R. Notebook

library(tidyverse) ## -- Attaching packages ----- tidyverse 1.2.1 --## v ggplot2 3.2.1 v purrr 0.3.3 ## v tibble 2.1.3 v dplyr ## v tidyr 1.0.2 v string 0.8.4 v stringr 1.4.0 ## v readr 1.3.1 v forcats 0.3.0 ## -- Conflicts ----- tidyverse_conflicts() --## x dplyr::filter() masks stats::filter() ## x dplyr::lag() masks stats::lag() library(FNN) ## knn.reg

The Key Functions

You need a function to compute the MSE, Variance, Bias, and Noise for the kNN Regression function. Note it depends on the function buildData

```
biasVarTO3.knn <- function(kVal,func,sizeDS,numDS,x0){</pre>
  allVals <- matrix(ncol=2,nrow=numDS)</pre>
  for(m in 1:numDS){
    ##the
    train.df <- buildData(func,sizeDS,sig)</pre>
    train.X <- as.matrix(train.df[c("x")])</pre>
    test.X <- as.matrix(x0)</pre>
    train.Y <- as.matrix(train.df[c("y")])</pre>
    mod.knn <- knn.reg(train.X,test.X,train.Y,k=kVal)</pre>
    allVals[m,1] <- mod.knn$pred
  allVals[,2] <- func(x0)+rnorm(numDS,0,sig)</pre>
  allVals.df <- data.frame(pred=allVals[,1],true=allVals[,2])</pre>
  mse <- with(allVals.df,mean((pred-true)^2))</pre>
  var0 <- with(allVals.df,var(pred))</pre>
  bias2 <- with(allVals.df,mean(pred-true))^2</pre>
  noise <- sig^2</pre>
  c(mse,var0,bias2,noise)
```

The buildData Function

```
buildData <- function(func,sizeDS,sig,xMin = -1, xMax = 1){
    ##predictor
    x<-runif(sizeDS,xMin, xMax) # inputs
    ## Repsonse</pre>
```

```
y<-func(x)+rnorm(sizeDS,0,sig) #realized values f(x)+noise
## Put in a data frame
data.frame(x,y)
}</pre>
```

Example

```
f3 <- function(x) x*(x-1)*(x+1)
sizeDS <- 100
sig <-0.5
numReps <- 25

kVal <- 20
x0 <- 0.5
vals <- biasVarT03.knn(kVal,f3,sizeDS,numReps,x0)

vals <- round(vals,3)
sprintf("MSE=%s, Var=%s, Bias^2=%s, Noise=%s",vals[1],vals[2],vals[3],vals[4])

## [1] "MSE=0.163, Var=0.015, Bias^2=0.022, Noise=0.25"</pre>
```