

## Gap Year Planning

January 29: 5:00 – 6:30 pm

Zoom only: <https://arizona.zoom.us/j/82615759625>

Do you find yourself thinking...

“I want to go to grad school, but don’t have enough research experience to be competitive.”

“What do I do if I don’t get into grad school?”

“I’m not clear on what I want to do after graduation.”

This panel discussion focuses on post-graduation options, featuring UA Astronomy & Physics Alumni who took a gap year between their undergraduate studies and their next careers in industry or academia. Learn why and how they took advantage of a gap year to find clarity and move further toward their goals.



Jiyun Di  
Astronomy & Math, 2022



Olivia Pitcl  
Physics, 2023



Sai Krishanth PM  
Physics & Astronomy, 2022



Charlie Goldberg  
Physics & Astronomy, 2023

Panelist bios  
and Zoom  
link here ➔



# ASTR400B Lecture 4

## Rotation Curve

- the velocity a test particle would have if it was on a circular orbit in an axially-symmetrized version of a galaxy's mass distribution. (**Jo Bovy**)

$$GMm/R^2 = mV^2/R$$

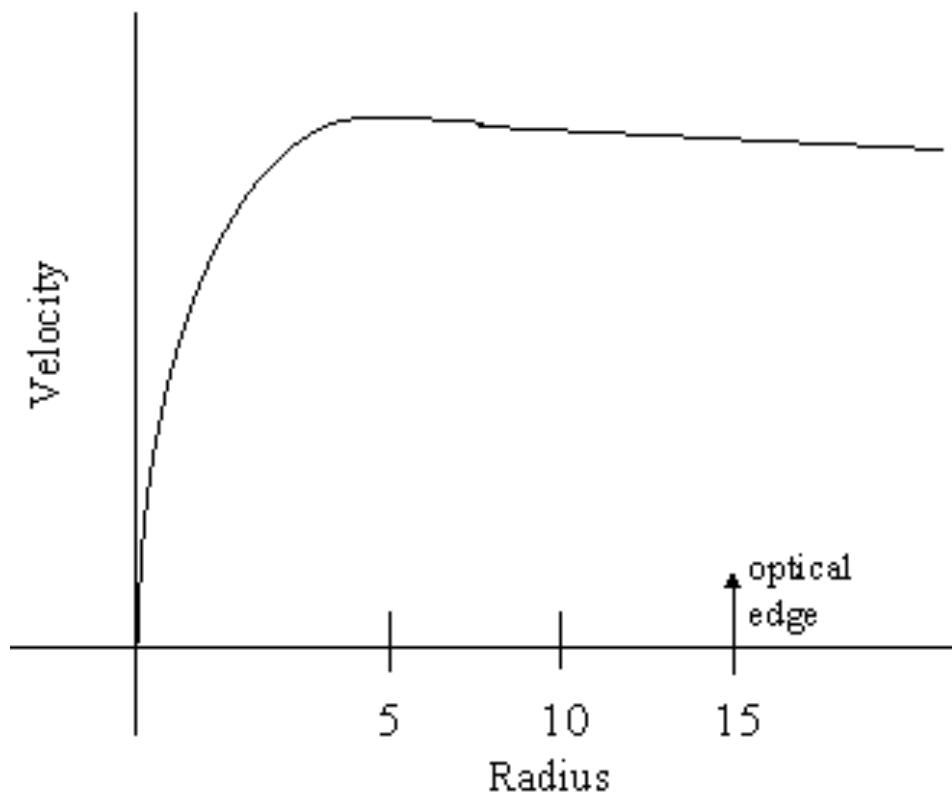
$$M(< R) \propto V^2 R$$

$$v_c(R)=\sqrt{GM(< R)/R}$$

$$v_c(R)=Rw$$

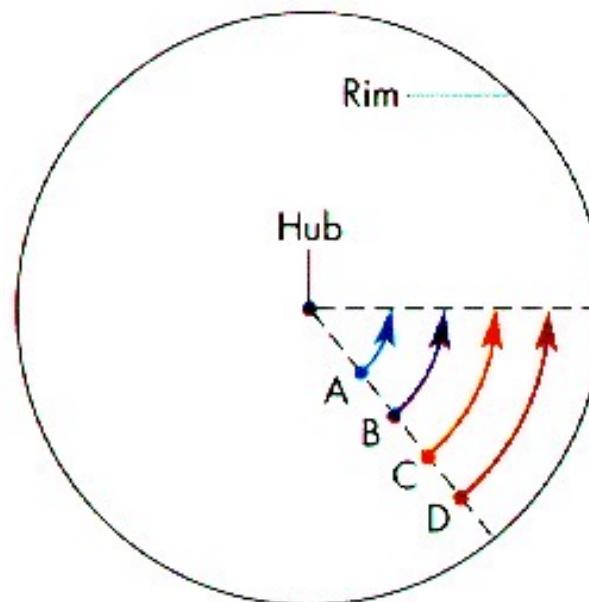
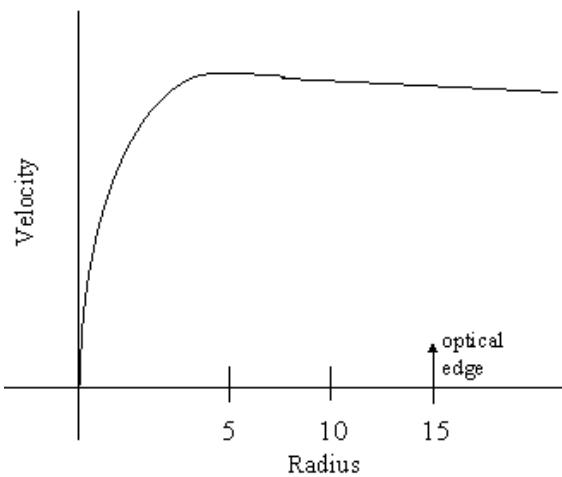
$$\scriptstyle 3$$

Rotation curve of typical galaxy



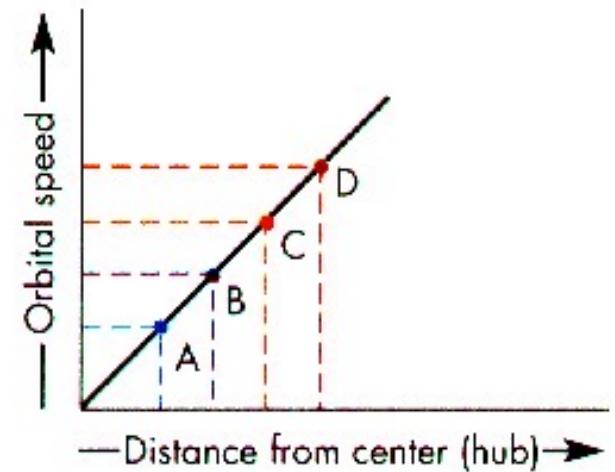
# Solid Body Rotation. $\omega = \text{constant}$

Rotation curve of typical galaxy



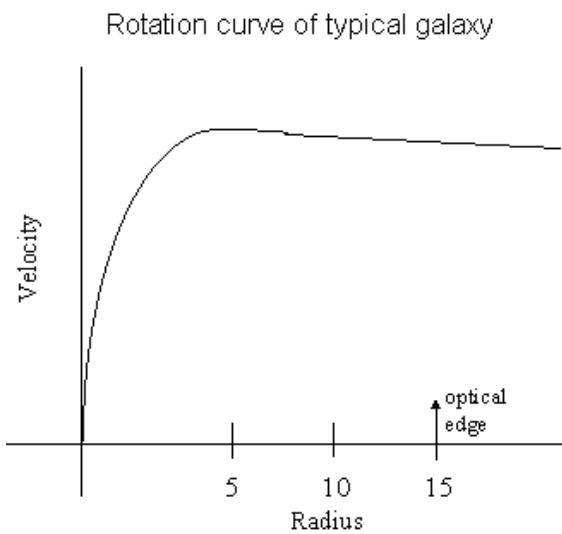
**Wheel-like rotation**

$V \propto R$   
Density is constant

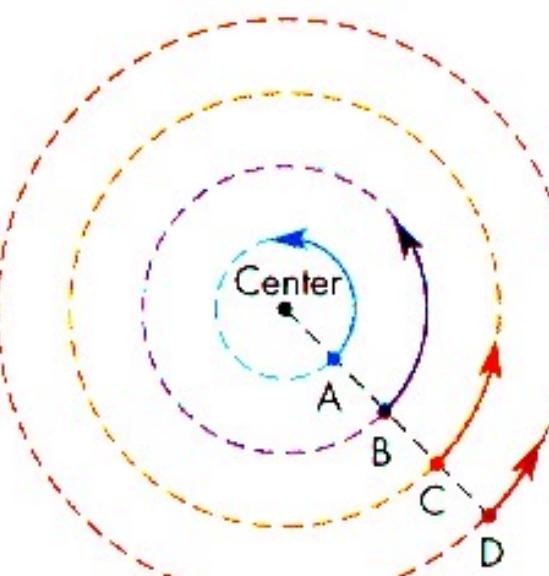


**Rotation curve for  
wheel-like rotation**

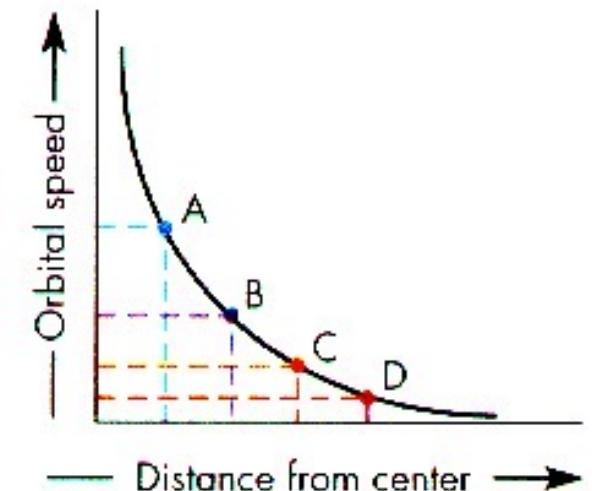
# Keplerian Rotation (mass is constant and at center)



$$V \propto R^{-1/2}$$

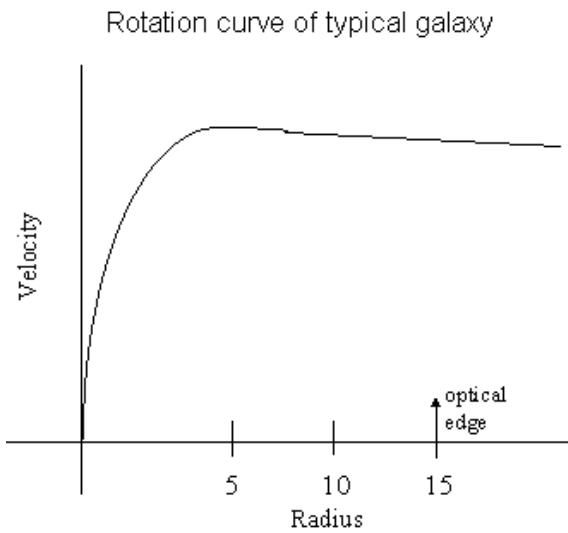


**Planet-like rotation**



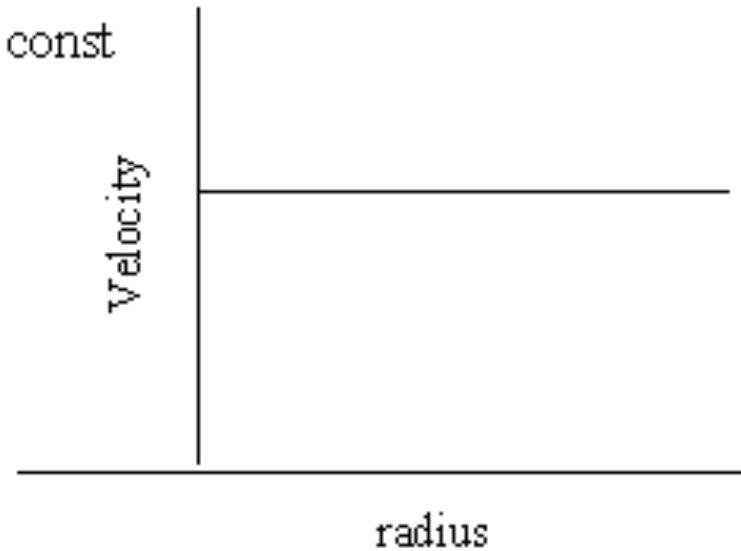
**Rotation curve for planet-like rotation**

