LEMMA 2.61

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I'll reproduce the Lemma and its proof here.

Lemma (2.61). For a locally-finite median graph (X, G) with finite hyperplanes, each end has a neighborhood basis of half-spaces.

Proof. Let $U \in \widehat{X} \setminus X$ be an end, $\hat{A} \ni U$ be a clopen neighborhood where $A \in \mathcal{H}_{\partial < \infty}(X)$. By Corollary 2.34, $\text{cvx}(\partial_{\text{ov}} A) \subseteq X$ is finite. By Lemma ∎