

Determine the coupling strength in level attraction

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Determine the coupling strength without ω_s mapping

Line shape of spectrum:

$$S_{21} = 1 + \frac{\kappa_{\text{ext}}}{i(\omega - \omega_c) - (\gamma_c + \kappa_{\text{ext}})} + \frac{g^2}{i(\omega - \omega_s) - \gamma_s}$$

✓
✓
✓
✓
?

Parameters we set fixed

$$\gamma_{\text{cavity}} = 10.9 \text{ MHz} \pm 0.5 \text{ MHz}$$

$$\kappa_{\text{ext}} = 754 \text{ MHz} \pm 8 \text{ MHz}$$

$$\omega_{\text{cavity}} \approx 2.33 \text{ GHz (influenced by dielectric material)}$$

$$\gamma_{\text{ssr}} = 3.0 \text{ MHz} \pm 0.2 \text{ MHz} \quad ?$$

$$\omega_{\text{ssr}} \approx 2.41 \text{ GHz (influenced by dielectric material)}$$

Extrinsic damping of SRR

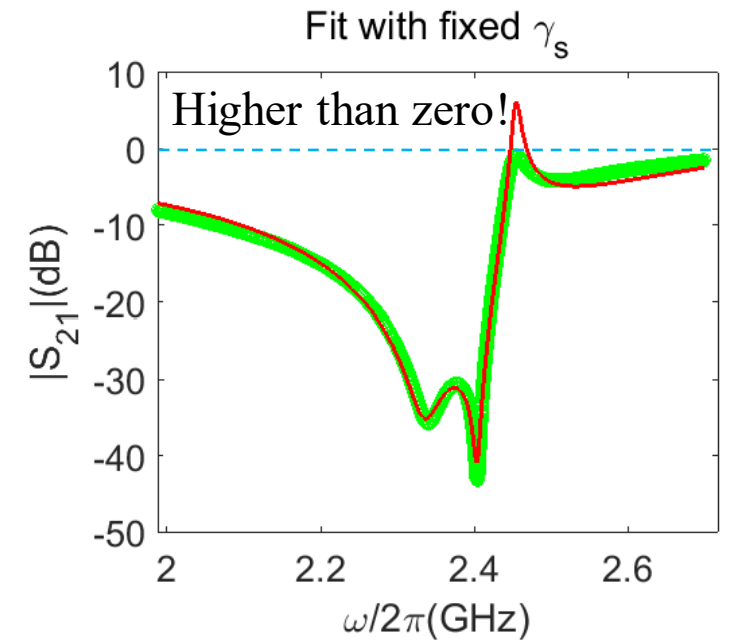
$$\kappa_{\text{ssr}} = 15.9 \text{ MHz} \pm 0.1 \text{ MHz}$$

Parameters we need to fit:

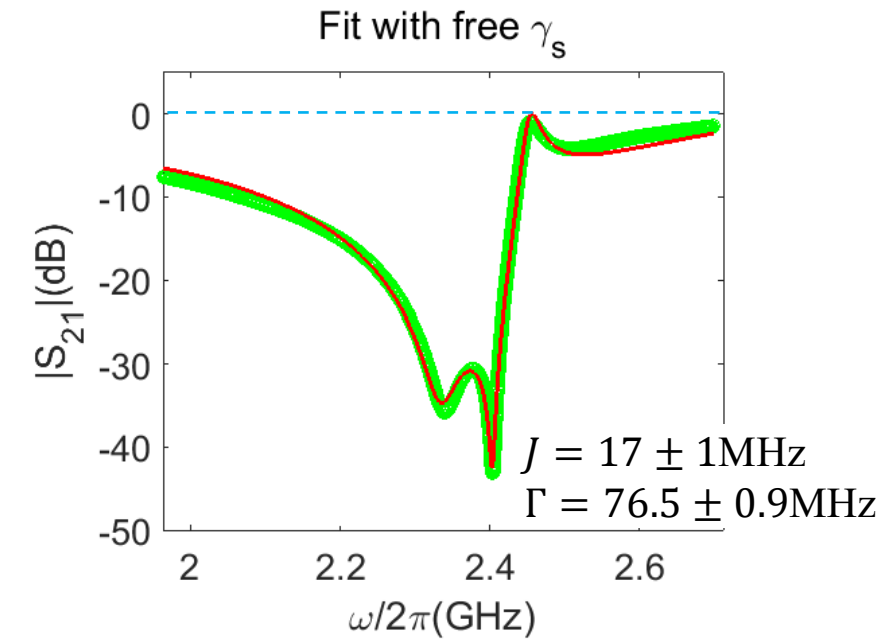
$$g = J + i\Gamma$$

Γ start point : $\sim 70 \text{ MHz}$ (estimated)

J start point : $\sim 10 \text{ MHz}$ (estimated)