# Flat Rotation Curve, V is constant

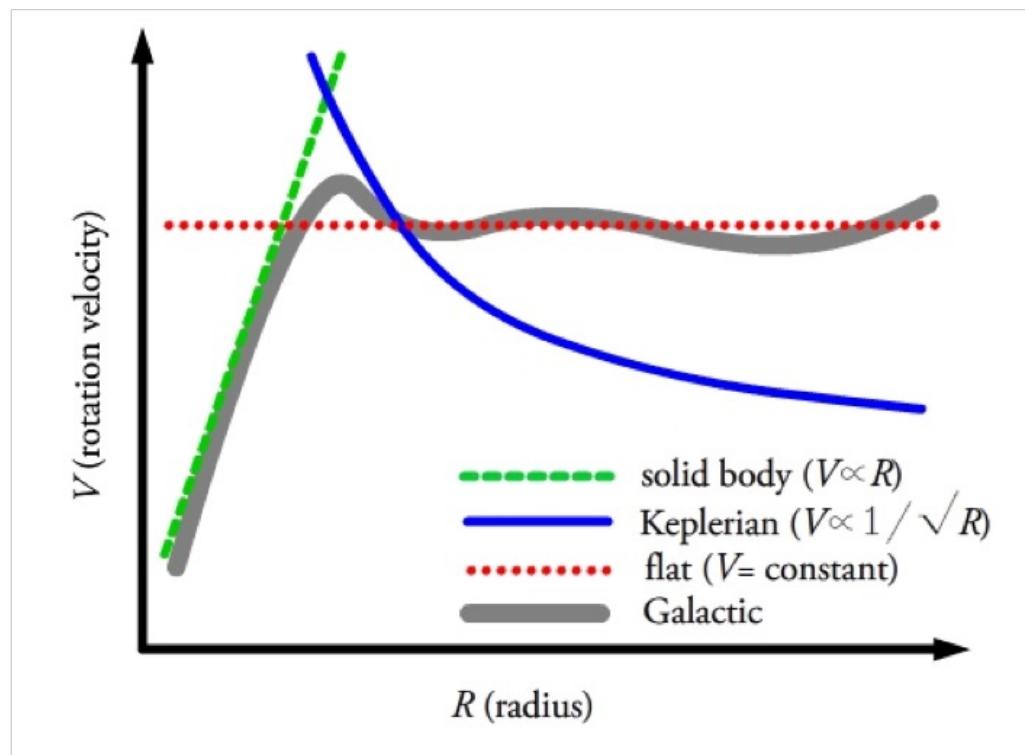


$$M \propto R$$

$$V = \text{const}$$



# Rotation curve and the dark matter

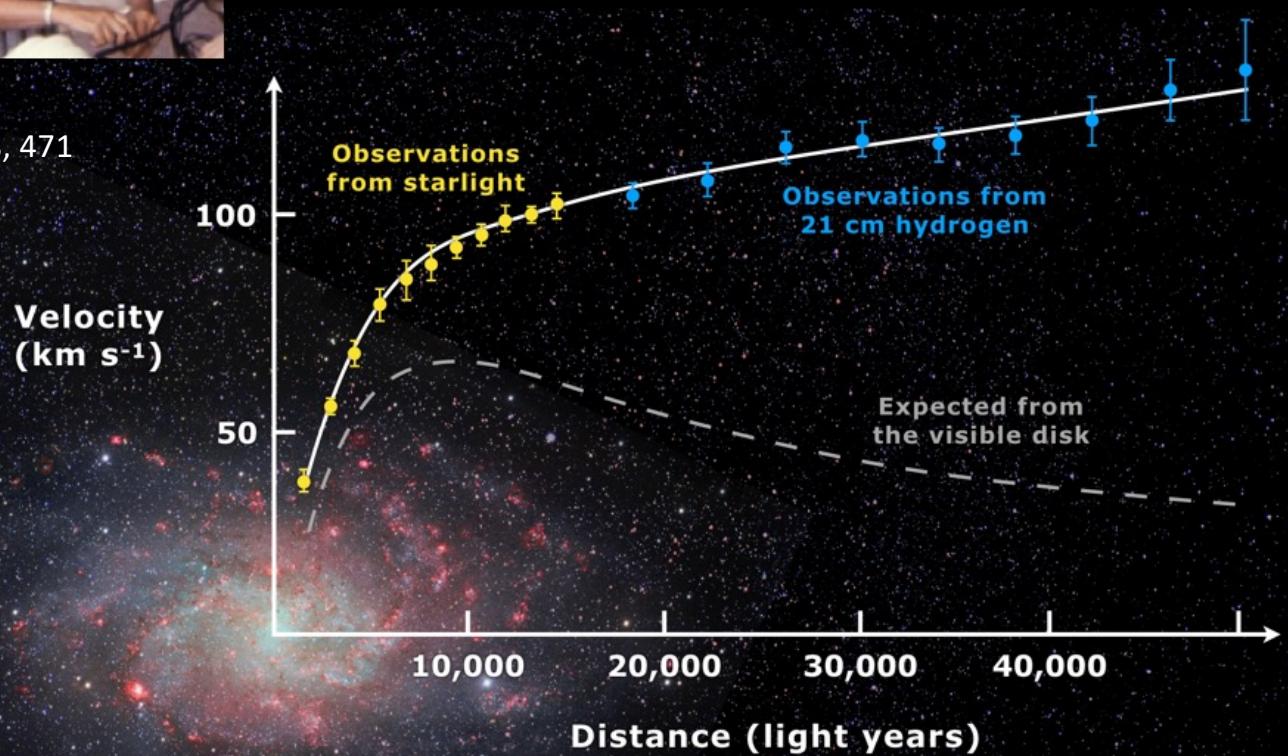


[https://en.wikipedia.org/wiki/Oort\\_constants](https://en.wikipedia.org/wiki/Oort_constants)



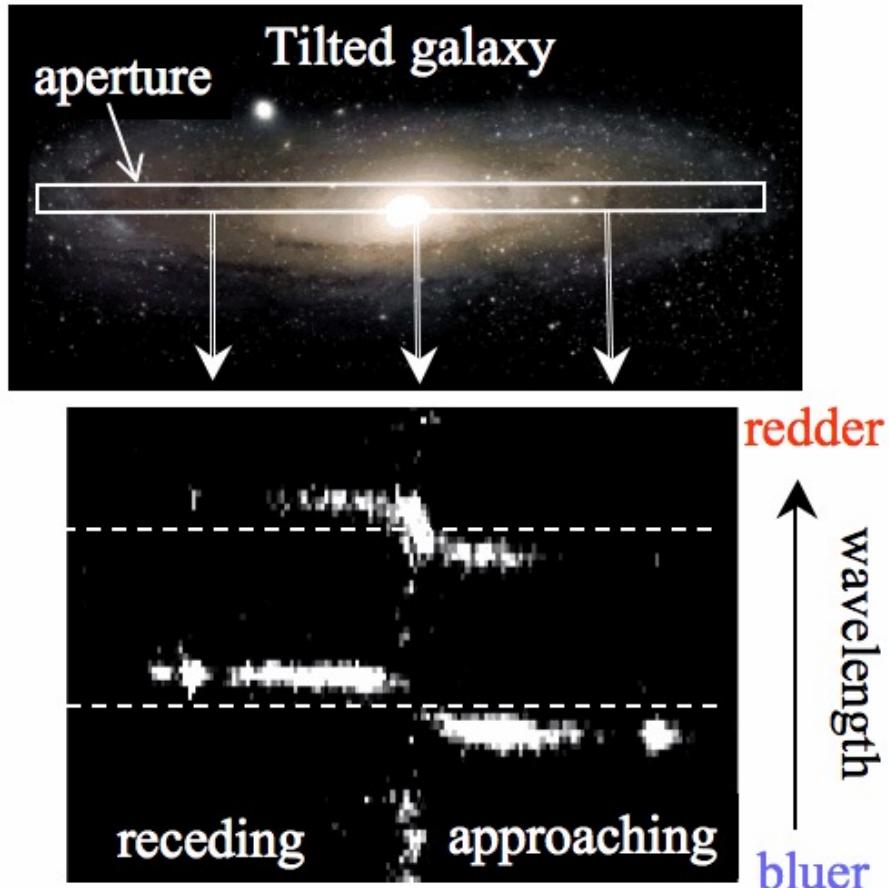
Vera Rubin measured that stars in galaxies are moving faster than they should be, inferring the existence of an unseen mass we call “dark matter”

Rubin+1980 AJ, 238, 471

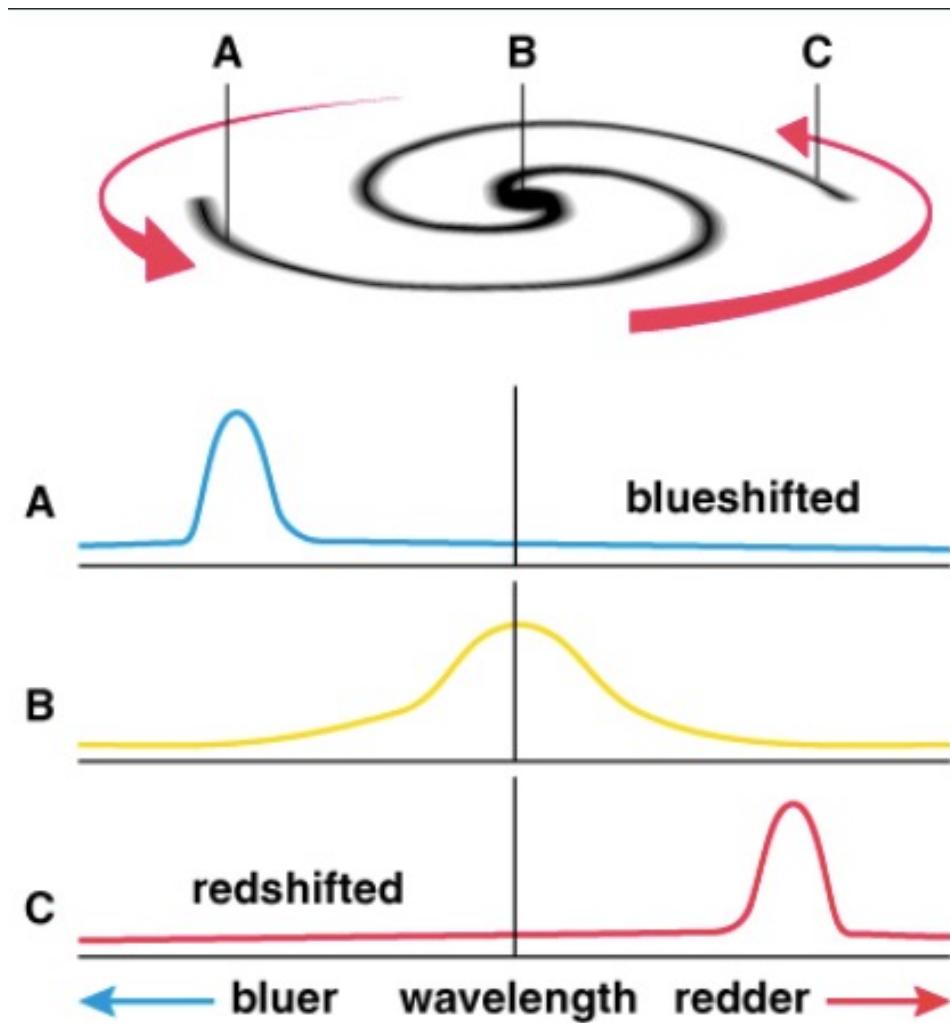




Vera Rubin measuring galaxy rotation curves (~1970)



