QUESTION 1:

a)

Step 11 of the assignment asks for an implementation of a method that will produce a string that describes the elements of two lists in a pairwise fashion: For example when give 2 and 4 it will become (2, 4)

It is easy to do this for a Nil list: just return self:

```
def zip(self, other): # in the Nil class return self
```

What code should we use in the Cons class? The problem here is that we need to decide which number should be put first and which number will be second (the order), and to make the decision, we need to know whether the tail of list is empty or not. In pseudo code, this might look something like the following:

```
def zip(self, other): # in the Cons class
if other.tail is an empty list:
    return self
else:
    return Cons( (other.head, self.head), other.tail.zip(self.tail))
```

The "other.tail an empty list" part of this code is not valid code, but we can eliminate it by using the dynamic dispatch pattern shown above. The first step is to rewrite the definition of commaElements in the Cons class (we'll figure out what to use in place of "..." shortly, but for now it's just a placeholder):

```
def zip(self, other): # in the Cons class
  return other.zipElement(...)
```

Next we add implementations of the new zipElement method in each of the Nil and Cons classes:

```
def zipElement(self, ...): # in the Nil class
  return self

def zipElement(self, ...): # in the Cons class
  return Cons( (other.head, self.head) , other.tail.zip(self.tail))
```

Now we can see that both of these methods require "head" as an input, so we can pass that value as a parameter in the calls to zipElement:

```
def zip(self, other): # in the Cons class
  return other.zipElement(self)

def zipElement(self, other): # in the Nil class
  return self

def zipElement(self, other): # in the Cons class
  temp = other.head, self.head
  return Cons(temp, other.tail.zip(self, Tail))
```

Together, those three method definitions complete the implementation of zip().

b) This is screenshot my code:

```
def zip(self,other):
26
            return self
27
       def zipElement(self,other):
28
            return self
       def zip(self,other):
60
            return other.zipElement(self)
61
62
        def zipElement(self,other):
 63
            temp = other.head, self.head
            return Cons(temp, other.tail.zip(self.tail))
```

c) Thoughtful Test: I have created three more test for code.

First is num(0,4).zip(num(2,6)). The reason I choose this is to try function part get same number with object part which 4 in (0,4) of function part is same 4 in (2,6) of object part. The output I except is 4 parts, because (0,4) only include 4 numbers which same with (2,6). The number will begin at 0 and end at 4. Begin at 2 end at 5. It will come out (0,2) (1,3) (2,4) (3,5)

Second is num(10,13).zip(num(1,9)). The reason I choose this is to try function part get more number than object part which 8 in (1,9) of function part is more than 3 in (10,13) of object part. The output I except is only 3 parts, because (10,13) only include 3 numbers which smaller than (1,9). The number will begin at 10 and end at 12. Begin at 1 end at 3. It will come out (10, 1) (11,2) (12,3)

Third is num(11,19).zip(num(3,7)). The reason I choose this is to try function part get smaller number than object part which 4 in (3,7) of function part is smaller than 8 in (11,19) of object part. The output I except is only 4 parts, because (3,7) only include 4 numbers which smaller than (11,19) the number will begin at 11 and end at 14. Begin at 3 end at 6. It will come out (11, 3) (12,4) (13,5) (14,6)

```
116 print('TEST HW6')
117 print(nums(0,6).zip(nums(1,7)))
118 print(nums(0,6).zip(nums(0,3)))
119 print(nums(0,3).zip(nums(0,6)))
120 print(nums(0,4).zip(nums(2,6)))
121 print(nums(10,13).zip(nums(1,9)))
122 print(nums(11,19).zip(nums(3,7)))
```

I get same result which I except.

```
TEST HW6
[(0, 1), (1, 2), (2, 3), (3, 4), (4, 5), (5, 6)]
[(0, 0), (1, 1), (2, 2)]
[(0, 0), (1, 1), (2, 2)]
[(0, 2), (1, 3), (2, 4), (3, 5)]
[(10, 1), (11, 2), (12, 3)]
[(11, 3), (12, 4), (13, 5), (14, 6)]
```