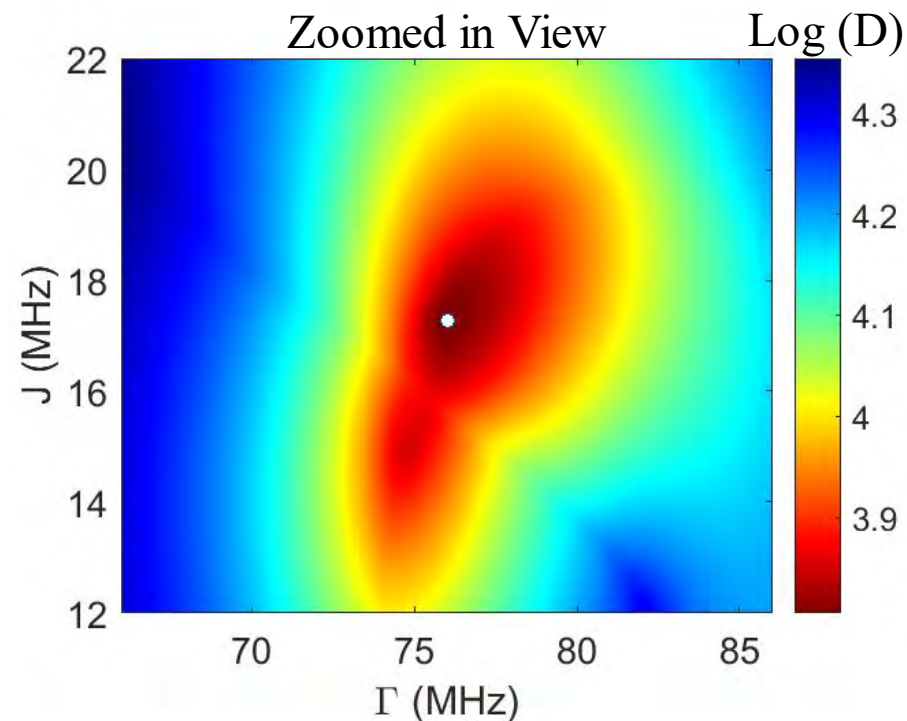
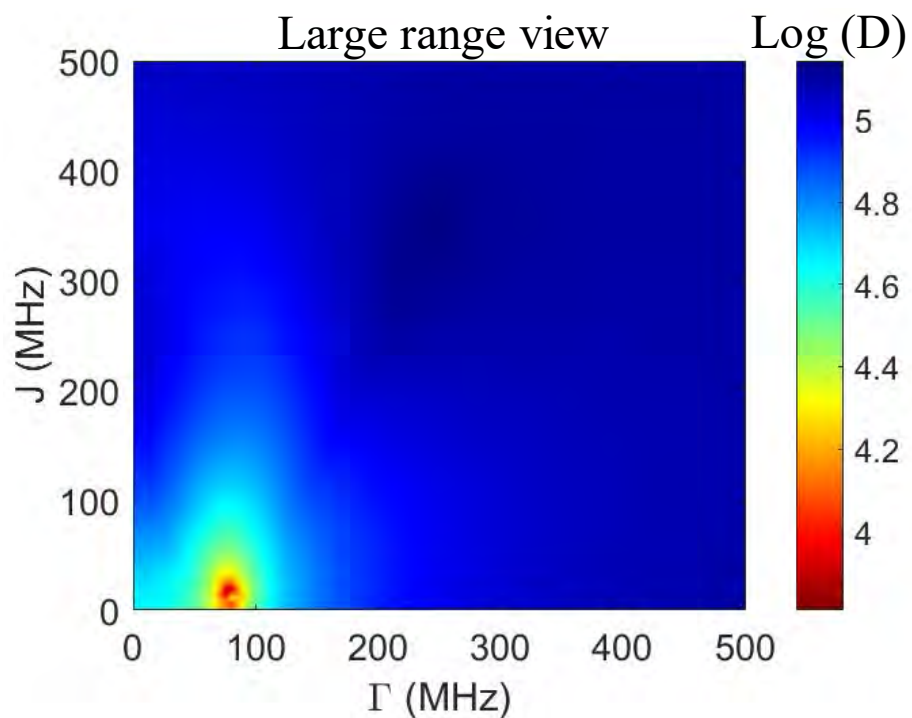
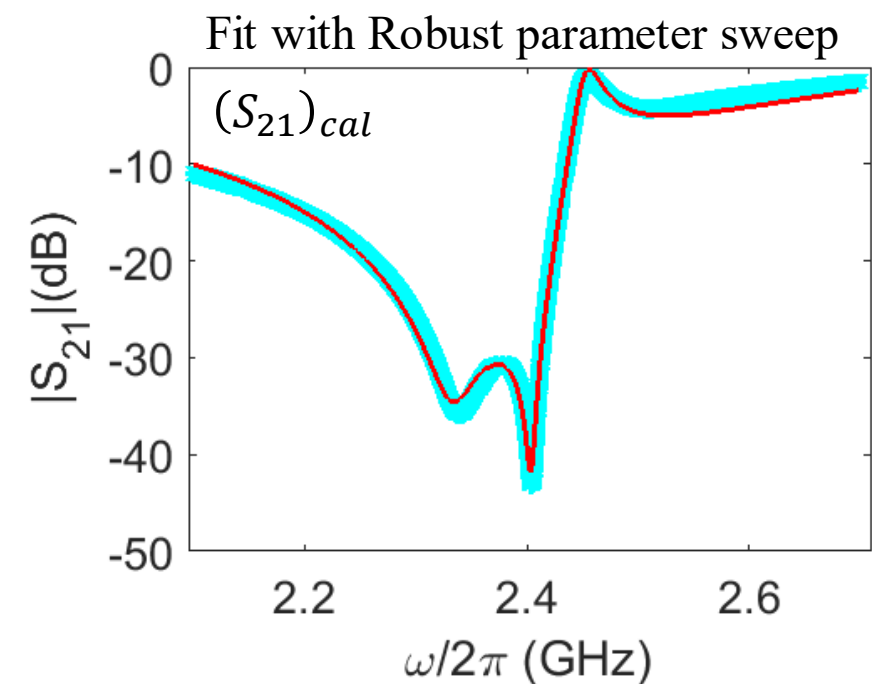
$$\gamma_{\text{ssr}} = 19.0 \text{ MHz} \pm 0.1 \text{ MHz}$$