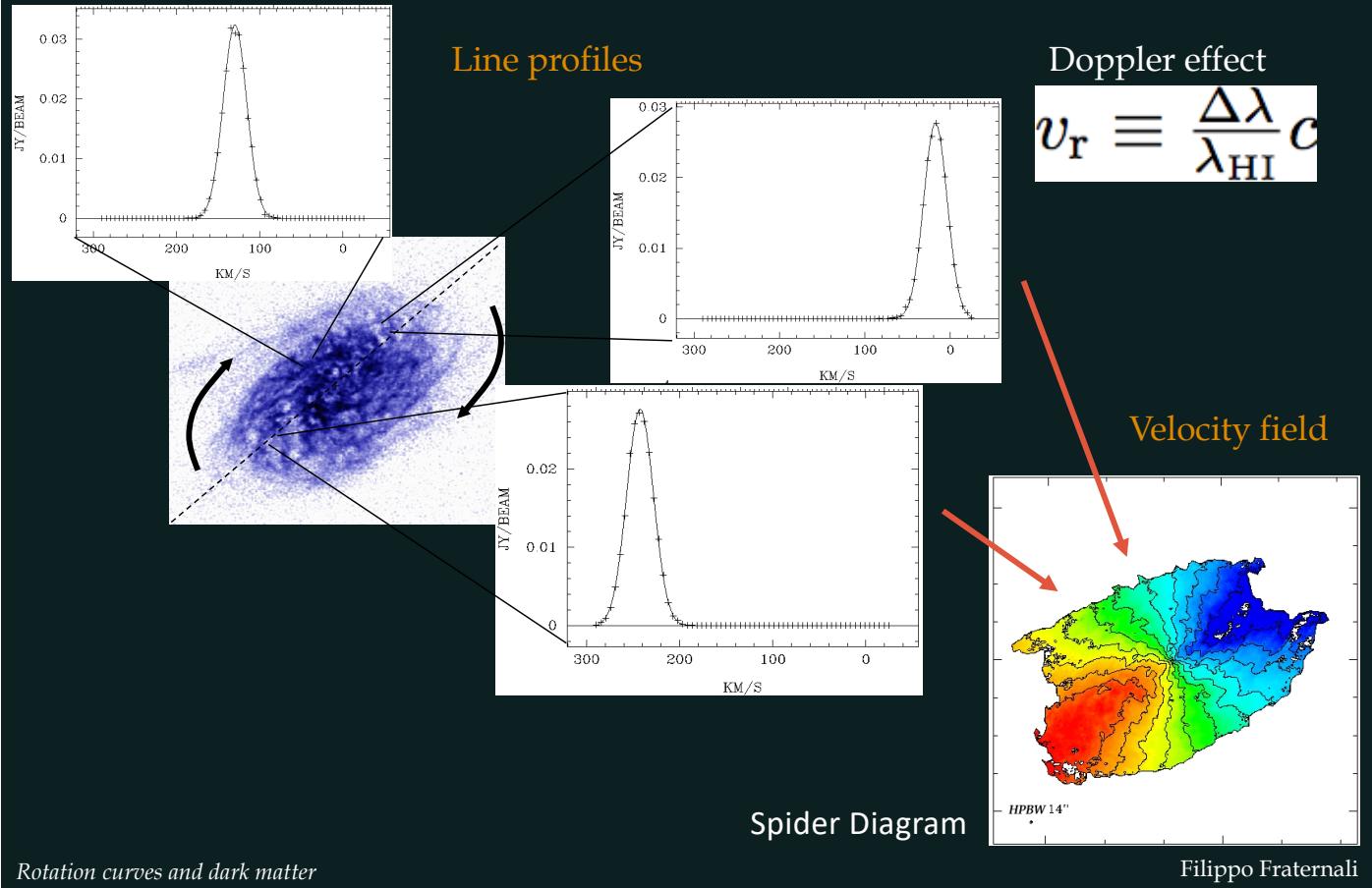
Resulting spectrum of light within aperture



Copyright © Addison Wesley.

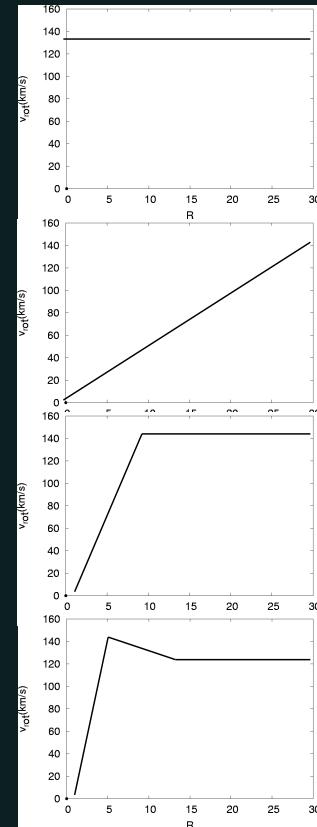
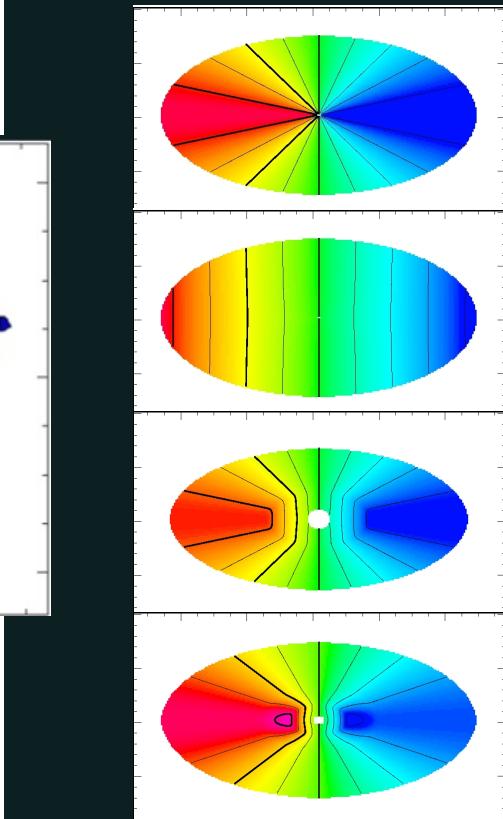
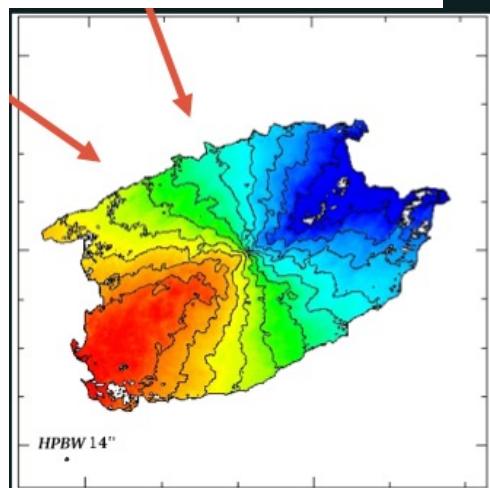
2D

# Rotation of a galactic disc



# Velocity fields versus rotation curves

$$V_{\text{LOS}} = v_{\text{sys}} + v_R \sin(\varphi) \sin(i) + v_\varphi \cos(\varphi) \sin(i) + v_z \cos(i)$$



Flat  $M \sim R$

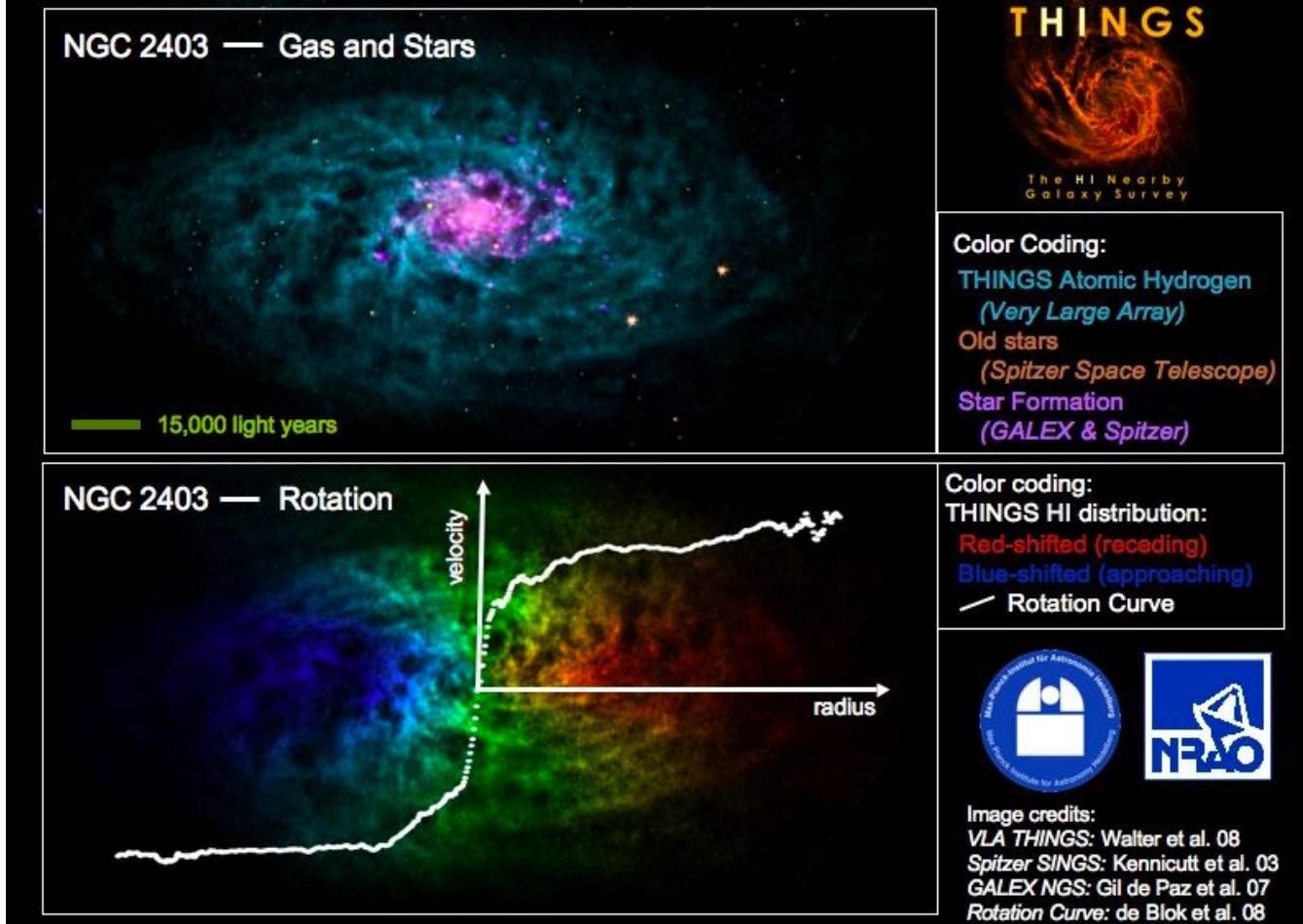
Solid body

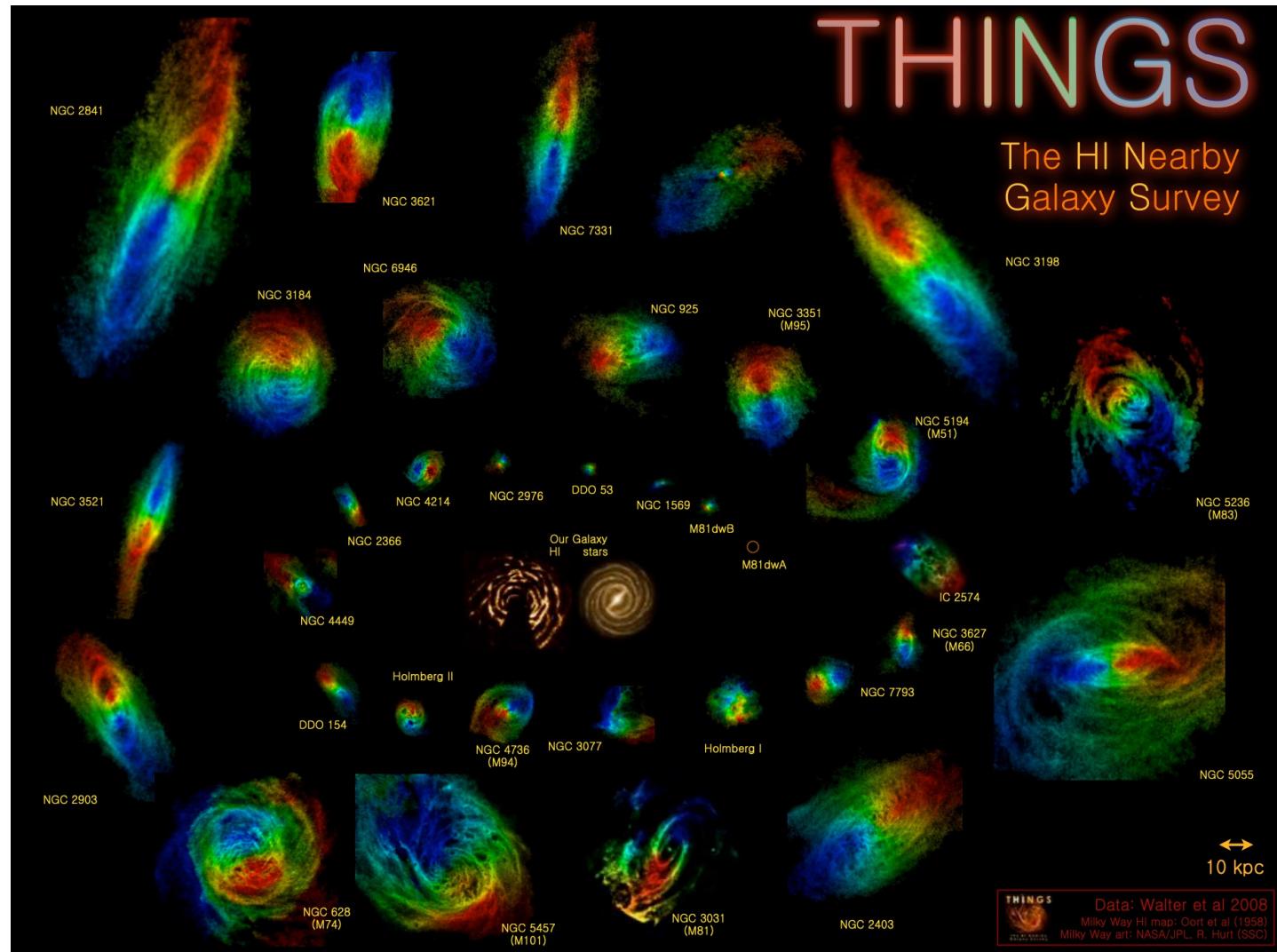
Rising + flat

Rise+decline+flat

Filippo Fraternali

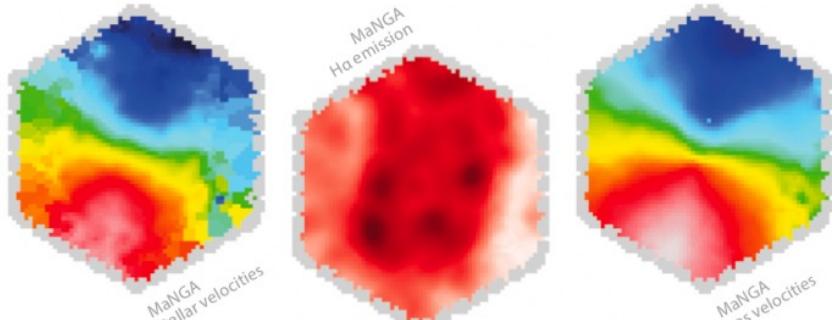
# Galaxy Dynamics in THINGS — The HI Nearby Galaxy Survey





