

Dielectric Constant Experiments Summary

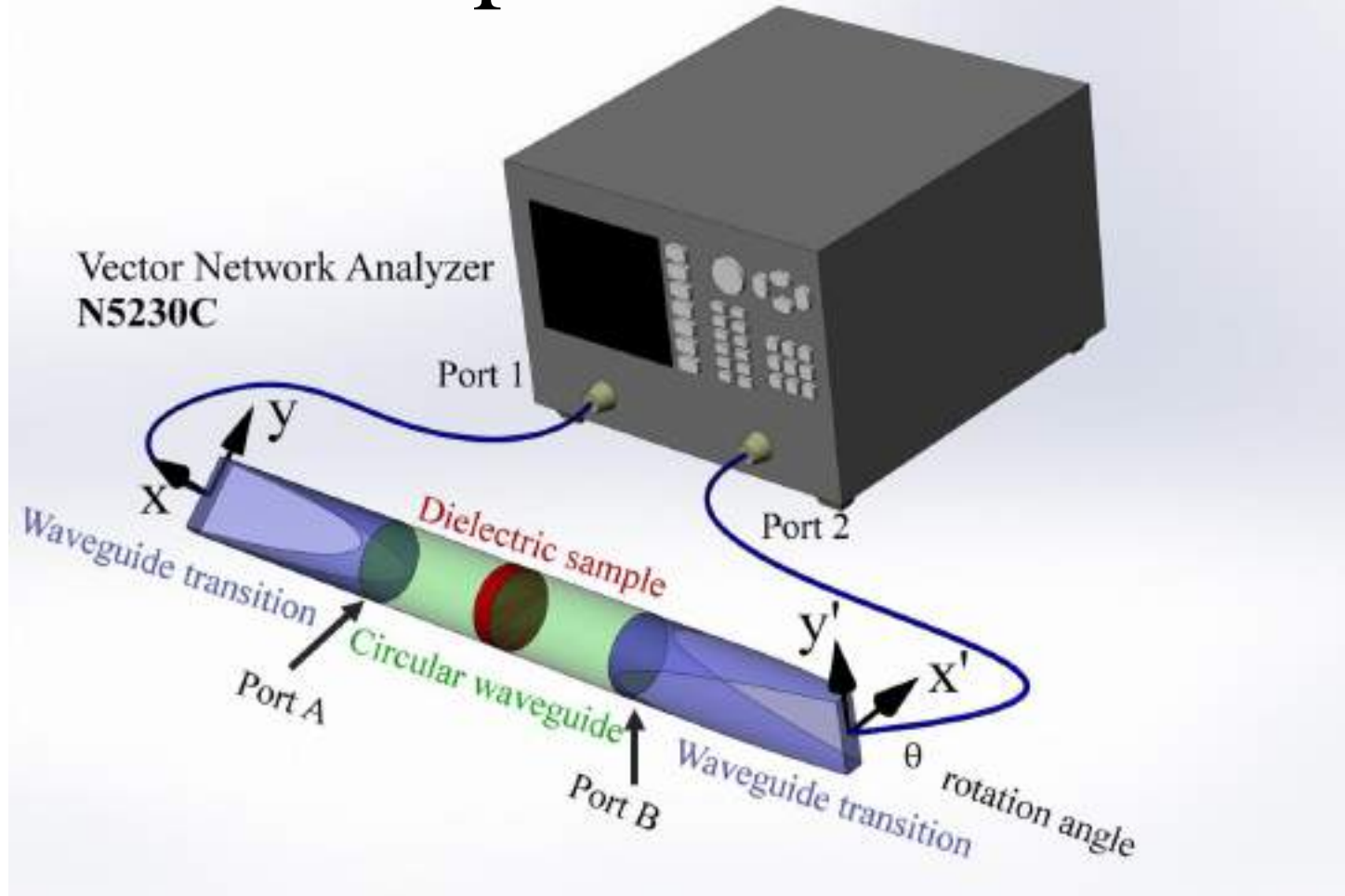
Yutong Zhao

Jan 25th, 2018

Task list

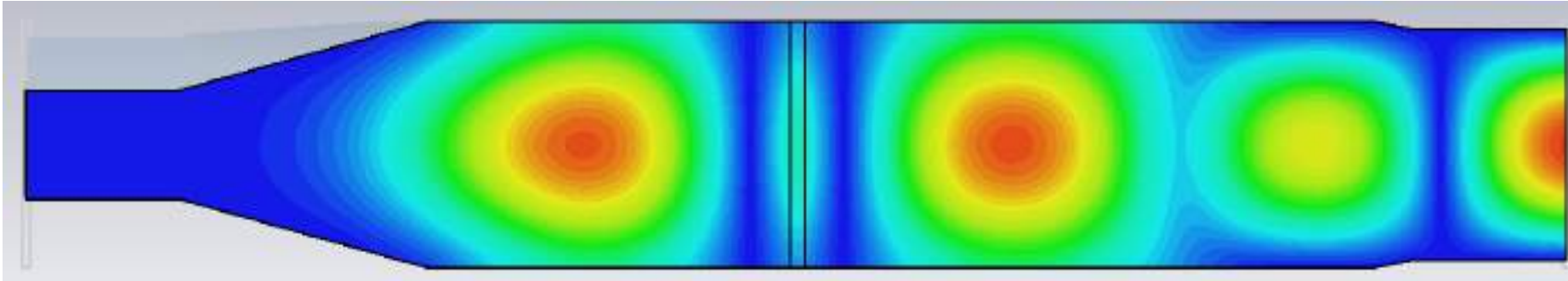
- 6.5.1 NaCl, NH_4NO_3 , KNO_3 , NaNO_3 , KClO_3 varying humidity from 0-10%
- 6.5.2 Mixing two powders of varying humidity from 0-10%
- 6.5.3 Aluminum powder
- 6.5.4 Water
- 6.5.5 Icing sugar (powder) humidity from 0-10%
- 6.5.6 Fuel oil (car gasoline and diesel)

Experiment setup

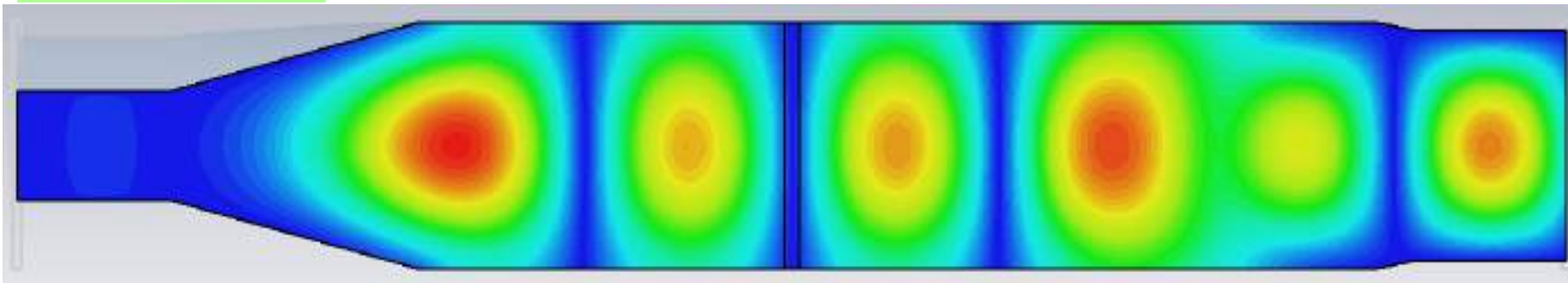


Simulations (E field, $\theta = 45^\circ$)

