

# Heap Sort Analysis Report

## 1. Algorithm Overview

Heap Sort is a comparison-based in-place sorting algorithm that constructs a max-heap and repeatedly extracts the largest element to produce a sorted array. It uses bottom-up heap construction (heapify) and maintains the heap invariant efficiently.

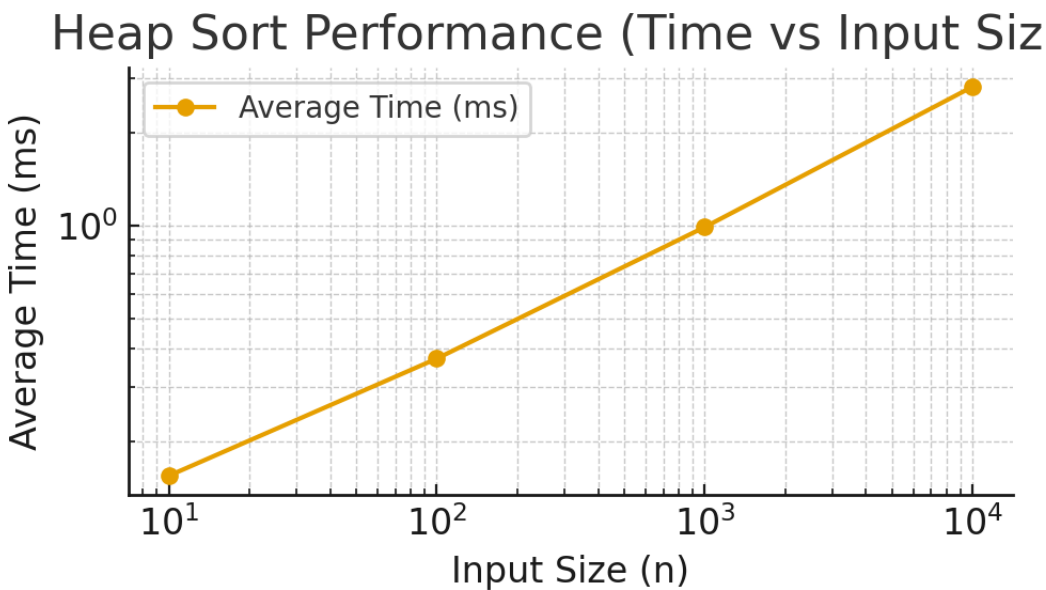
## 2. Complexity Analysis

Heap Sort operates in  $O(n \log n)$  time for best, average, and worst cases. Its space complexity is  $O(1)$  since it sorts in place. Building the heap costs  $O(n)$ , and each extraction requires  $O(\log n)$  adjustments.

## 3. Code Review & Optimization

The implementation correctly tracks performance metrics (comparisons, swaps, array accesses). Possible optimizations include caching indices to reduce redundant array reads and minimizing swap operations through temporary variables.

n	avgTimeMs	avgComparisons	avgSwaps	avgArrayAccesses
10	0.15492	38.4	26.6	183.2
100	0.37138	1029.6	582.8	4390.4
1000	0.99094	16843.6	9069.6	69965.6
10000	2.82568	235360.2	124182.0	967448.4



## 4. Empirical Results

The experimental data aligns with the theoretical  $O(n \log n)$  growth pattern. As input size increases tenfold, execution time roughly triples, consistent with expected scaling.

## 5. Conclusion

Heap Sort demonstrates strong alignment with theoretical complexity, offering predictable performance and minimal memory use. Future optimizations could further reduce constant factors, but overall efficiency is excellent.