Solution space

Is this the only solution for J and Γ ?

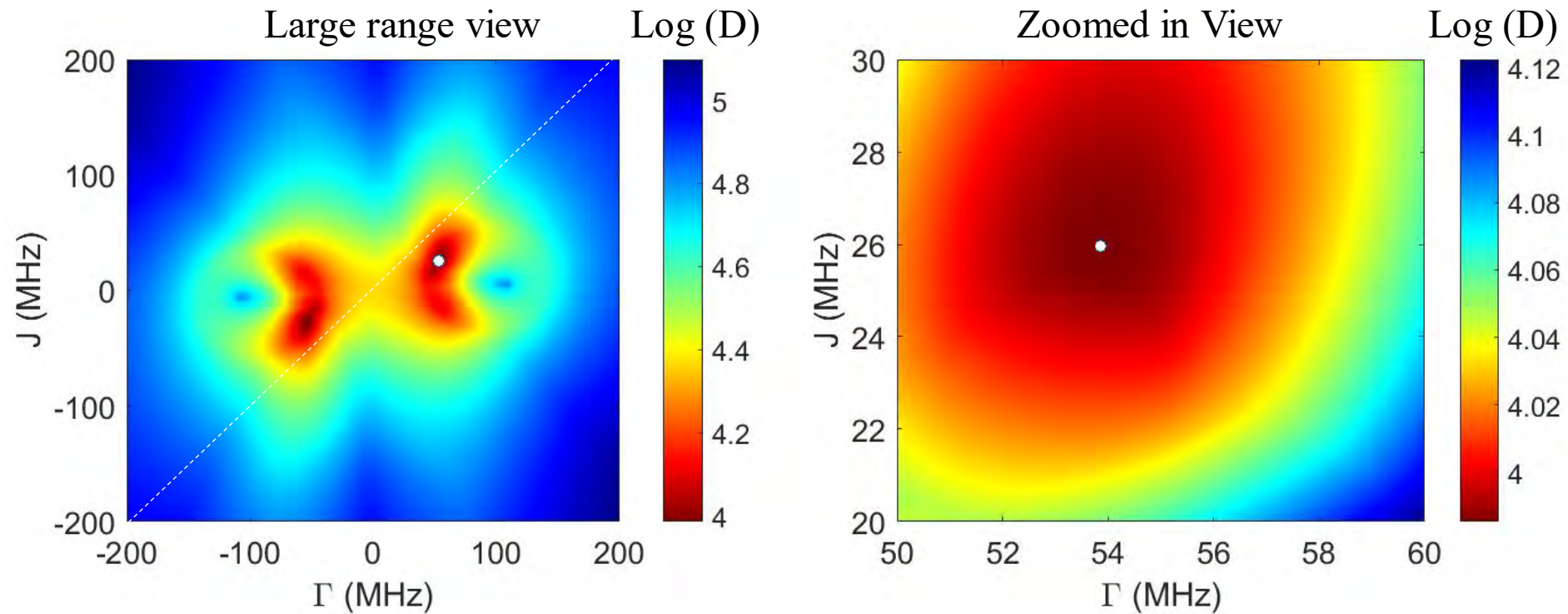
$$D(J, \Gamma) = \sum [|(S_{21})_{cal}(J, \Gamma) - (S_{21})_{mea}|]$$



$$J = 17.23 \text{ MHz}$$
$$\Gamma = 76.06 \text{ MHz}$$

From curve fitting:
 $J = 17 \pm 1 \text{ MHz}$
 $\Gamma = 76.5 \pm 0.9 \text{ MHz}$

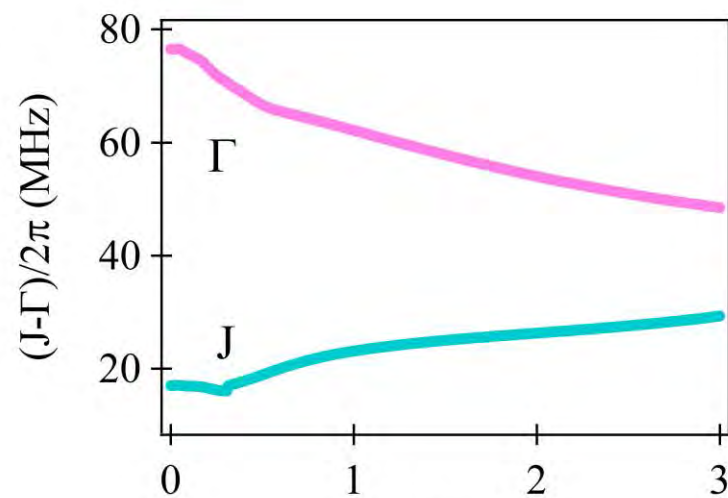
Further check: if J and Γ not always greater than zero