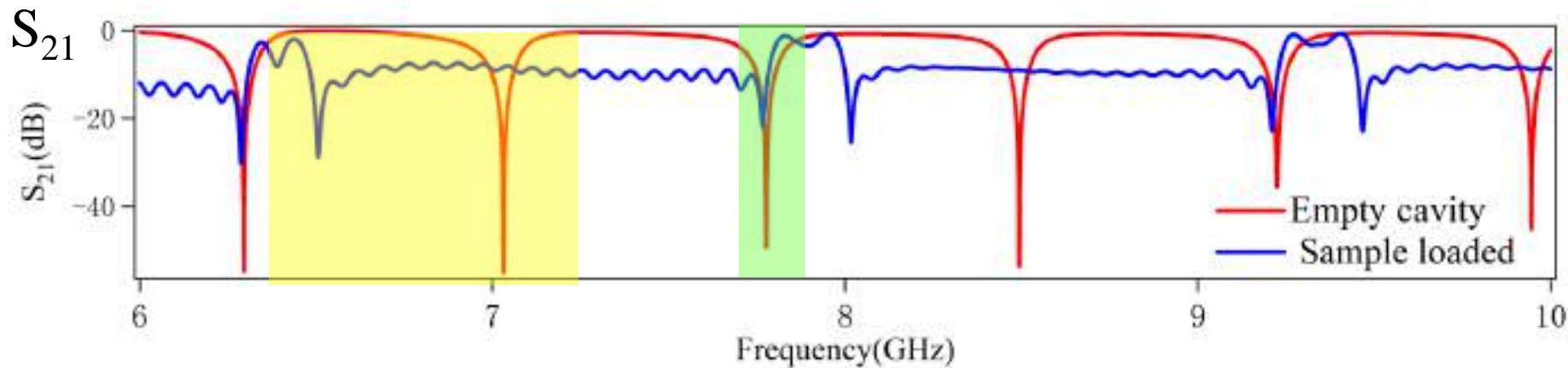
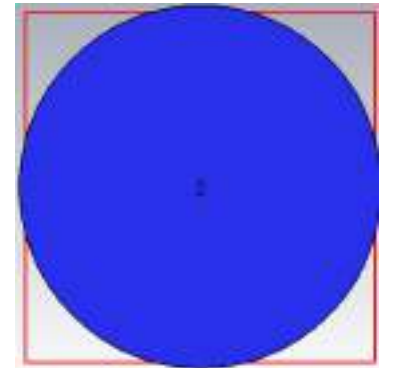
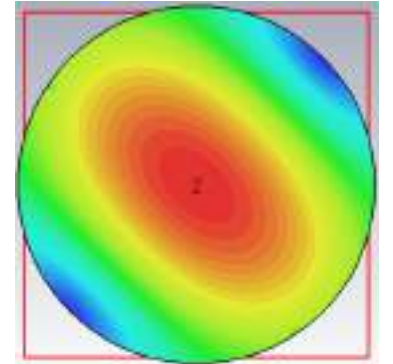
E-mode



H-mode



Z = 0 plane



Resonant method

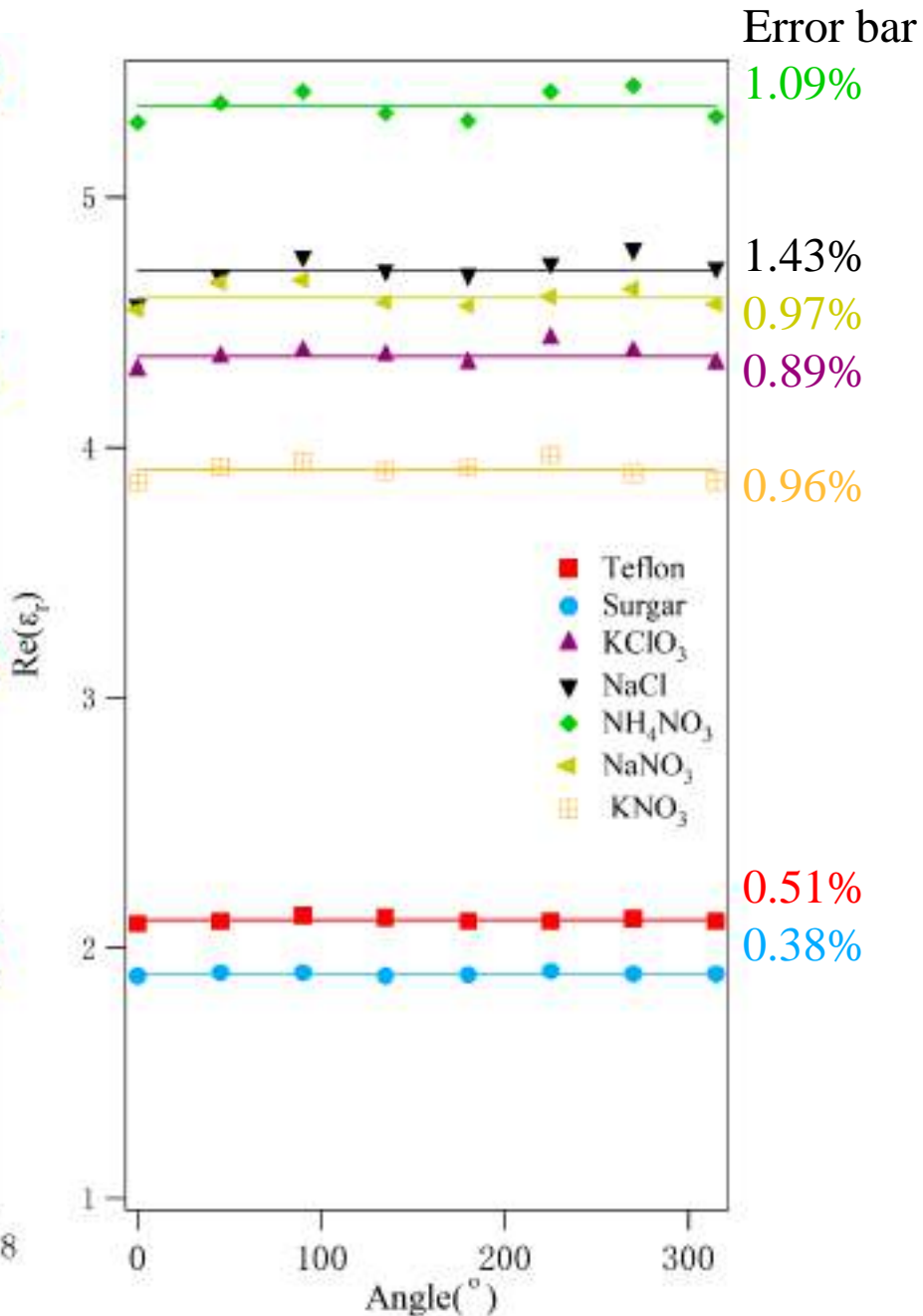
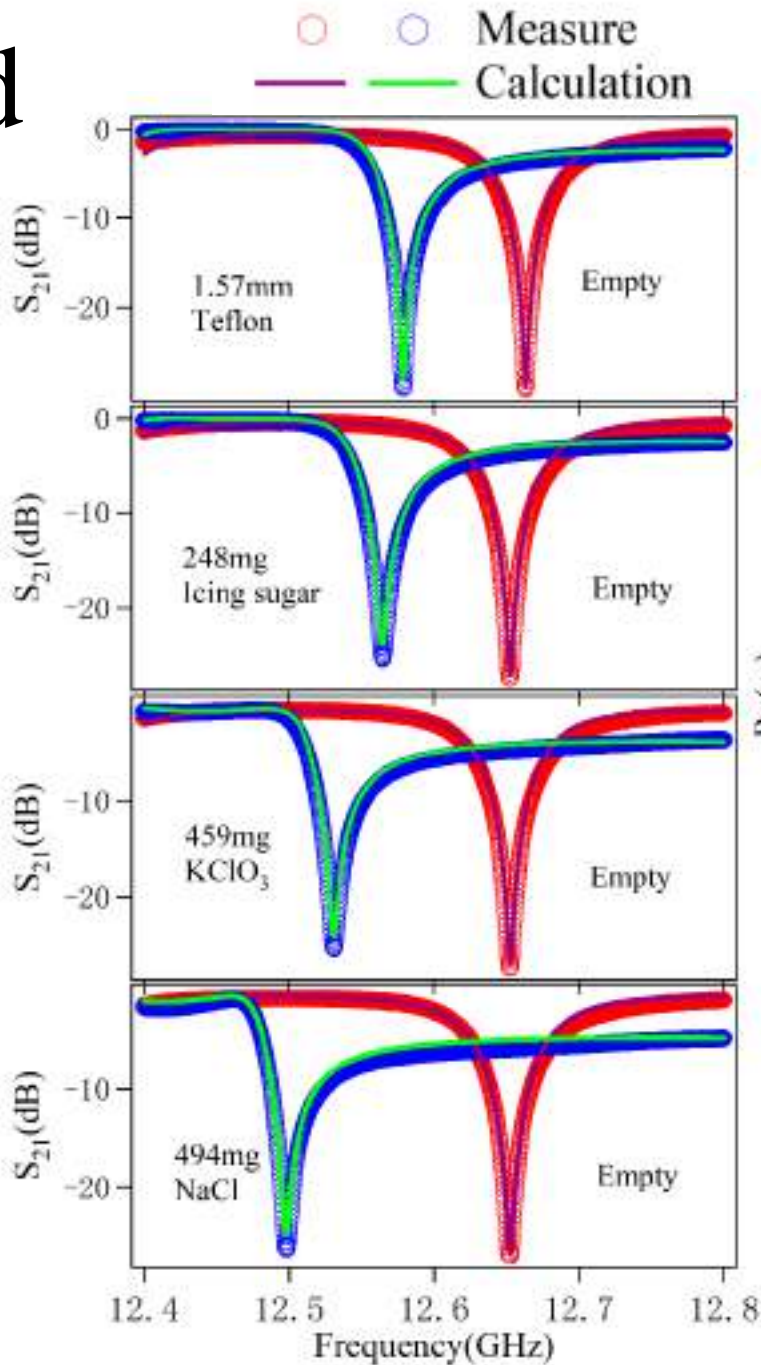
| Sample | ϵ_r |
|---------------------------------|--------------|
| NaCl | 4.71 |
| NH ₄ NO ₃ | 5.37 |
| KNO ₃ | 3.91 |
| KClO ₃ | 4.36 |
| Sugar | 1.90 |
| NaNO ₃ | 4.60 |
| Teflon | 2.11 |