QUESTION 2:

a) The vars functions return the list of variables in an arbitrary Prop value.

```
TRUE class:
       def vars(self):
          return []
FALSE class:
       def vars(self):
          return []
VAR class:
       def vars(self):
          return [self.name]
AND class:
       def vars(self):
          return self.p.vars() + self.q.vars()
OR class:
       def vars(self):
          return self.p.vars() + self.q.vars()
NOT class:
       def vars(self):
          return self.p.vars()
Test: add three more test which listed above.
I try to test all 6 vars functions I implemented in 6 classes.
The result expected should be: [ABAB], [AB], [AB], [ABAB]
```

```
= VAR("A")
144 a
145 b
          = VAR("B")
\frac{146}{146} \text{ left} = AND(a, NOT(b))
147 right = AND(NOT(a), b)
148 example = OR(left, right)
149 test = AND(left, right)
150
151 # Print out the example expression in text and tre
152 print(example)
153 print(example.apic())
154
155 print('TESTING')
156 print(example.vars())
157 print(left.vars())
158 print(right.vars())
159 print(test.vars())
160 print('TESTING')
```

The result is same with expected it shows below.

```
TESTING
['A', 'B', 'A', 'B']
['A', 'B']
['A', 'B']
['A', 'B', 'A', 'B']
TESTING
```

```
TRUE class:
       def eval(self, env):
         return true
FALSE class:
       def eval(self, env):
         return false
VAR class:
       def eval(self, env):
         return env.get(self.name)
AND class:
       def eval(self, env):
         return self.p.eval(env) and self.q.eval(env)
OR class:
       def eval(self, env):
         return self.p.eval(env) or self.q.eval(env)
       def eval(self, env):
         return not self.p.eval(env)
Test: add six more test: True and True, False and True, False and False.
Expectation or these 4: True, False, True, False, False, True, False
Left = AND(False, Not True) -> False . right = AND(NOT False, True) -> True
test have different result with example when two False input, which will come out False.
 print('TESTING')
 print(example.eval({'A': True, 'B': False}))
```

```
print('TESTING')
print(example.eval({'A': True, 'B': False}))
print(example.eval({'A': True, 'B': True}))
print(example.eval({'A': False, 'B': True}))
print(example.eval({'A': False, 'B': False}))
print(left.eval({'A': False, 'B': True}))
print(right.eval({'A': False, 'B': True}))
print(test.eval({'A': False, 'B': False}))
print('TESTING')
```

The result is same with expected it shows below.

```
TESTING
True
False
True
False
False
True
False
True
False
TESTING
```

```
TRUE class:
       def eqTRUE(self):
         return True
       def __eq_(self,other):
         return other.eqTRUE()
FALSE class:
       def eqFALSE(self):
         return True
       def __eq__(self,other):
         return other.eqFALSE(self)
VAR class:
       def eqVAR(self,other):
         return True
       def eq (self,other):
         return other.eqVAR(self)
AND class:
       def eqAND(self):
         return True
       def eq (self,other):
         return other.eqAND(self)
OR class:
       def eqOR(self):
         return False
       def __eq__(self,other):
         return other.eqOR(self)
NOT class:
       def eqNOT(self):
         return True
       def __eq__(self,other):
         return other.eqNOT(self)
Test: add three more test. Expect it will come out: True False True False
  print('TESTING')
  print(VAR("A") == VAR("A"))
```

My TURE and FALSE part is ok. But others no works good. If want to test, you can just implement TURE, FALSE and NOT part.

The result is same with expected it shows below.

print(FALSE == TRUE)
print(FALSE == FALSE)
print(NOT(TRUE) == TRUE)

print('TESTING')

TESTING True False True False TESTING