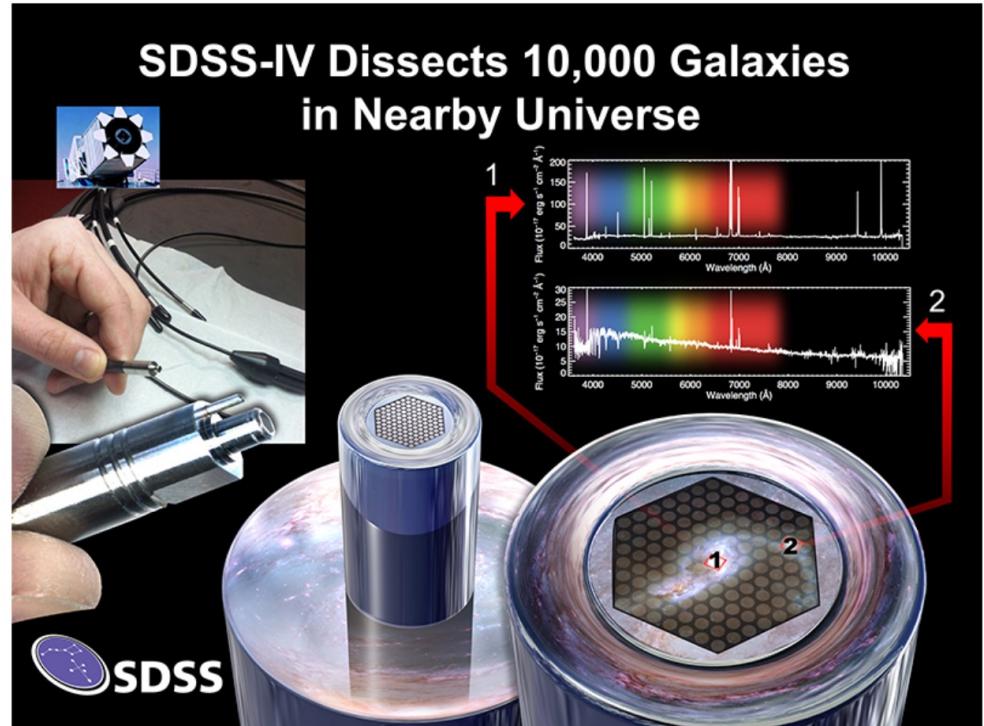
# IFUs : SDSS V, IV

(Integral Field Units)



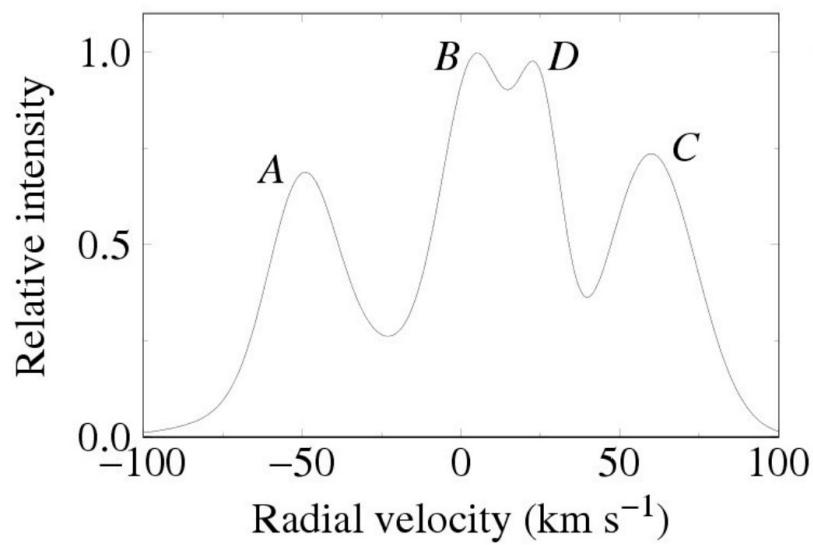
Credit: Francesco Belfiore, Univ. of St Andrews Print & Design.

Bundy + 2015



MaNGA obtains spectra across the entire face of target galaxies using custom designed fiber bundles. The bottom right illustrates how the array of fibers spatially samples a particular galaxy. The top right compares spectra observed by two fibers at different locations in the galaxy, showing how the spectrum of the central regions differs dramatically from outer regions. Image Credit: Dana Berry / SkyWorks Digital Inc., David Law, and the SDSS collaboration.

Galactic rotation: a gas cloud at marked points. Gas cloud at C with longitude  $l$  and Galactocentric radius  $R$ , at distance  $d$  from the Sun, orbits with speed  $V(R)$ . The line of sight is closest to the Galactic center at the tangent point, C.



NOTE: This only works within  $R_{\text{sun}}$

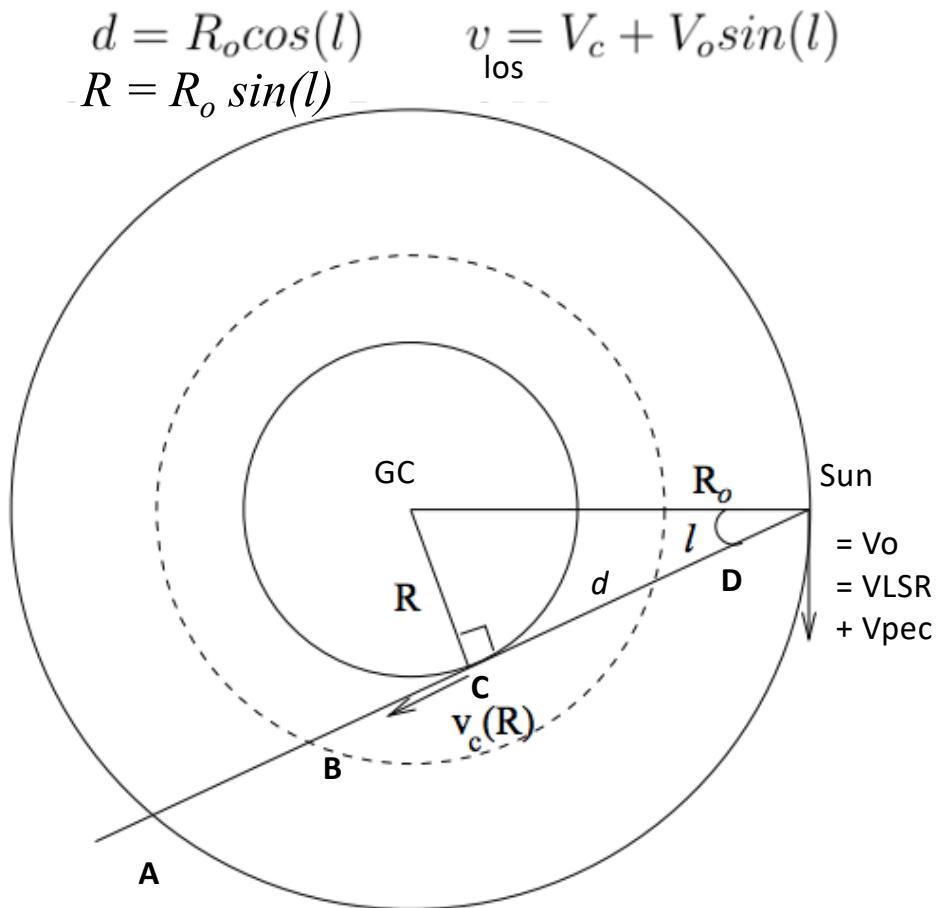


Figure 1: The tangent point method

To compute the MW's rotation Curve we need to measure:

- **VLSR** Velocity of the Local Standard of Rest
  - Equivalent to the velocity a test particle would have if it was on a circular orbit at the location of the Sun
  - (this is not the Sun's motion).
- **R<sub>0</sub>** : Distance of the Sun from the Galactic Center
- **V<sub>pec</sub>** : Peculiar motion of the Sun with respect to the VLSR