1.57mm
Teflon

248mg
icing sugar

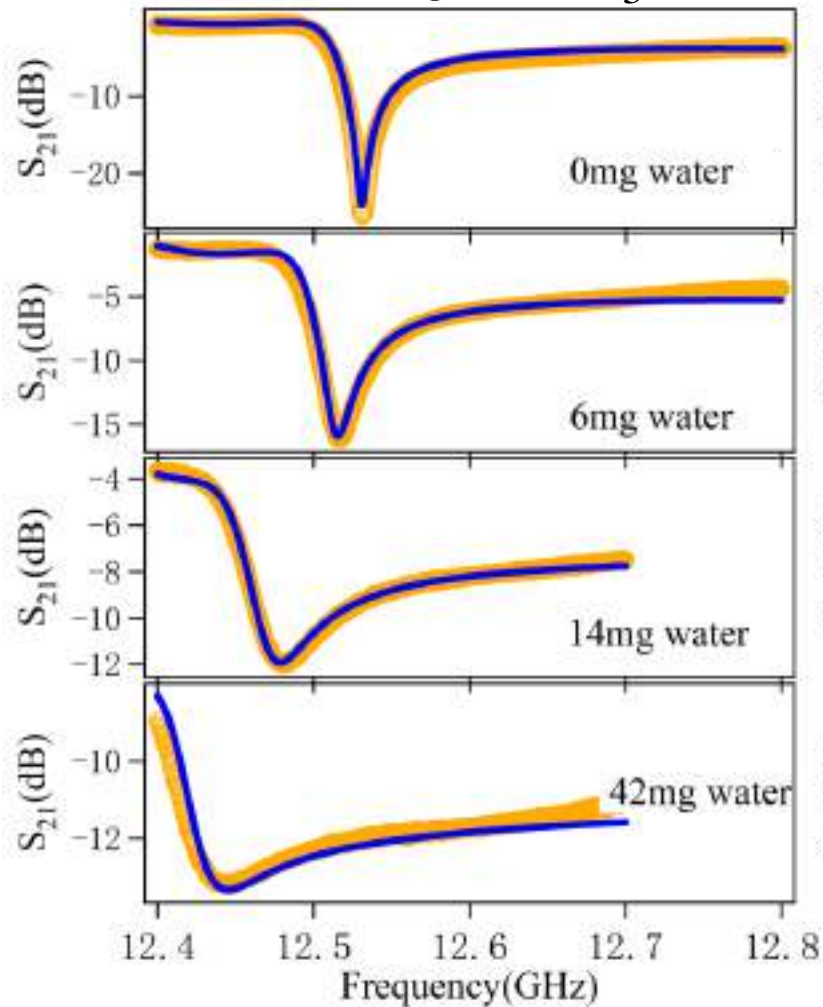
459mg
KClO₃

494mg
NaCl

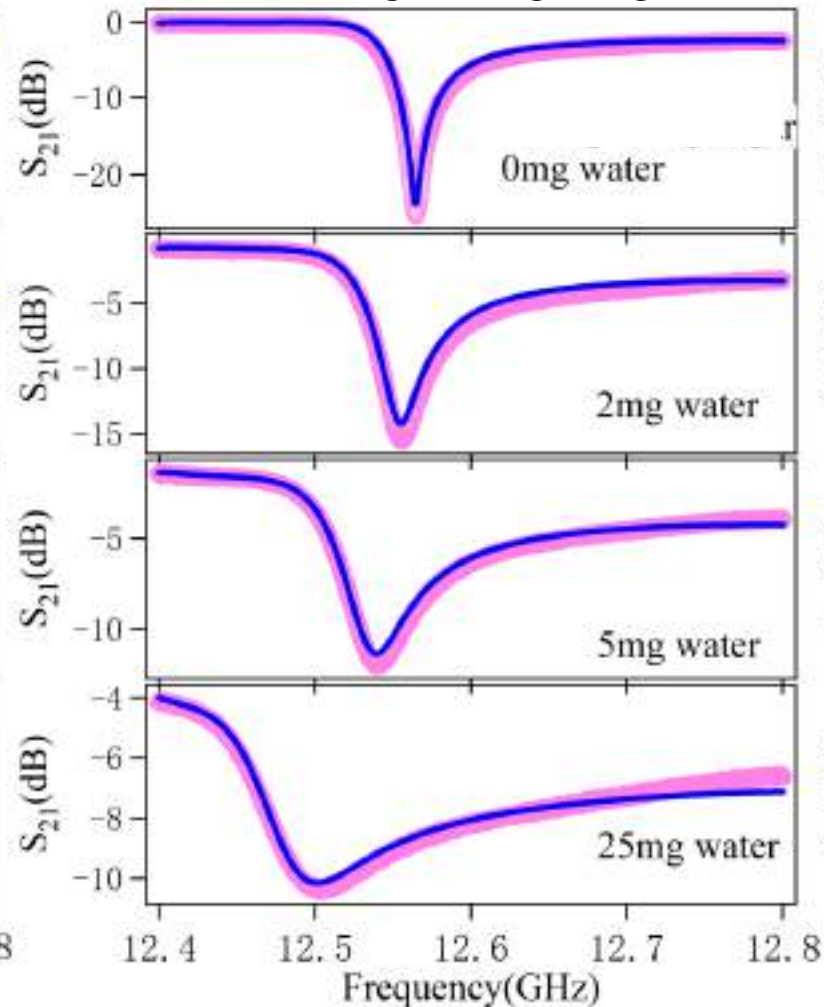


Spectra vs. humidity

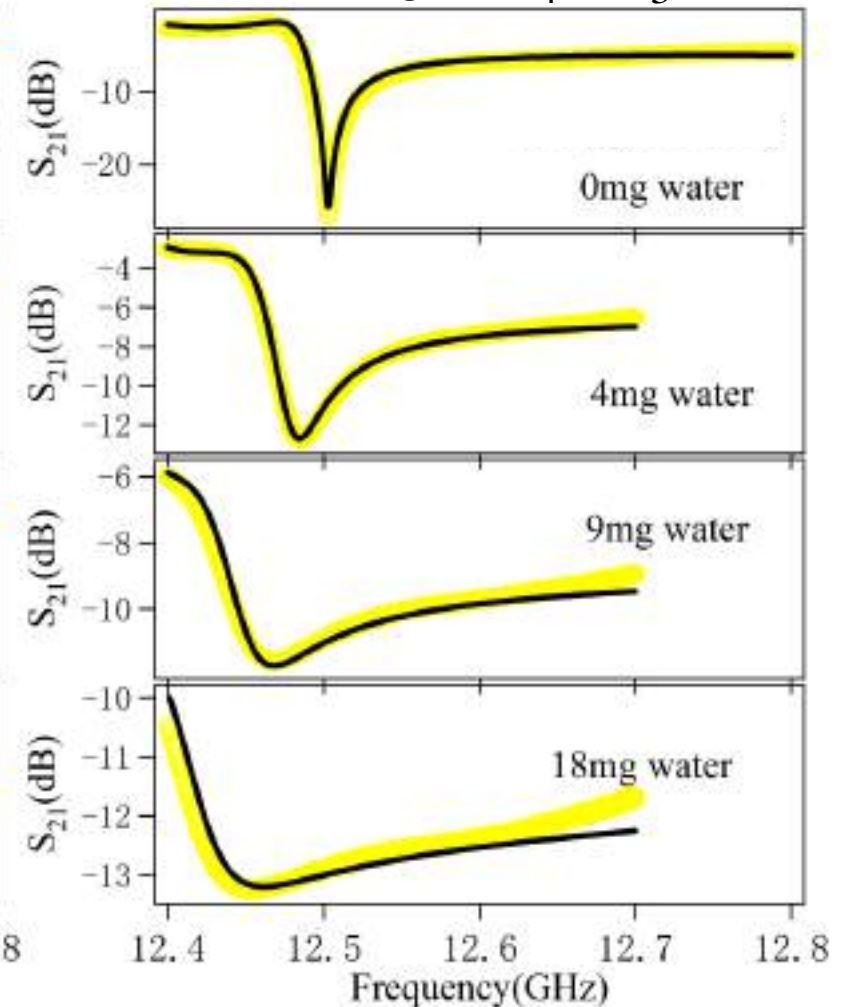
459mg KClO_3



248mg icing sugar



309mg NH_4NO_3



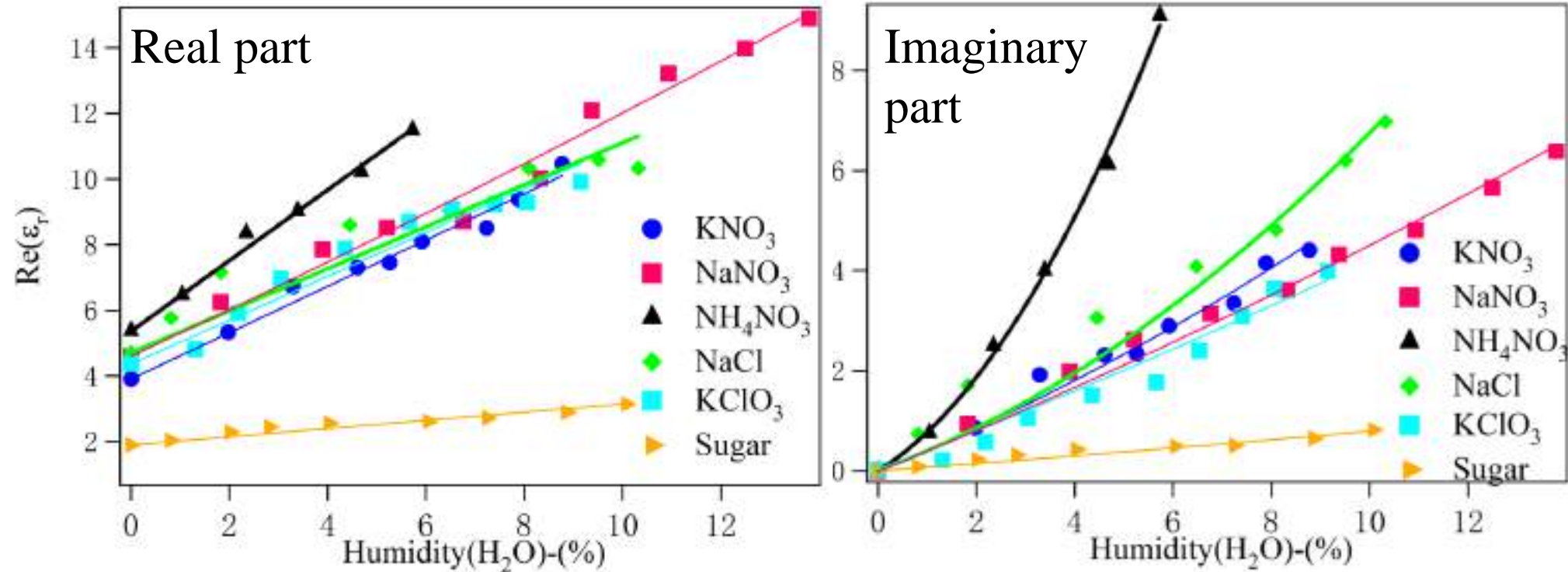
Empirical model for water content

$$\epsilon = \epsilon_s + a\epsilon_w w_c + b\epsilon_w w_c^2 + i \cdot \alpha w_c^2$$

- ϵ_s -- dielectric constant at dry material
- ϵ_w -- dielectric constant of water ($57.95 + 32.72i$) [Barthel et al];
- a, b -- empirical parameter
- α -- conductivity loss parameter
- w_c -- water content in mass(%)

