

## Generative Model

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Following definitions in previous notes *Normative Model I*, refine a generative process to create causal relations (hypotheses) as follows.

1. Create one causal relation. Start by sampling number of cause sentences (from a gamma distribution, say  $\Gamma(1.5, 1)$ ?); number of effect sentences is 2 by definition (one sentence for  $R'$  lightness, and one sentence for  $R'$  sidedness).

Each sentence is created by

- (a) Sample relations, controlled by a relation parameter  $\alpha$ :

$$P(\text{pick } =) = P(\text{pick } \neq) = \alpha/2, P(\text{pick } >) = P(\text{pick } <) = (1 - \alpha)/2.$$

- (b) Sample a subject (left-hand side of the picked relation):

For cause sentences, sample  $A$  or  $R$  are equally likely,  $P(\text{pick } A) = P(\text{pick } R) = 1/2$ ; effect sentences always take  $R'$  as subjects.

- (c) Sample an object (right-hand side of the picked relation):

Objects can be absolute - an exact lightness or sidedness value, or relative -  $A$ 's lightness (sidedness) or  $R$ 's. Relative values, in addition, can combine with the increase or decrease by level 1 option (eg.  $L(R') = L(A) + 1$ ).

Assume that each type of values are picked equally like:

$P(\text{pick } l_i) = \frac{1}{3|L|}$  where  $l_i$  is an exact lightness value, and  $|L|$  is the total number of lightness values (in current experiment setup);

$P(\text{pick } s_i) = \frac{1}{3|S|}$  where  $s_i$  is an exact sidedness value and  $|S|$  is the total number of sidedness values (in current experiment setup);

$P(\text{pick } A) = P(\text{pick } R) = \frac{1}{6}$  for effect sentences,  $P(\text{pick } A) = P(\text{pick } R) = \frac{1}{3}$  for cause sentences (because for a cause sentence the object has to be different from the subject);

$P(\text{pick } A, +1) = P(\text{pick } A, -1) = P(\text{pick } R, +1) = P(\text{pick } R, -1) = \frac{1}{3 \times 4} = \frac{1}{12}$  for effect sentences; and  $\frac{1}{6}$  for cause sentences by similar reasons.

2. With probability  $\beta$  sample an extra causal relation that will join the others as an *if-else*.  $\beta$  decreases as the number of existing causal relations increases.

The above procedure generates *one* hypothesis, that can potentially contain multiple causal relations by an *if-else* relation.