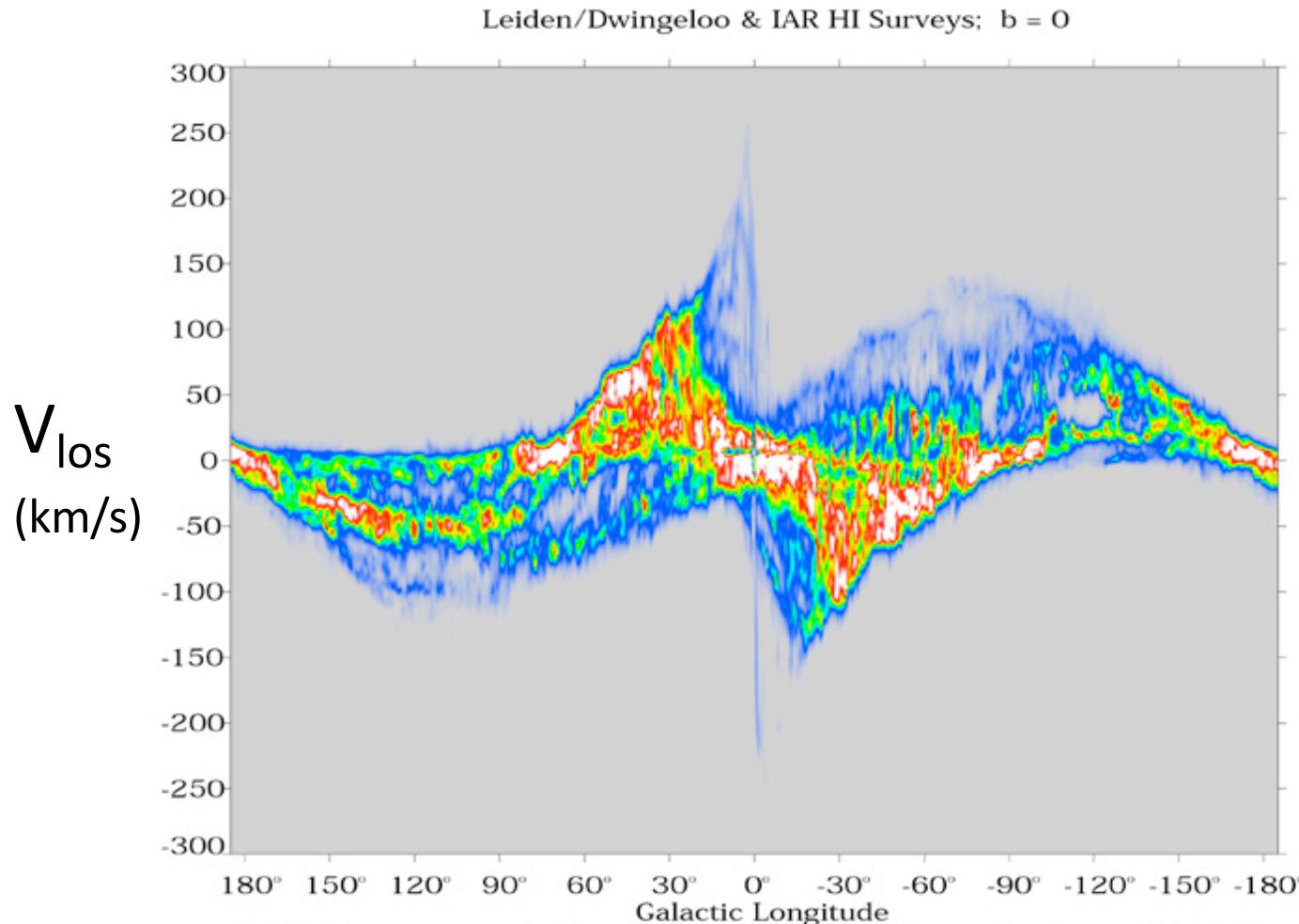


Fig 2.20 (D. Hartmann) 'Galaxies in the Universe' Sparke/Gallagher CUP 2007

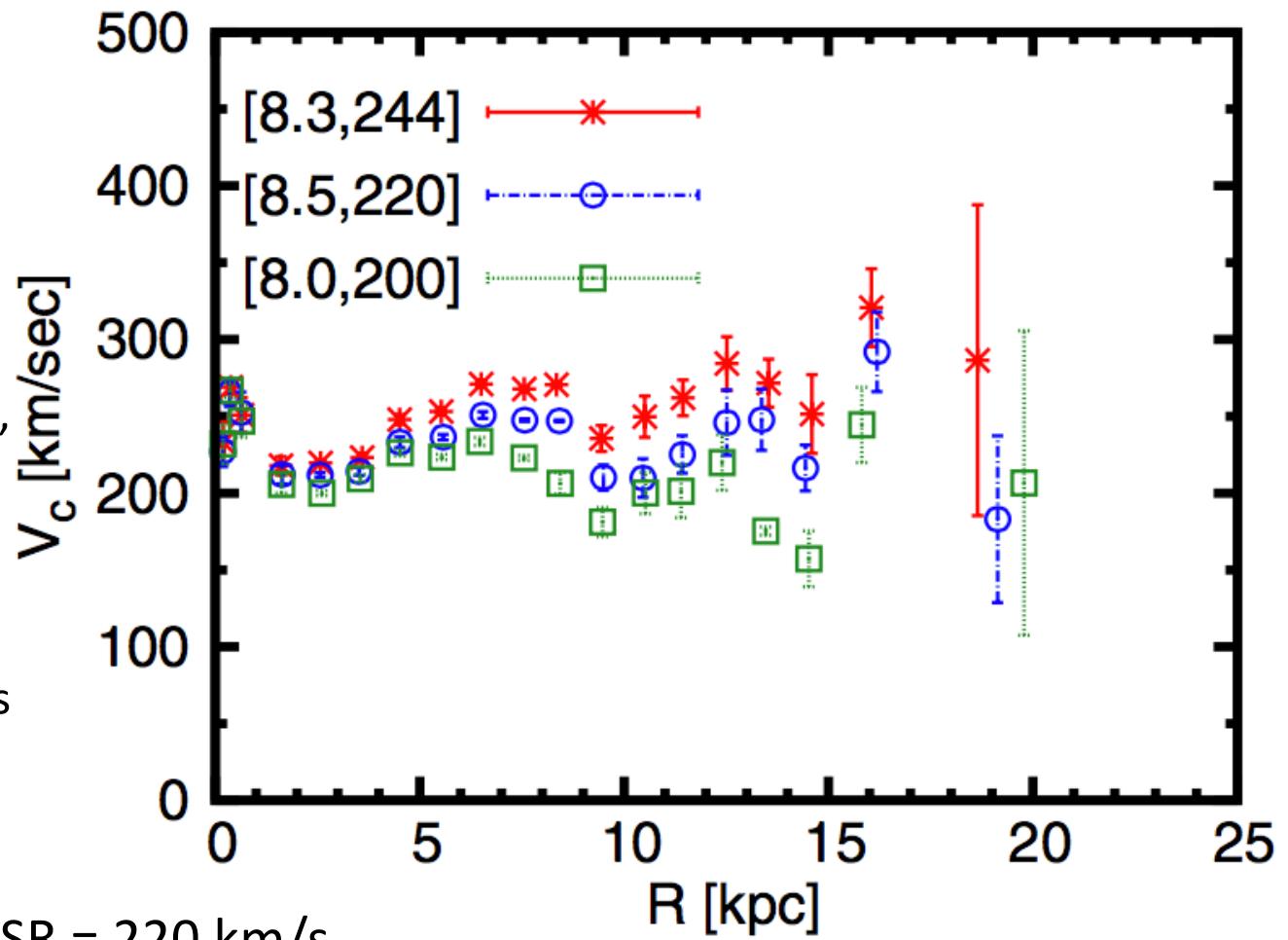
Longitude  
Velocity  
Diagram for  
the MW

In the plane of the disk, the intensity of 21 cm emission from neutral hydrogen moving toward or away from us with velocity  $V_{\text{LSR}}$  measured relative to the local standard of rest.

Yields terminal  
velocity at  
each Galactic I

Bhattacharjee + 2014 ApJ  
785 Fig. 2

Average rotation curves obtained by weighted averaging over the combined  $V_c$  data from all the disk tracer samples (HI, Cepheids, HII regions, Carbon stars, CO), for three different sets of values of  $[(R_o/kpc), (V_{LSR}/km\ s^{-1})]$  as indicated

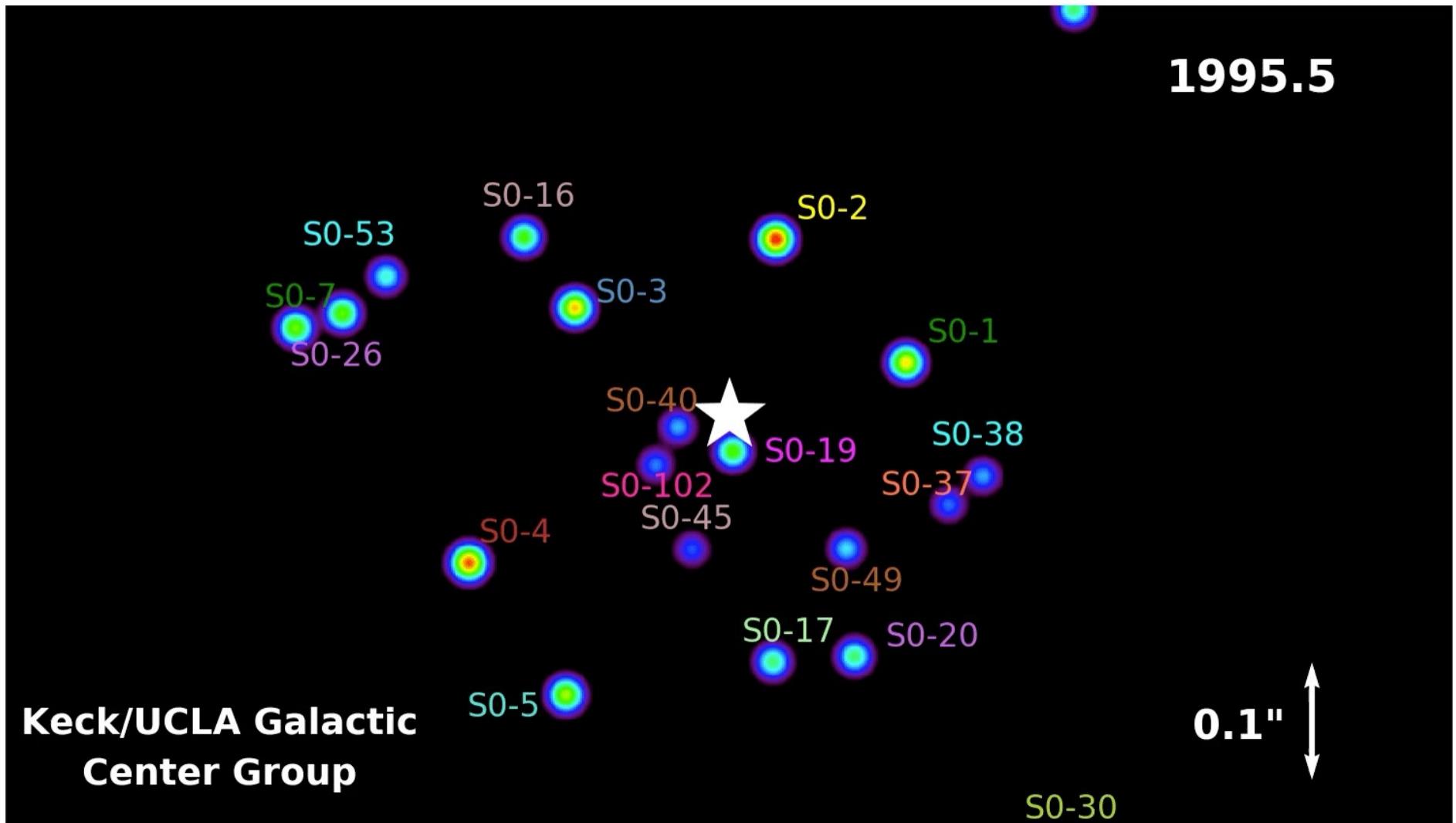


## Proper Motion of Sgr A\*

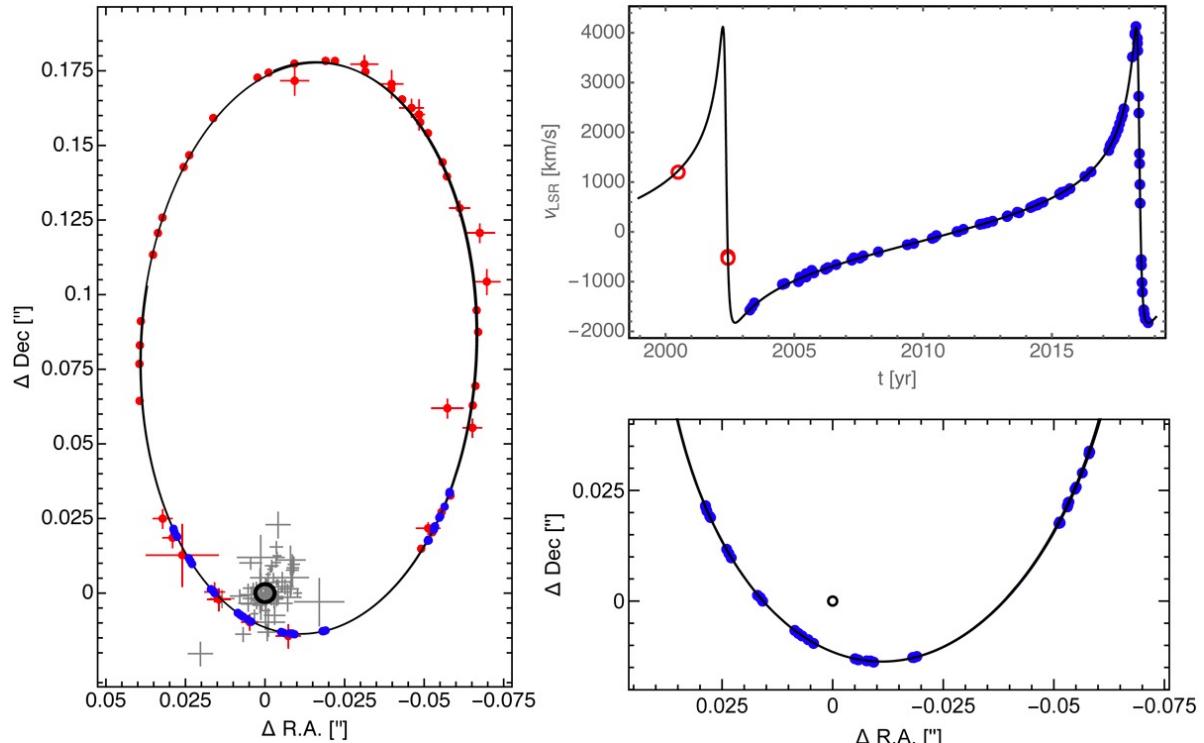
$$\mu_{SGRA*} = -6.379 \pm 0.026 \text{ mas/yr}$$

Reid & Brunthaler 2004, VLBI measurements of SgrB2

$$v_{tan} = 4.74 \frac{\mu}{\text{mas/yr}} \frac{R_o}{\text{kpc}} = V_{LSR} + v_\odot$$



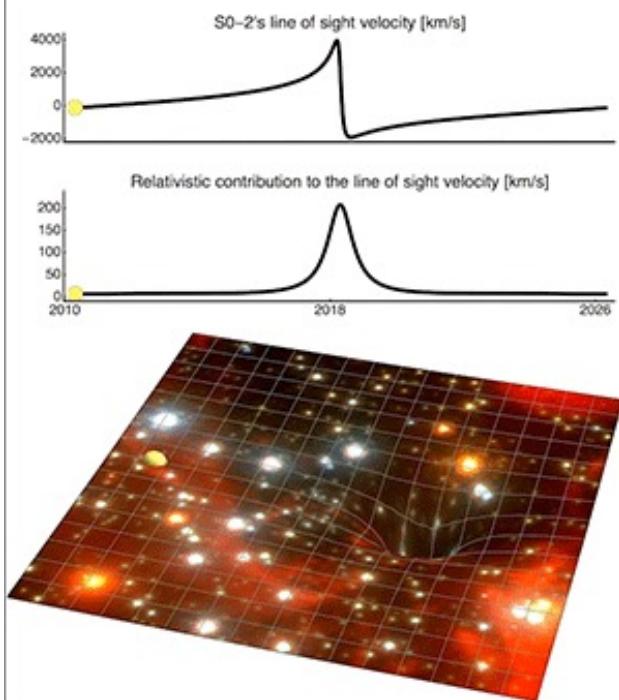
## Galactic Center Distance: Fitting the orbit of S2



Orbit of S2. *Left:* on-sky view of the astrometric data (red: AO data, blue: GRAVITY data) in the down-sampled version with the best-fit orbit (black ellipse). The black circle marks the position of Sgr A\*. The locations of previous AO-based flares agree with that position (gray crosses). *Right top:* radial velocity data of S2 together with the best-fit orbit. The blue data are from the VLT, the red are earlier epochs from the Keck data set ([Ghez et al. 2008](#)). *Right bottom:* zoom into the on-sky orbit in 2017 and 2018, showing the GRAVITY data that have error bars smaller than the symbol size.