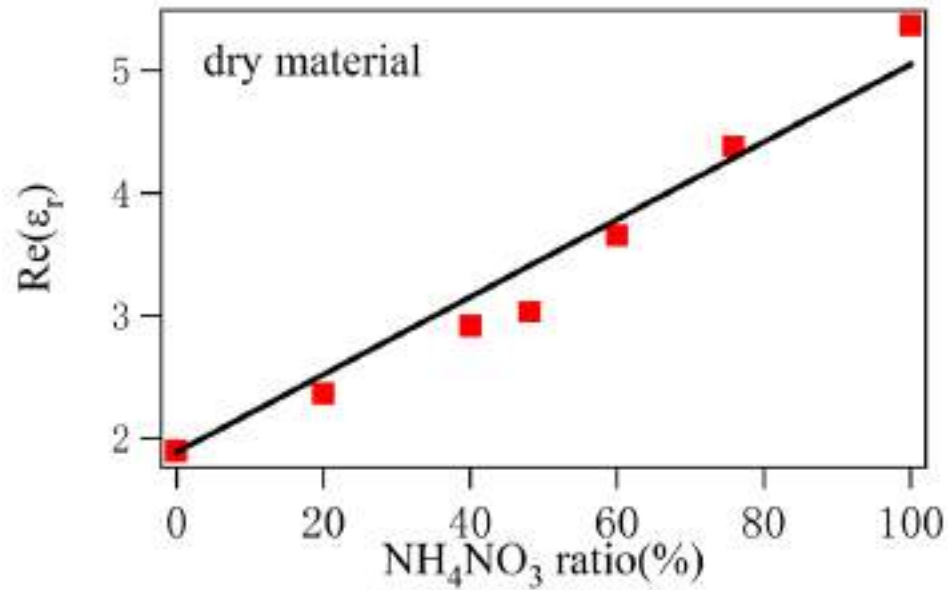
Pure chemicals at humidity from 0-10%

Solid lines: calculation results

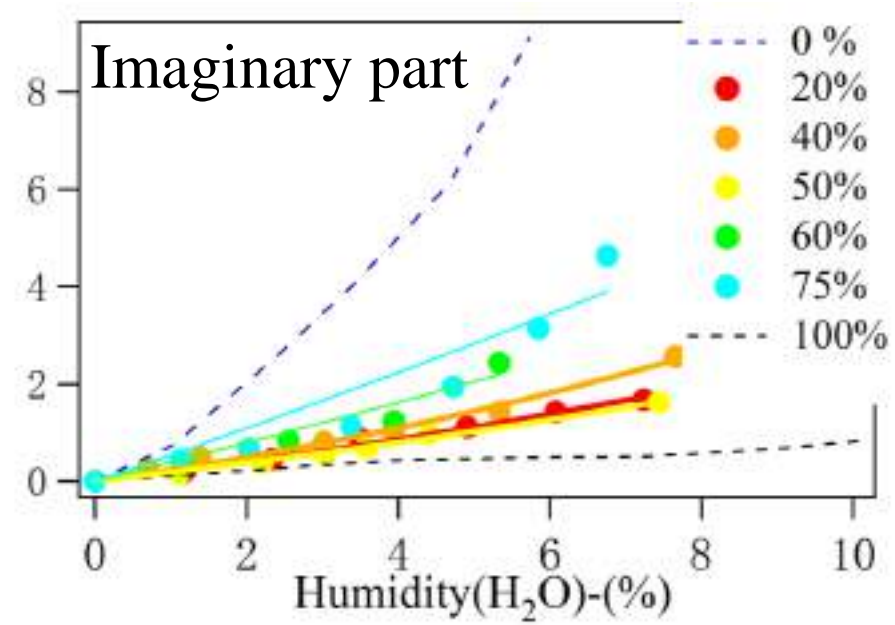
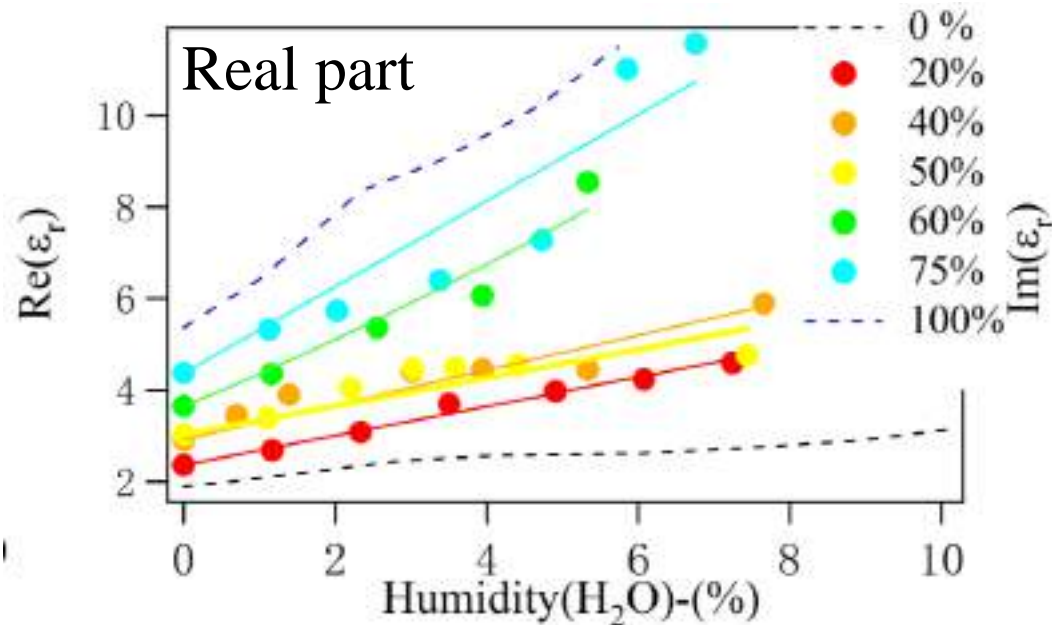


| | $\epsilon_w = 57.95 + 37.22i$ [Barthel et al] | | | | | | |
|---------------------------------|---|------|--------|-------------------|-------|---|-------|
| Sample | a | b | Alpha | Sample | a | b | Alpha |
| KNO ₃ | 1.216 | 0.01 | 133.0 | NaCl | 1.104 | 0 | 315.5 |
| NaNO ₃ | 1.208 | 0.7 | 28.5 | KClO ₃ | 1.152 | 0 | 40.7 |
| NH ₄ NO ₃ | 1.856 | 0 | 1650.5 | sugar | 0.216 | 0 | 8.4 |

Mixture: NH_4NO_3 in sugar



| Percent(%) | a | b | Alpha |
|------------|-------|-----|--------|
| 0 | 0.216 | 0 | 8.4 |
| 20 | 0.522 | 0 | 80.5 |
| 40 | 0.656 | 0 | 109.5 |
| 50 | 0.536 | 0 | 57.5 |
| 60 | 1.176 | 0.4 | 84.5 |
| 75.87 | 1.624 | 0.4 | 144 |
| 100 | 1.856 | 0 | 1650.5 |



Task list

6.5.1 NaCl, NH_4NO_3 , KNO_3 , NaNO_3 , KClO_3 varying humidity from 0-10%



6.5.2 Mixing two powders of varying humidity from 0-10%



6.5.3 Aluminum powder

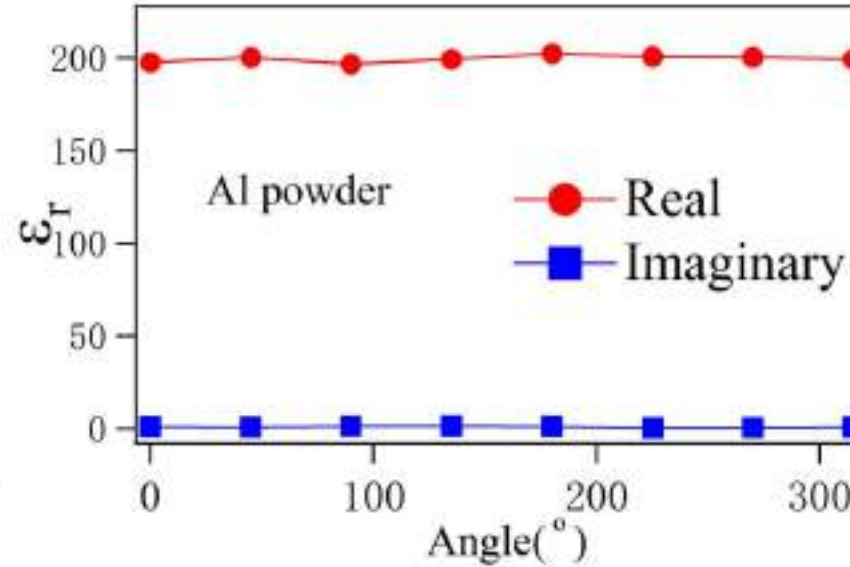
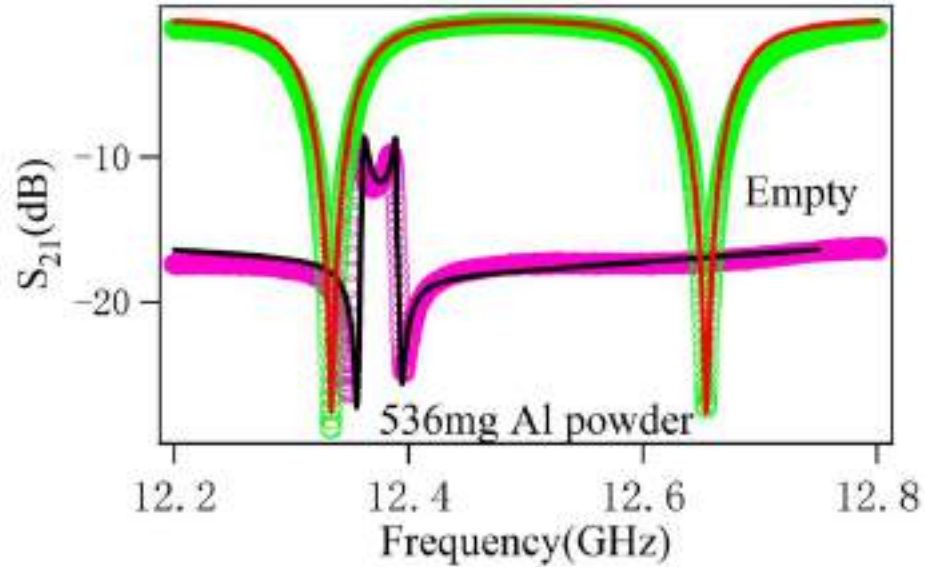
6.5.4 Water