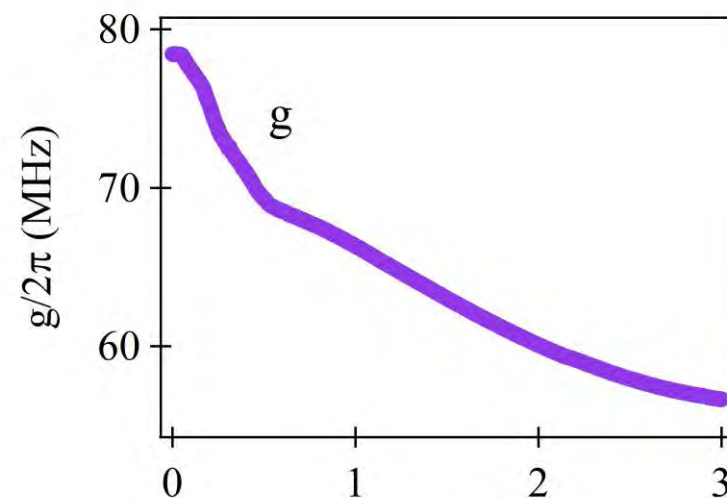
→ There is only one set of the solution of J and Γ !

Fitting Results

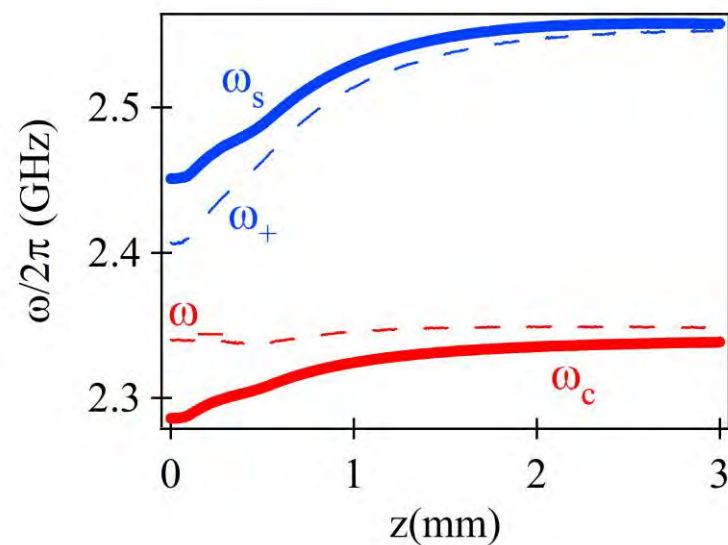
Coupling strength