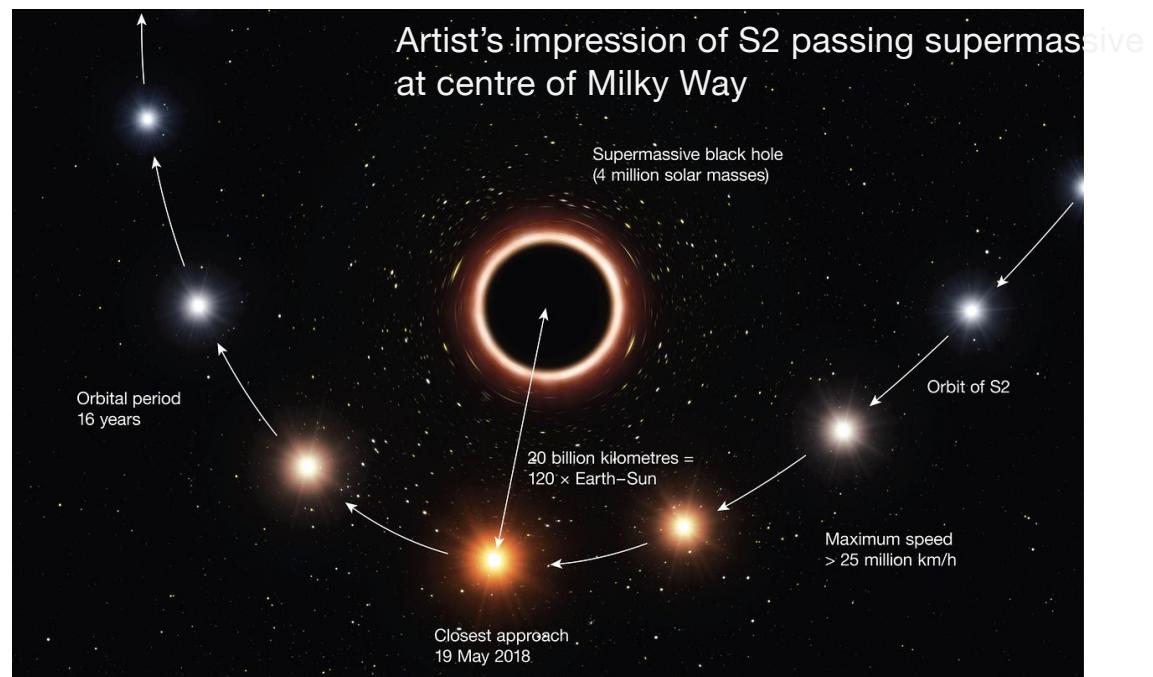
Abuter + 2019 GRAVITY Collaboration

$$R_0 = 8.178 \pm 0.013_{\text{stat}} \pm 0.022_{\text{sys}}$$



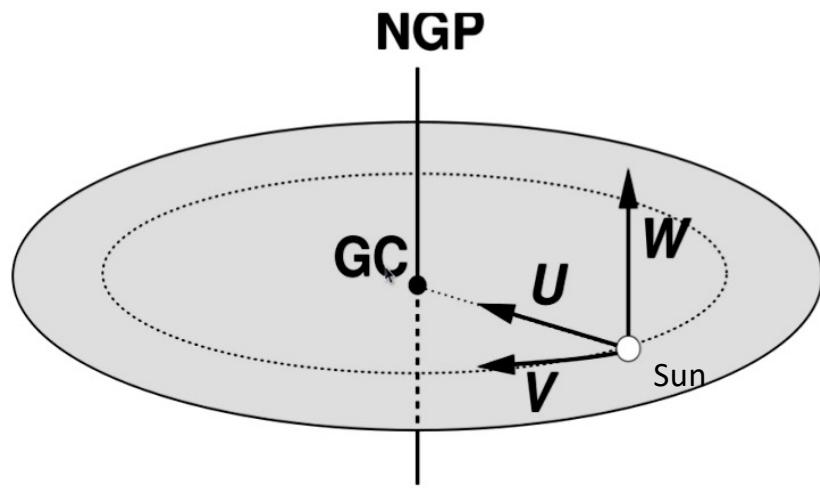
As the star S0-2 nears our galaxy's supermassive black hole (orbit exaggerated), the light it emits has to climb out of the gravitational potential well, losing energy. This process reddens the light. The star's motion along our line of sight also shifts the light's wavelengths, and so astronomers measure both shifts in km/s.

*Credit: Aurelien Hees / Keck UCLA Galactic Center Group*



# Peculiar motion of the Sun wrt LSR

See Carroll & Ostlie Chap 24

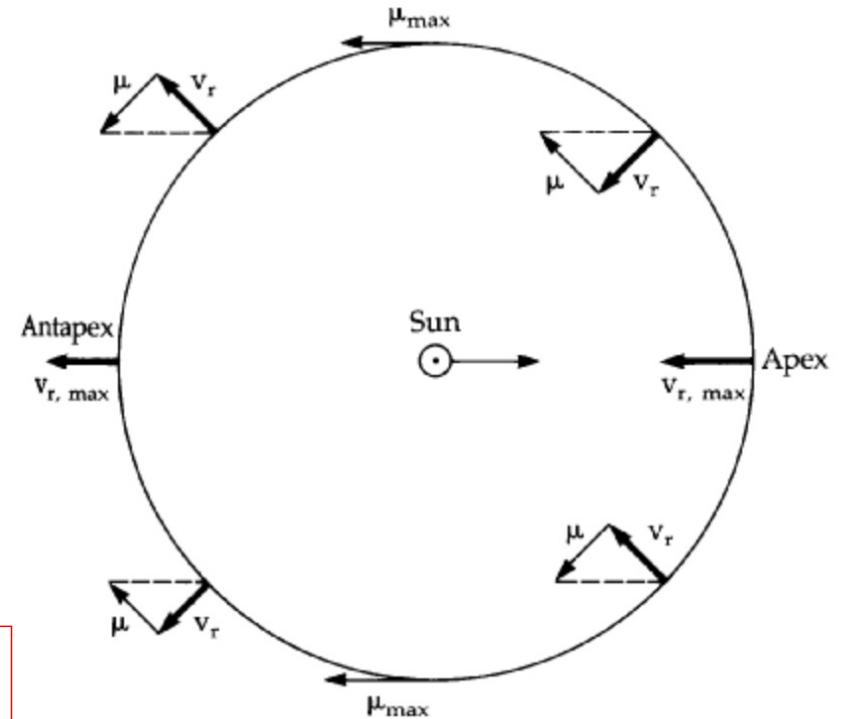


Solar Peculiar Motion: Schonrich+ 2010

$$(u, v, w)_\odot = 11.1 \pm 1.23, 12.24 \pm 2.05, 7.25 \pm 0.62$$

Units of km/s

Vpeculiar we care about is in the v direction



So going back to the proper motion of Sgr A\*

$$v_{tan} = 4.74 \frac{\mu}{\text{mas/yr}} \frac{R_o}{\text{kpc}} = V_{LSR} + v_\odot$$

V<sub>LSR</sub> = → LAB 1 !

Local Standard of Rest = The average velocity of stars near the sun.

$R_{\text{sun}} = 8.09 \text{ kpc}$   
 $S_0 : V_{\text{LSR}} = \sim 233 \text{ km/s}$

Most studies adopt:

$R_{\text{sun}} = 8.29 \pm 0.16 \text{ kpc}$   
 $V_{\text{LSR}} = 239 \pm 5 \text{ km/s}$   
McMillan+2011

## Milky Way Rotation Curve

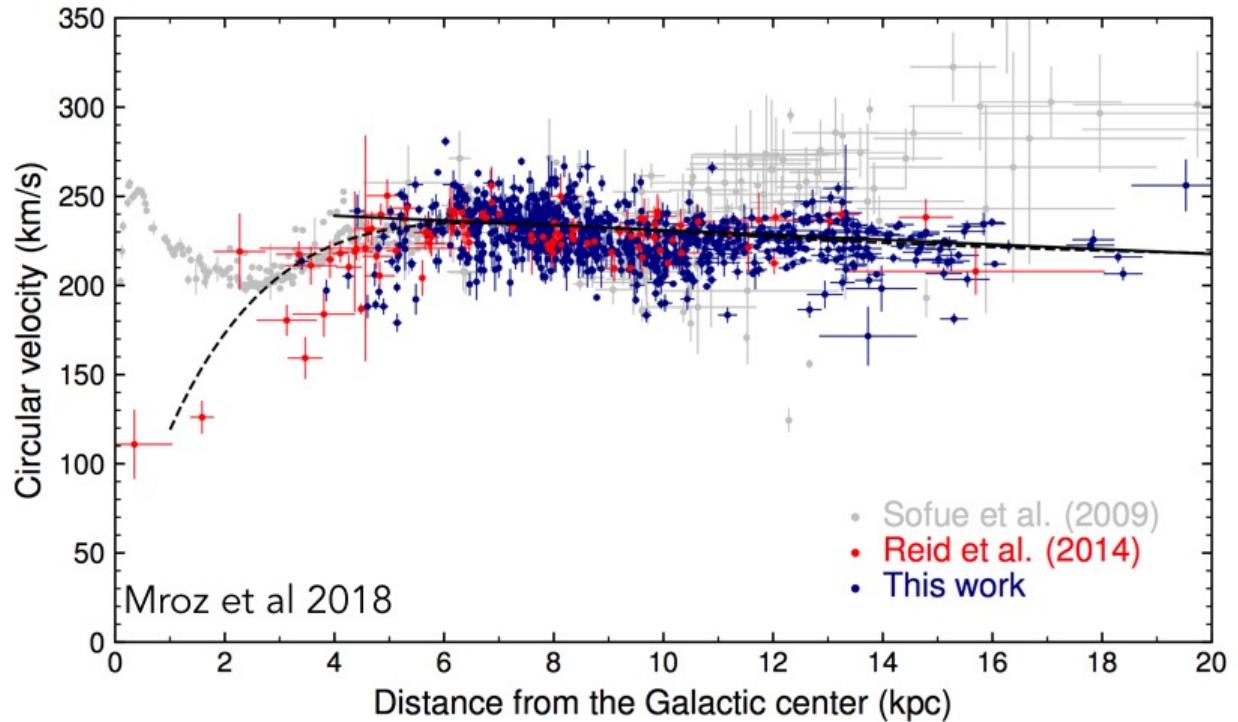
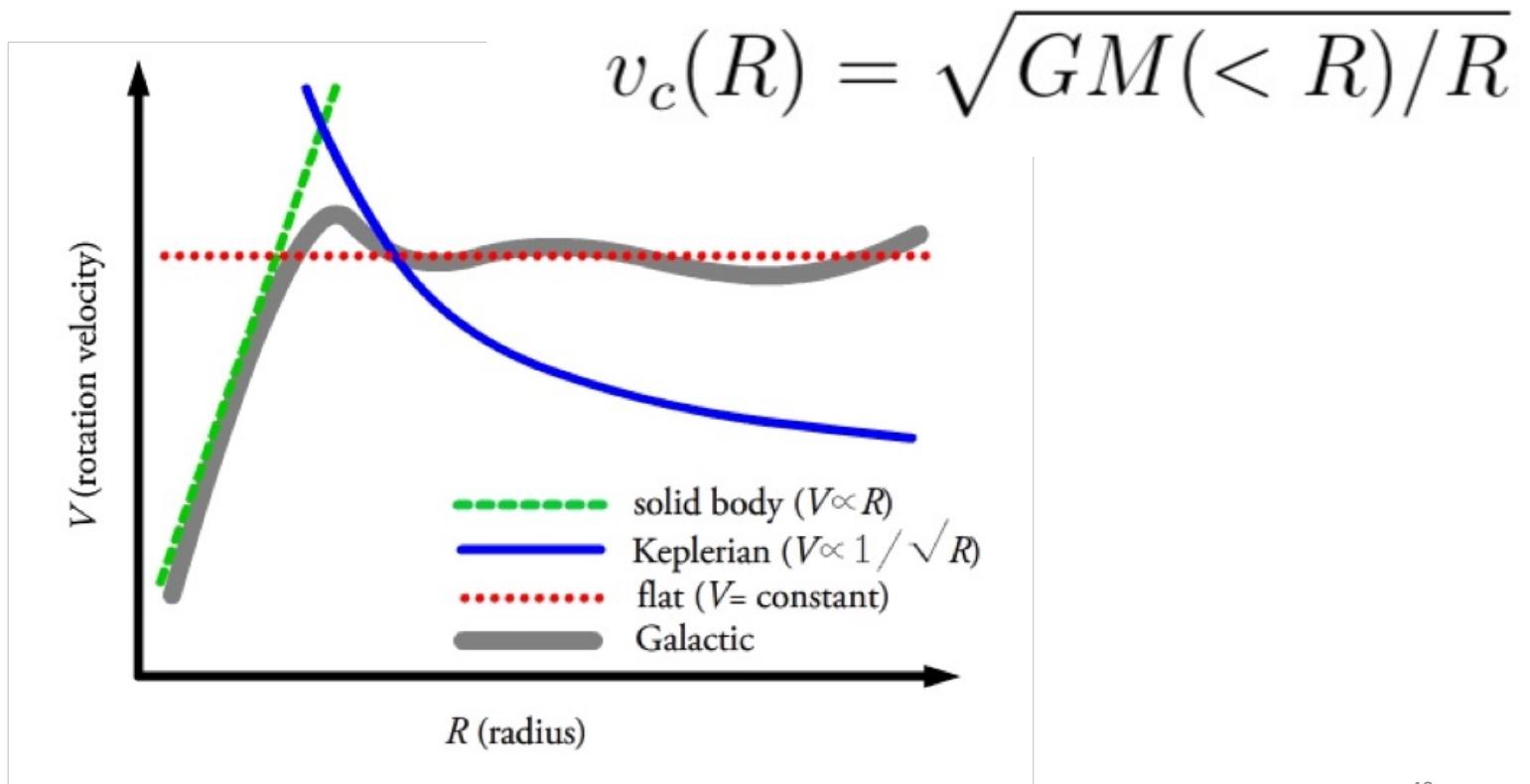