6.5.5 Icing sugar (powder) humidity from 0-10%

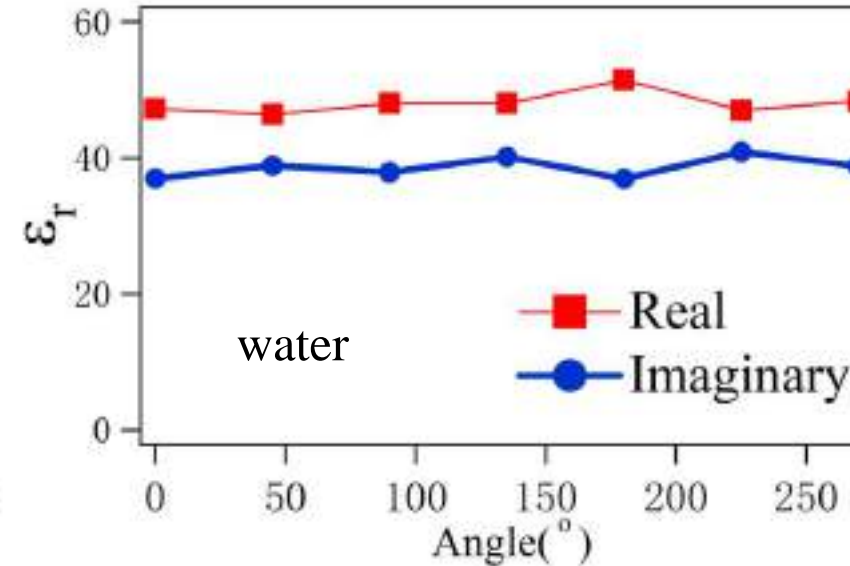
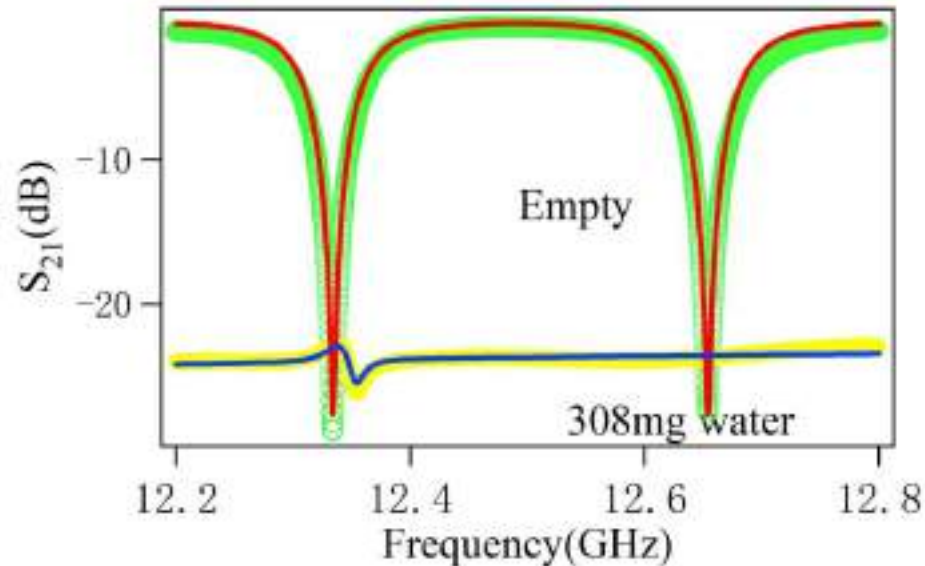


6.5.6 Fuel oil (car gasoline and diesel)

Problem: water and Al powder

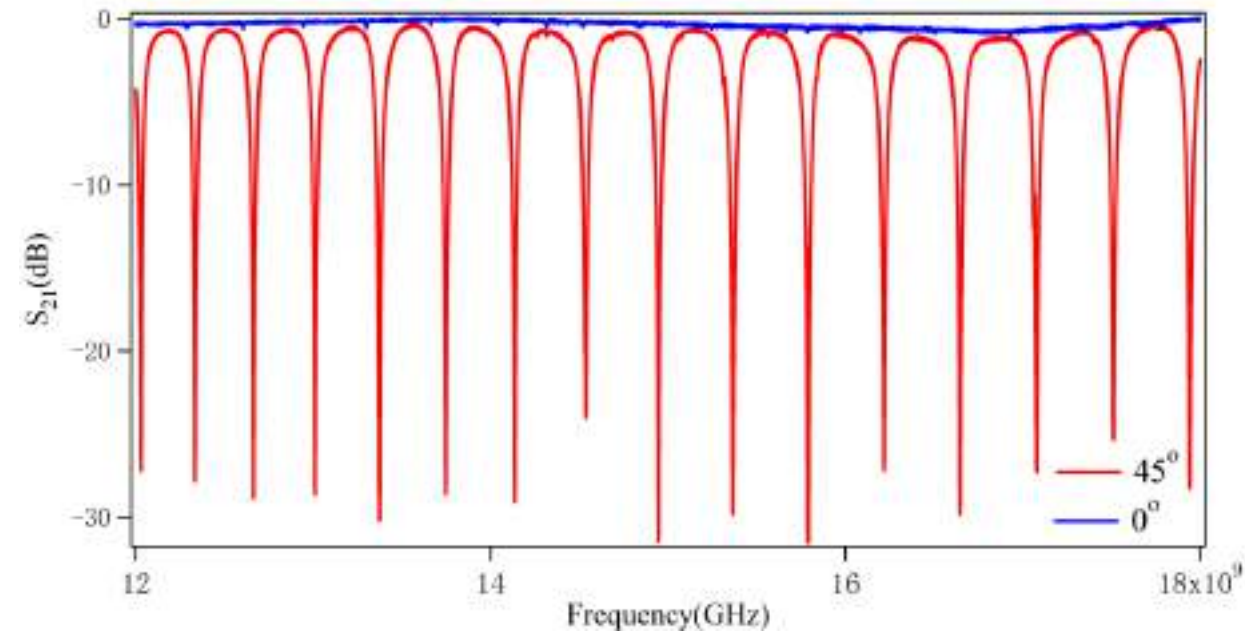
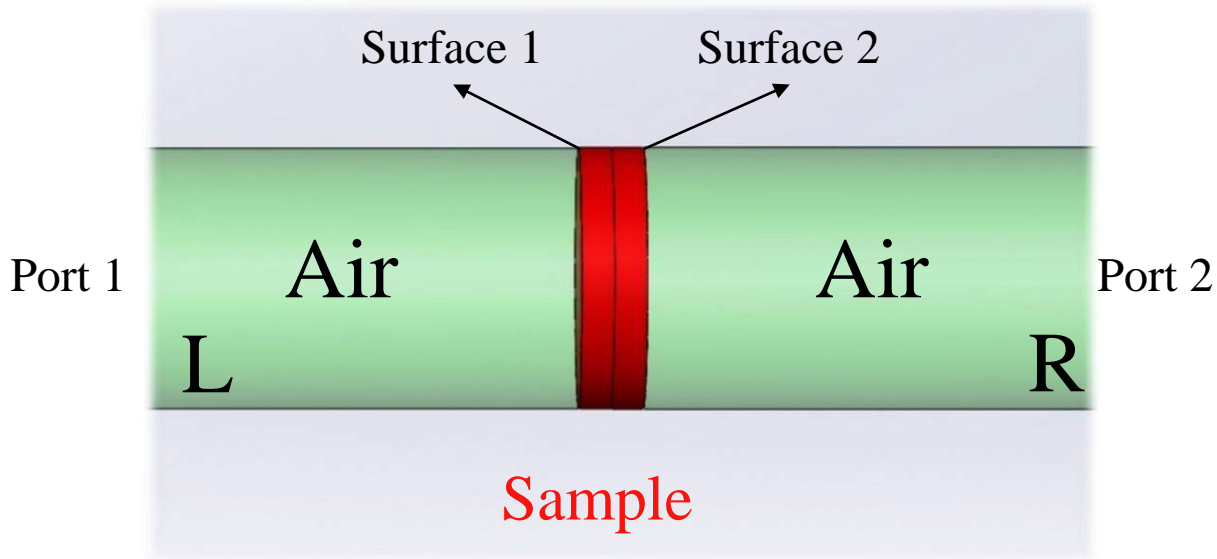


$$\epsilon_r = 199.65 + 0.96i$$
$$\Delta\epsilon_r = 3.7\%$$



$$\epsilon_r = 45.12 + 38.00i$$
$$\Delta\epsilon_r = 7.9\%$$

Non-resonant measurement (theta = 0°)