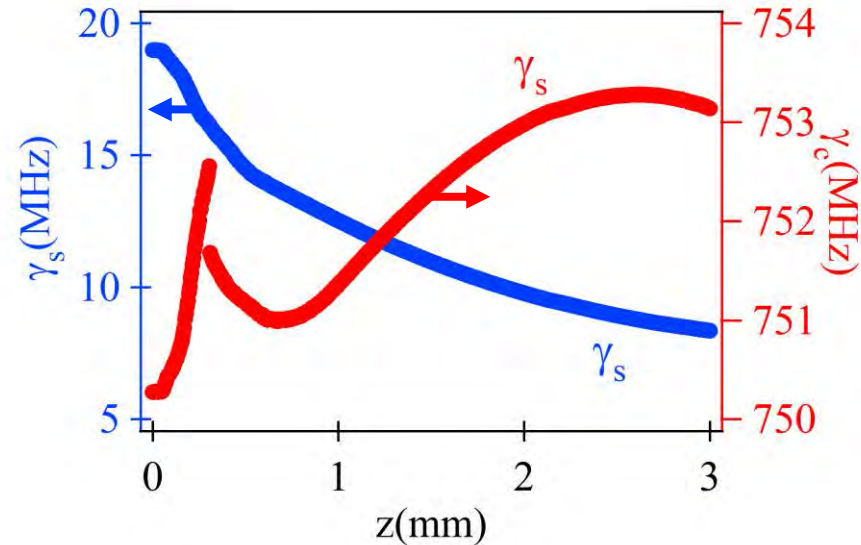
Total Coupling strength



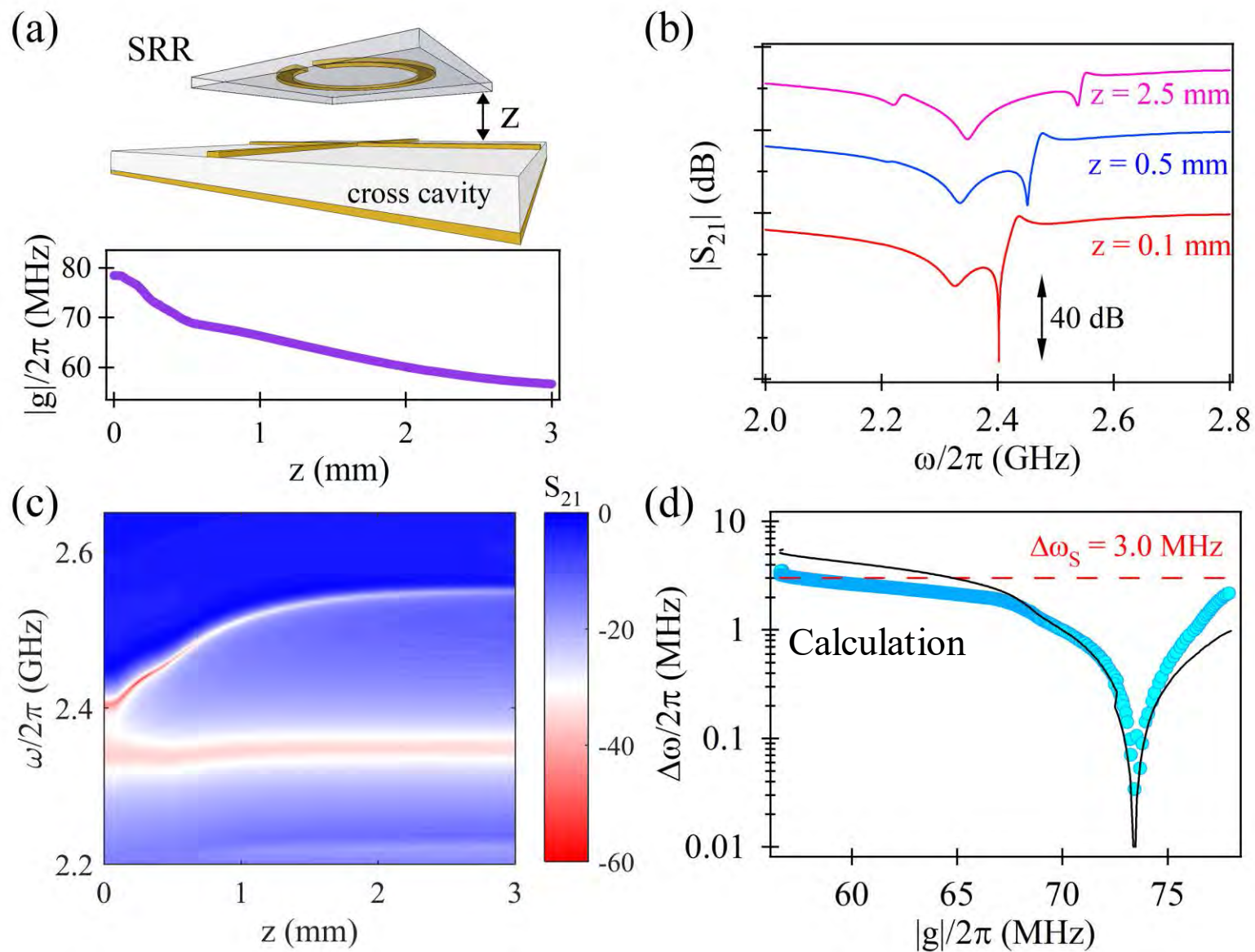
Dispersion



Damping evolution



Modified Fig. 2



Alternatively