FIG. 2.— Rotation curve of the Milky Way for Cepheids assuming  $R_0 = 8.09 \text{ kpc}$  and  $\Theta_0 = 233.6 \text{ km s}^{-1}$  (model 2). Red data points represent high mass star forming regions (Reid et al. 2014). Grey data points are taken from Sofue et al. (2009) and were rescaled to new  $(R_0, \Theta_0)$  using formula  $V_{\text{new}} = V_{\text{old}} + \frac{R}{8.0} (\Theta_0 - 200)$ . Solid and dashed lines show the best-fitting models (linear and universal, respectively).

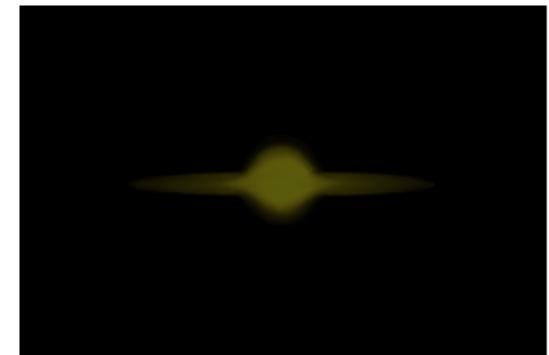
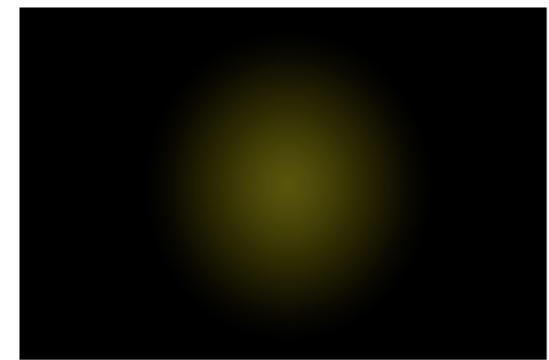
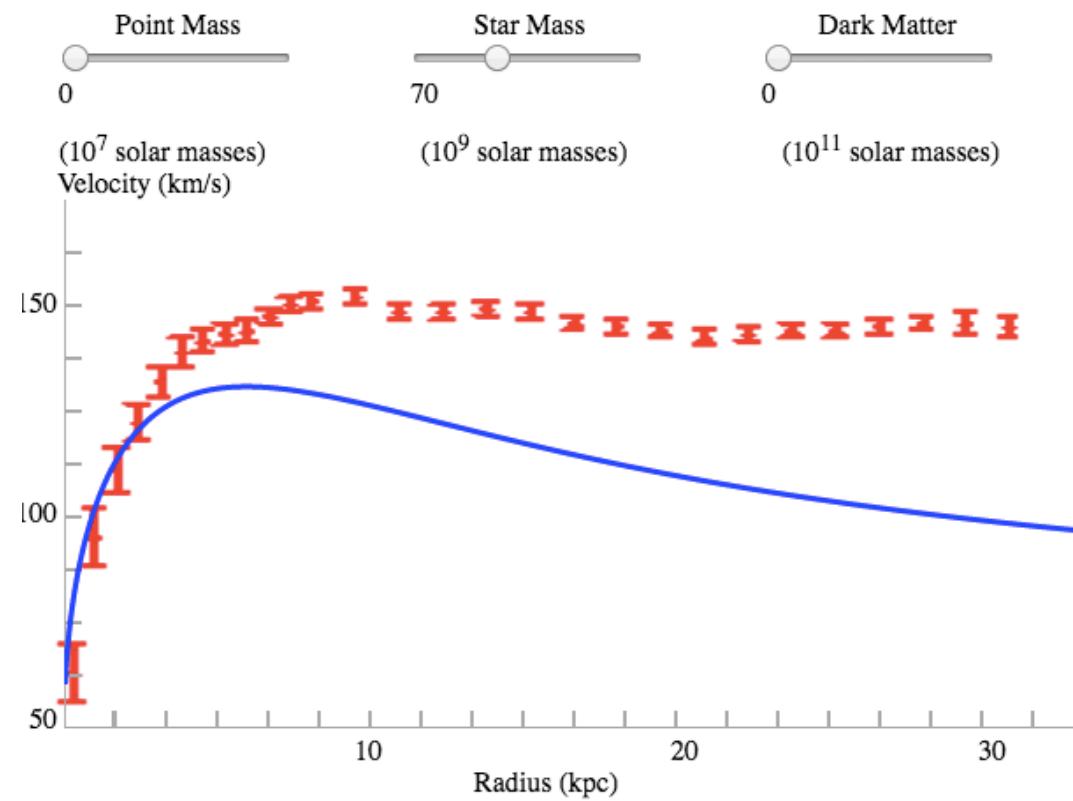
Recall ...

## Rotation curve and the dark matter



Try for yourself:

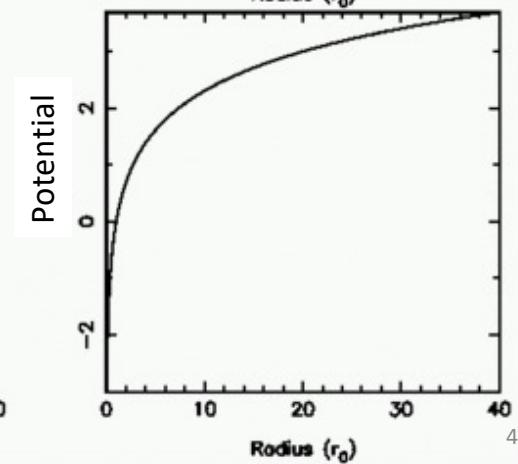
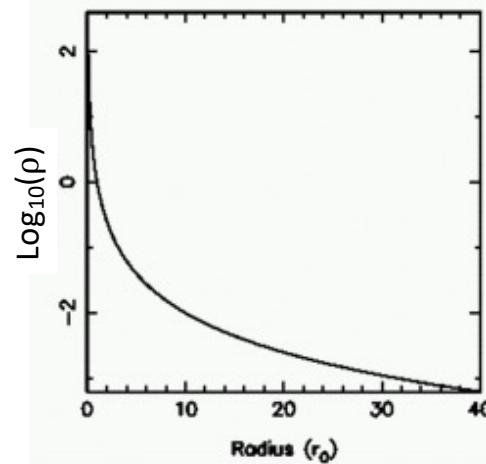
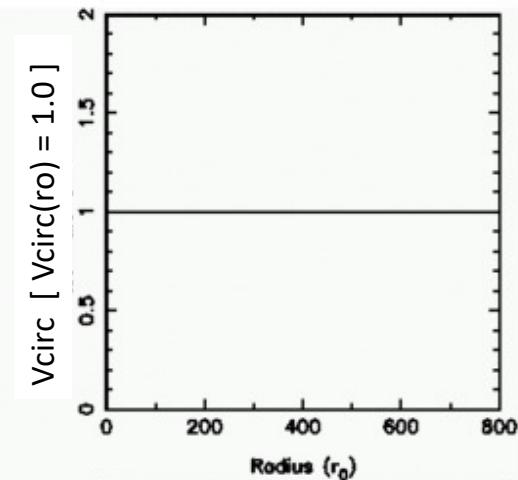
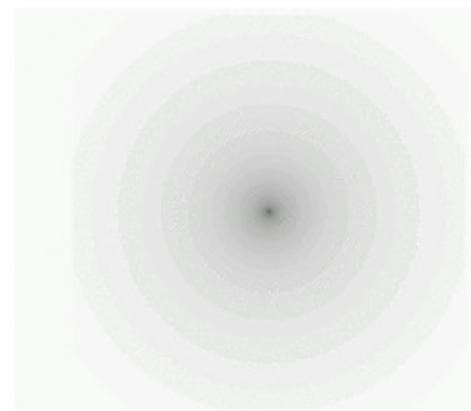
<http://wittman.physics.ucdavis.edu/Animations/RotationCurve/GalacticRotation.html>. (google wittman galactic rotation)



## Isothermal Sphere

$$\rho(r) = \frac{V_o^2}{4\pi G r^2}$$

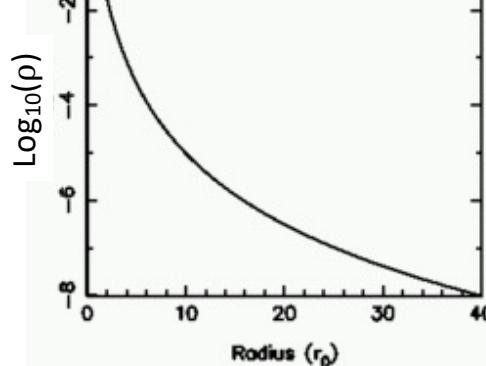
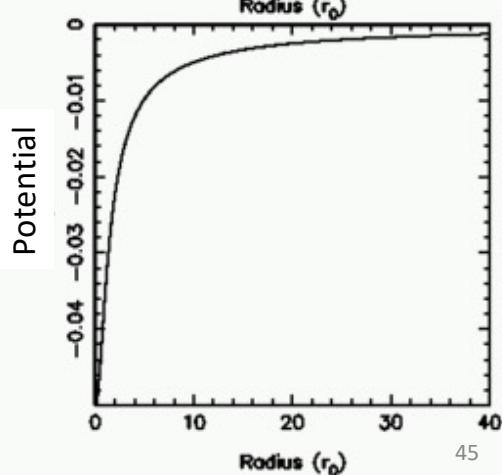
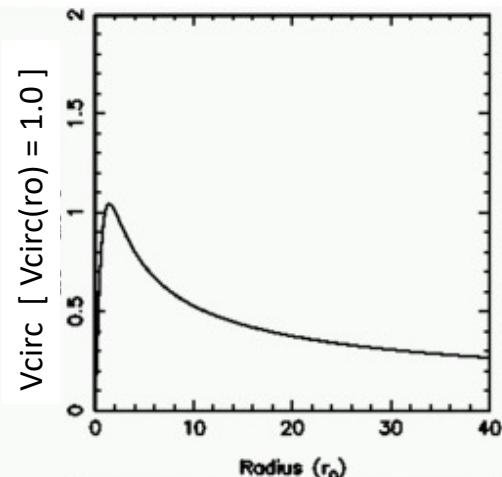
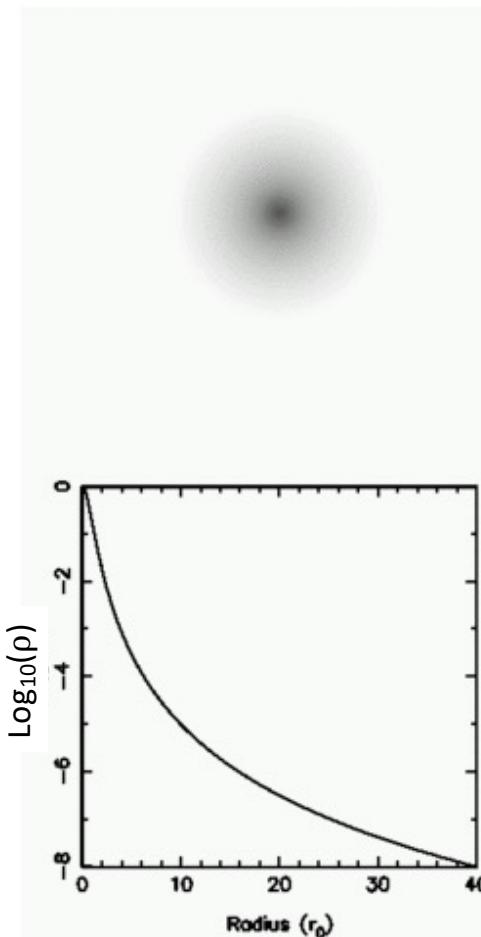
$$\Phi(r) = 4\pi G \rho_o \ln(r) = V_o^2 \ln(r)$$