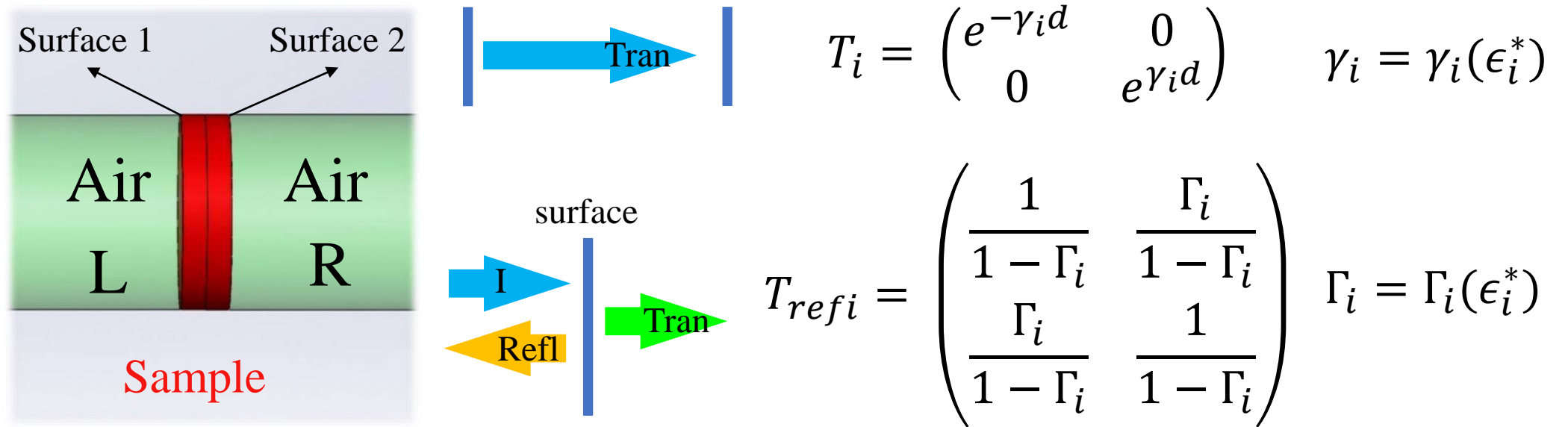


$$M_i = L \cdot T_{refi} T_i T_{refi}^{-1} \cdot R$$

$$M_i = \begin{pmatrix} S_{12}^i - \frac{S_{11}^i S_{22}^i}{S_{21}^i} & \frac{S_{11}^i}{S_{21}^i} \\ -\frac{S_{22}^i}{S_{21}^i} & \frac{1}{S_{21}^i} \end{pmatrix}$$

- ➔ Measure 4 S parameters
- ➔ Define transfer matrix
- ➔ Fit result

Definition of transfer matrix



$$M_i = L \cdot T_{refi} T_i T_{refi}^{-1} \cdot R$$

Sample measure

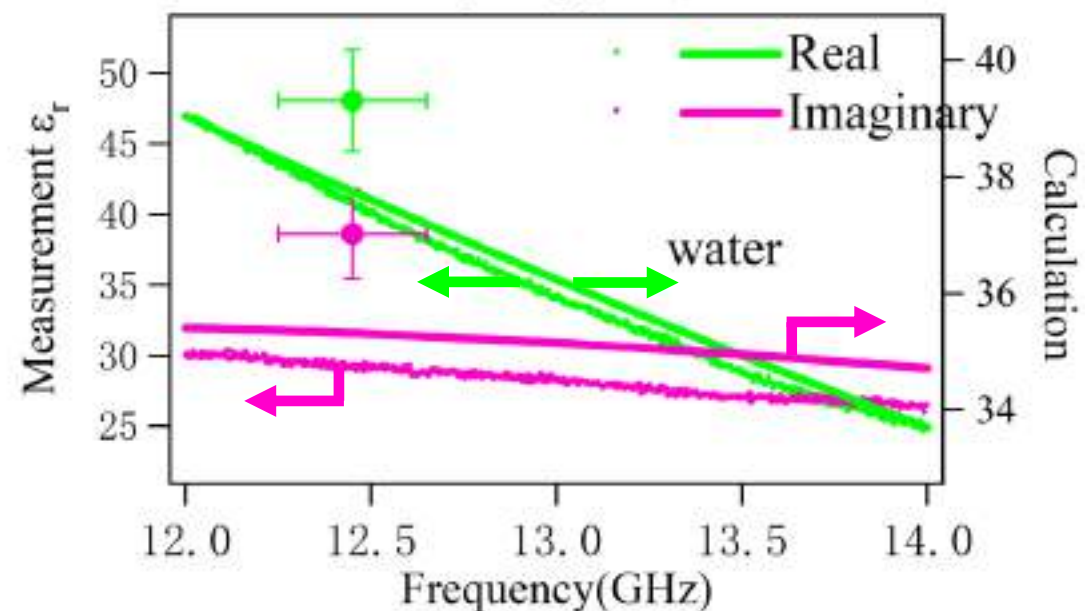
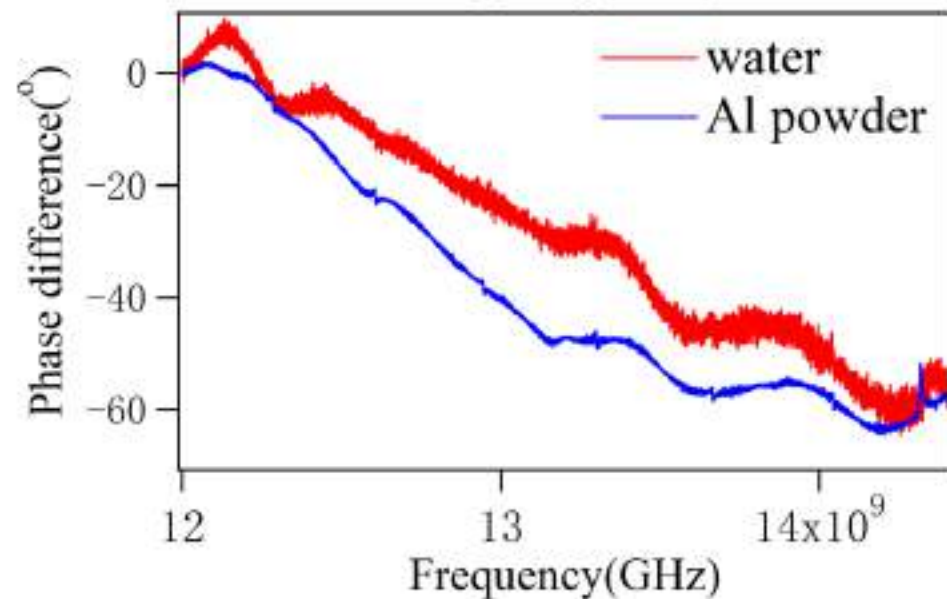
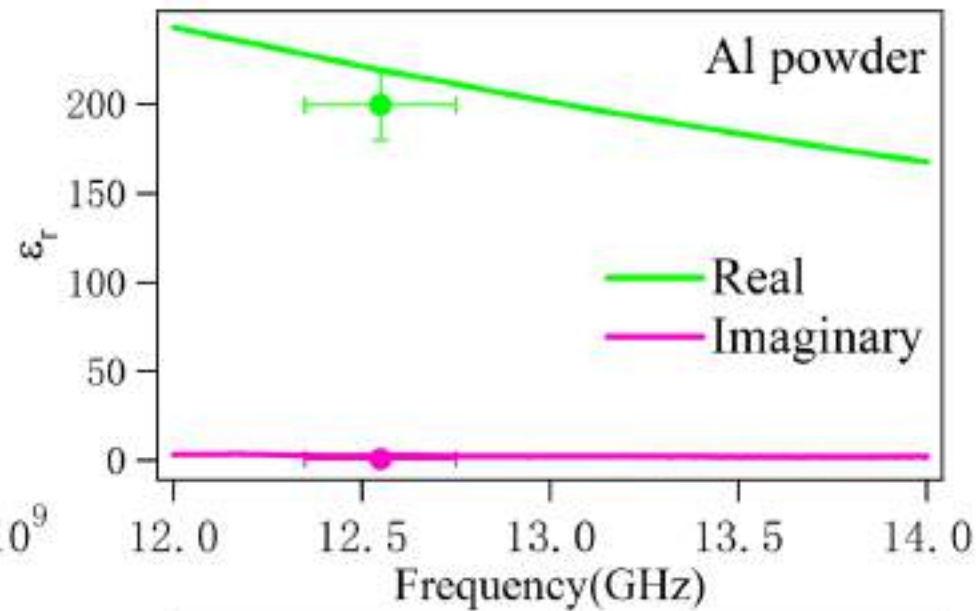
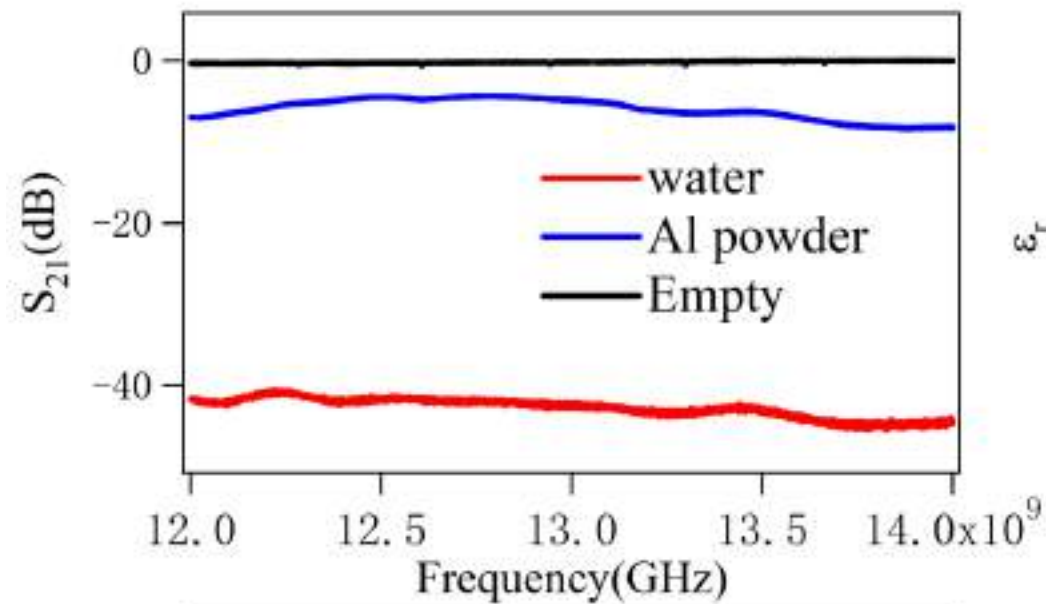
$$M_0 = L \cdot T_{ref0} T_0 T_{ref0}^{-1} \cdot R$$

