(C/s))$