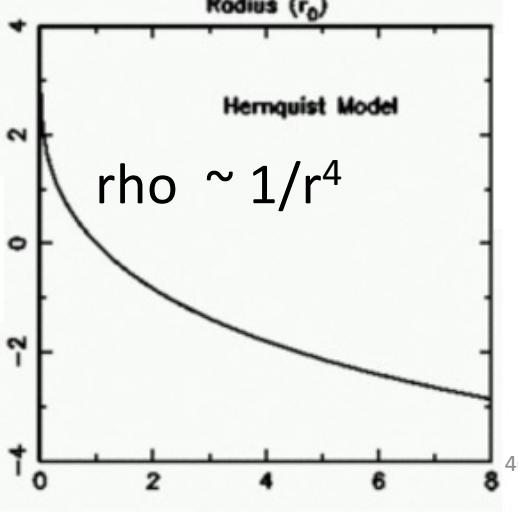
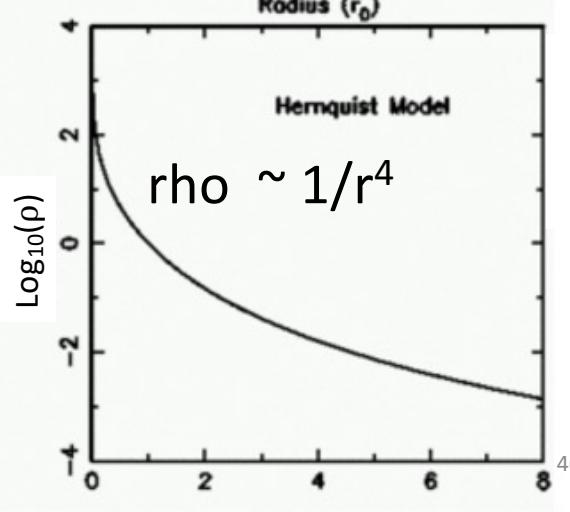
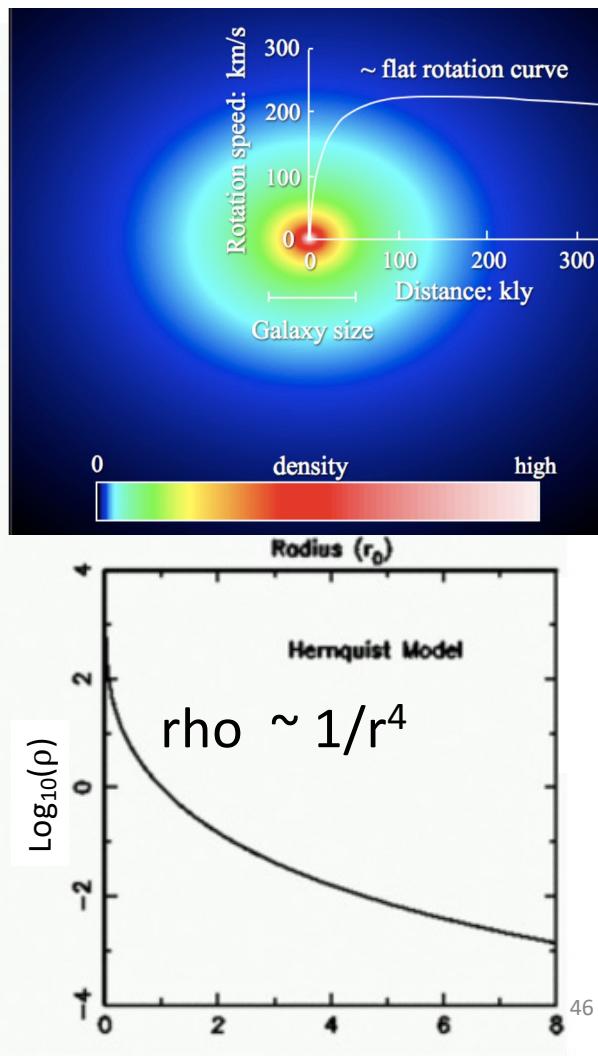
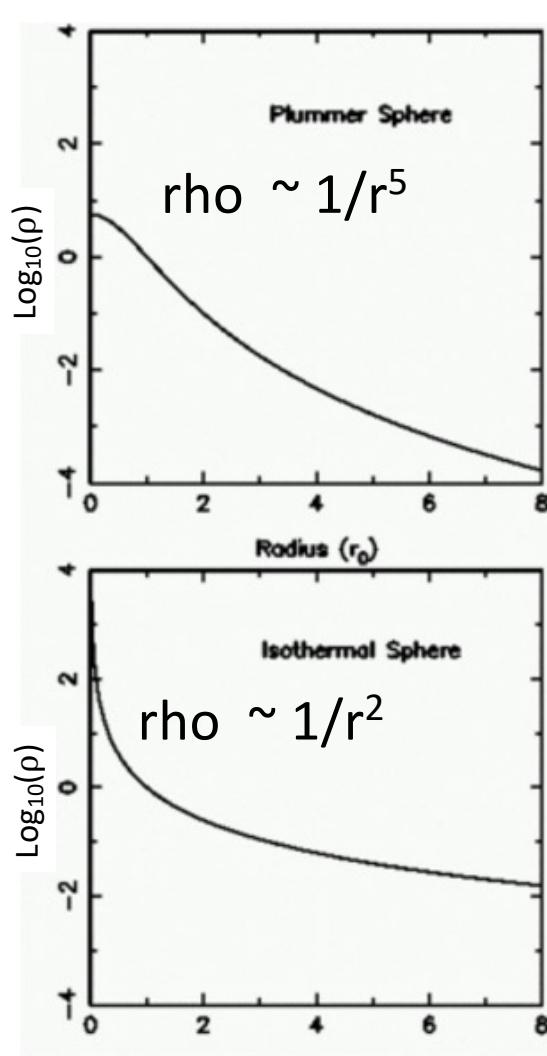


## Plummer model

$$\rho(r) = \frac{M}{4/3\pi a^3} (1.0 + r^2/a^2)^{-5/2}$$

$$\Phi(r) = -GM/\sqrt{r^2 + a^2}$$





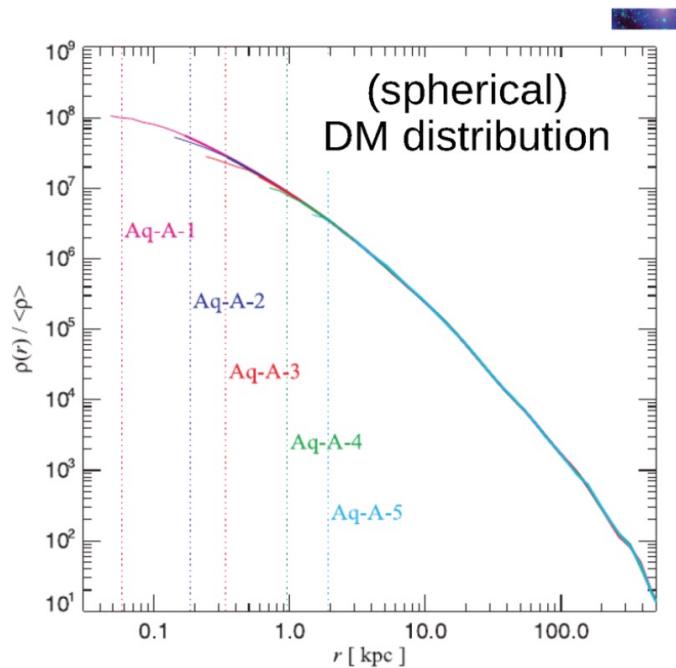
$$\rho \sim 1/r^3$$

NFW

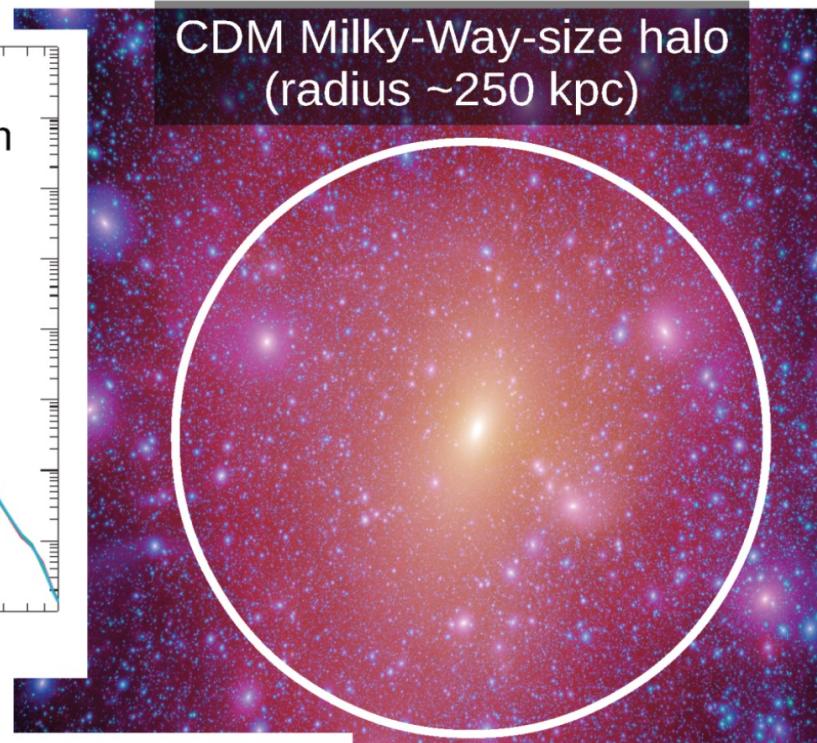
$$\rho(r) = \frac{\rho_o}{r/r_s(1+r/r_s)^2}$$

$$\Phi_{\text{NFW}}(r) = -\sigma_N^2 \frac{\ln(1+r/r_s)}{r/r_s}$$

$$\sigma_N = 4\pi G \rho_o r_s^2$$



CDM Milky-Way-size halo  
(radius  $\sim 250$  kpc)



# Some complications at larger radii...

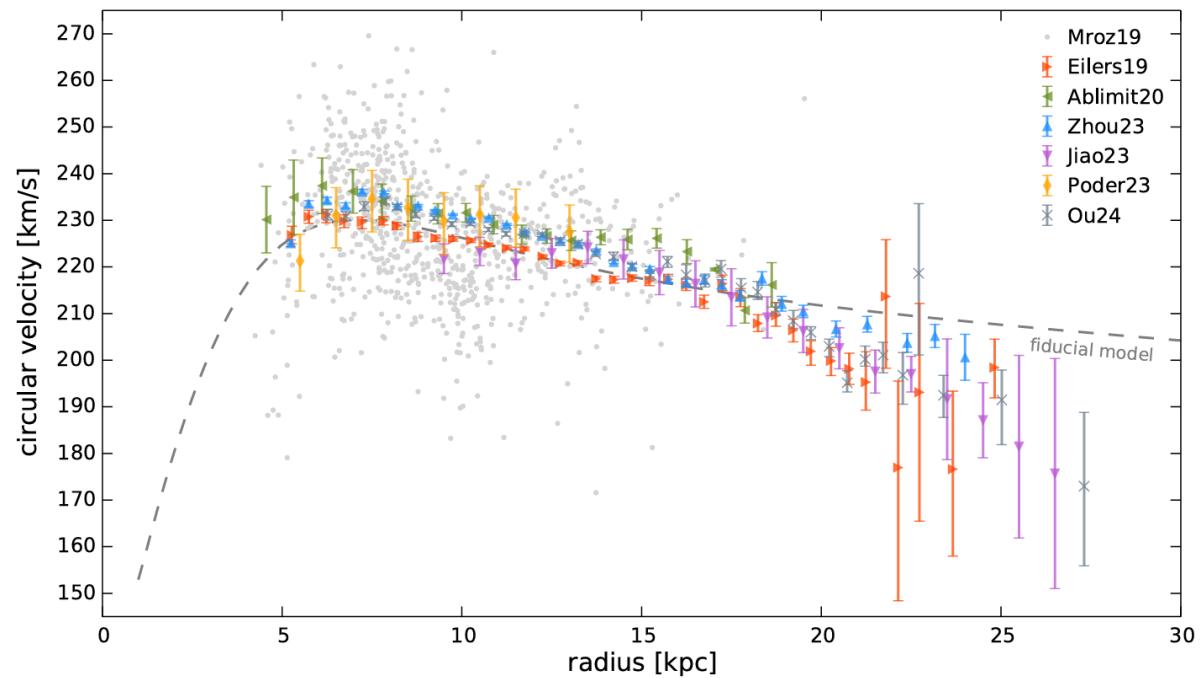


Figure 17: A compilation of measurements of the Milky Way circular-velocity curve in the radial range 5–30 kpc. The dashed line shows the same fiducial model as in the previous plot.

# Outer rotation curve is at odds with tracers at large radii