Standard measure

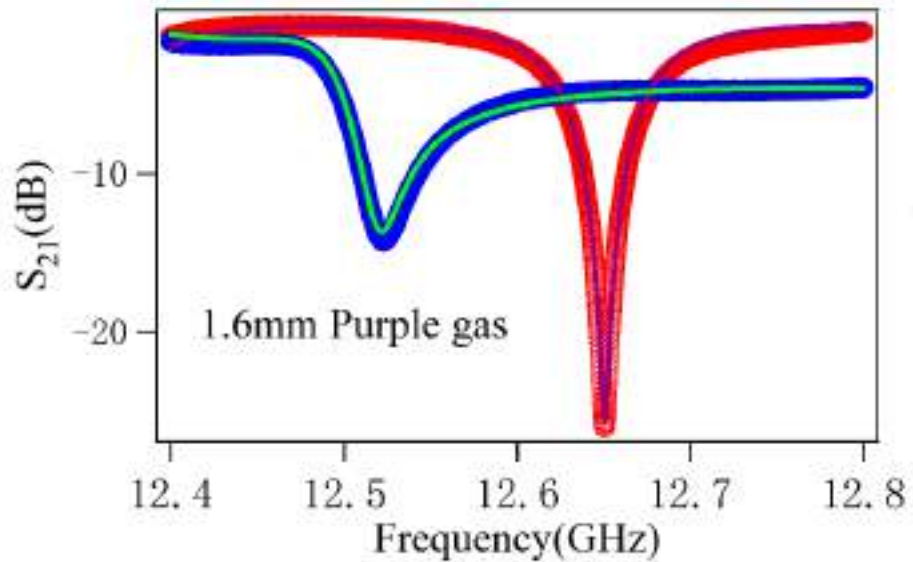
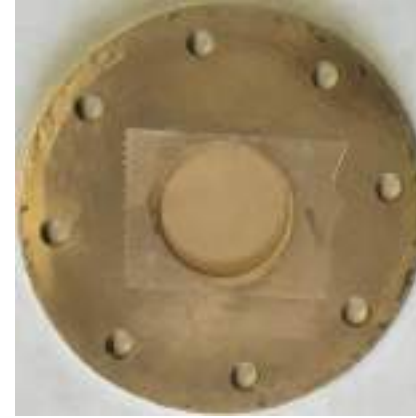
$$M_0^{-1} = R^{-1} \cdot T_{ref0}^{-1} T_0^{-1} T_{ref0} \cdot L^{-1}$$

~~$$M_i M_0^{-1} = (T_{refi} T_i T_{refi}^{-1} T_{ref0}^{-1} T_0^{-1} T_{ref0} T_i T_{refi}^{-1} T_{ref0}) L^{-1}$$~~

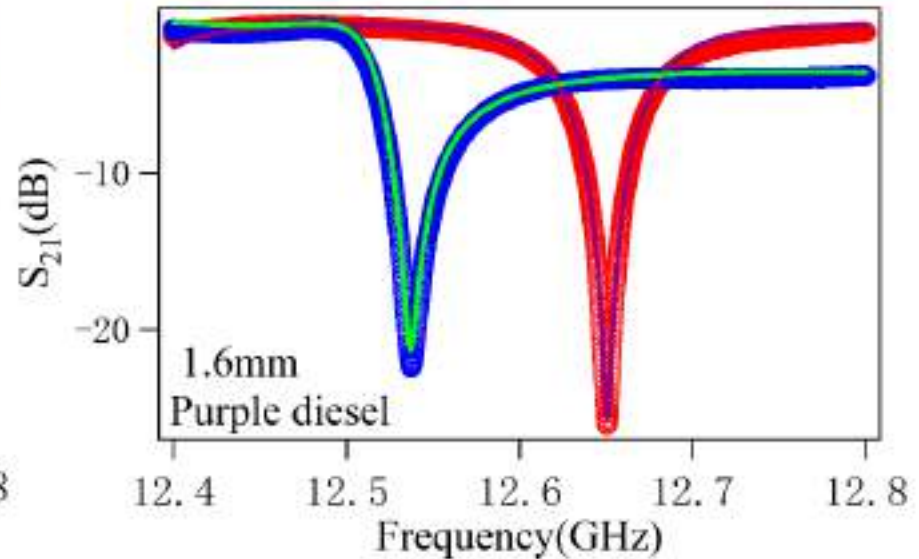
Raw data and fitting results



Car fuel Measurement



$$\epsilon_r = 3.016 + 0.196i$$



$$\epsilon_r = 2.666 + 0.028i$$

Task list

6.5.1 NaCl, NH_4NO_3 , KNO_3 , NaNO_3 , KClO_3 varying humidity from 0-10%



6.5.2 Mixing two powders of varying humidity from 0-10%



6.5.3 Aluminum powder



6.5.4 Water



6.5.5 Icing sugar (powder) humidity from 0-10%



6.5.6 Fuel oil (car gasoline and diesel)



Next step

- Redo measurement of water.