LAC

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Algorand™



NIST Second PQC Standardization Conference

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• Nov 2017: LAC round 1 submission



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- Jun 2019: Pattern attack (CCA)
- Aug 2019: Hybrid dual attack

A brief review

- $(pk, sk) \leftarrow \texttt{KeyGen}()$
 - pk = (a, b := as + e), sk = s
- $c \leftarrow \text{Enc}(\text{msg}, \text{sk})$
 - $\tilde{\mathbf{m}} = \mathtt{BCH_encode}(\mathtt{msg})$
 - $c_1 = as_1 + e'$, $c_2 = bs_1 + e'' + q/2\tilde{m}$
 - $c = (\mathbf{c}_1, \mathbf{c}_2)$
- $msg \leftarrow Dec(c, pk)$
 - ...
 - $msg = BCH_decode(\tilde{\mathbf{m}})$

3/16

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- The focus of the cryptanalysis

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- A summary of the cryptanalysis on LAC;
- The updated parameter sets in Round 2;

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- A summary of the cryptanalysis on LAC;
- The updated parameter sets in Round 2;
- And more cryptanalysis...

Subfield Attack [Alp18a]

Strategy

- $x^n + 1 = \mathbf{hg} := (x^{n/2} + 91x^{n/4} + 250)(x^{n/2} + 160x^{n/4} + 250) \mod 251$
- Given (a, b = as + e), try to recover
 - $\bullet \ (\mathbf{s}_g,\mathbf{e}_g):=(\mathbf{s},\mathbf{e}) \ \mathsf{mod} \ \mathbf{g}$
 - $\bullet (\mathbf{s}_h, \mathbf{e}_h) := (\mathbf{s}, \mathbf{e}) \mod \mathbf{h}$

Analysis

- $|\mathbf{s}_g, \mathbf{e}_g|_{\infty} = 25$ too large, c.f. RHF
- No impact on LAC parameters for Round 1 submission

High Hamming Weight Attack [Alp18b]

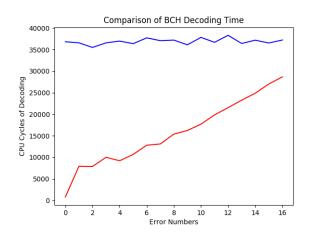
Strategy

- $\mathbf{s}_1, \mathbf{e}'$ follows binomial distribution
- ullet Choose $\mathbf{s}_1, \mathbf{e}'$ with higher-then-normal Hamming weight
- Decryption error rate increased to $2^{-44.4}$
- Produce 2^{19.6} decryption failures with 2²⁰⁷ pre-computation and 2⁶⁴ oracle queries for level 5.

Counter-measure

• Use binomial distribution with fixed Hamming weight.

Timing attack on ECC [DTVV19]



- Round 1 BCH: non-constant time, O(err)
- Round 2 BCH: almost constant time, O(max(err))

Error Correlation [DVV19]

Round 1 parameter

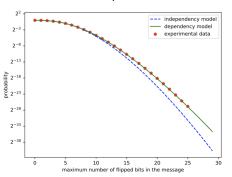
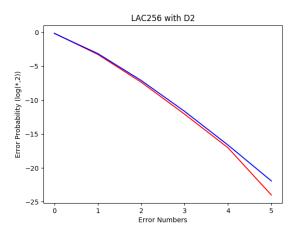


Figure 2: Probability of failure for various error correction capabilities of ecc_enc

• Dependency aware model: "independence assumption is suitable for schemes without error correction, but that it might lead to under-estimating the failure probability of algorithms using error correcting codes"

Error Correlation [DVV19], continued

Round 2 parameter



- Red line: Experimental data
- Blue line: Dependency aware model

Categories	n	q	dis	ecc	l_{m}	pk	sk	ct	bit-er	$\operatorname{dec-er}$
LAC-128	512	251	$\Psi_1^n, \Psi_1^{n,\frac{n}{2}}$	[511, 256, 33]	256	544	512	712	$2^{-12.61}$	2^{-116}
LAC-192			1 2 2						$2^{-22.27}$	
LAC-256	1024	251	$\Psi_1^n, \Psi_1^{n,\frac{n}{2}}$	[511,256,33]+D2	256	1056	1024	1424	$2^{-12.96}$	2^{-122}

dissecret and noise distributionseccerror correction code l_m message lengthsksecret key size (bytes)pkpublic key size (bytes)ctciphertext size (bytes)bit-ersingle bit error rate without BCHdec-erdecryption error rate

Table 2. Recommended parameter of LACv2

Major updates

	Round 1	Round 2		
Message space	256, 384, 512	256		
Noise dist.	binomial	fix-weight		
	BCH(511,264,29)	BCH(511,256,16)		
ECC	BCH(511,392,13)	BCH(511,256,8)		
	BCH(1023,520,55)	BCH(511,256,16)+D2		

Hybrid attacks, Round5 team and [Son19]

Hybrid primal attack

- Reduces security margin of LAC-192 from 286 to 278
- No impact on LAC-128/256

Hybrid dual attack

- Discovered by Round5 team and Son independently last week
- We are evaluating the impact
- Current thought: may affect security margin by a few bits

Pattern Attack [GJY19]

Strategy

- ullet Assume ${f e}'$ has certain pattern
 - e.g., 33 consecutive 1, -1, ...; happens with prob 2^{-122}
- s has certain distribution
 - e.g., $|\mathbf{s}_{odd}(1)| + |\mathbf{s}_{even}(1)| > 208$; happens with prob 2^{-70}
- A higher than normal error rate
 - e.g., $< 2^{-30}$, c.f., norm error rate 2^{-122}
- Repeat for enough errors to attack secret key
 - \bullet e.g., $\approx 2^{30}$ errors (?), with a total cost $2^{122+70+30+30} \approx 2^{252}$

Impact

- [GJY19] focused on LAC256 of round 1 parameter
- Our evaluation on round 2 parameter:
 - LAC128/192 remain intacct;
 - LAC256 needs a revision on error correct code.

Performance

Scheme	Size (in Bytes)			AV	Security		
Scheme	sk	pk	ct	gen	enc	dec	Security
NewHope512	1888	928	1120	68,080	109,836	114,176	101
Kyber512	1632	800	736	33,428	49,184	40,564	100
LAC-128	1056	544	712	59,584	89,055	140,221	133
Kyber768	2400	1184	1088	62,396	83,748	70,304	164
LAC-192	2080	1056	1188	119,246	137,653	320,135	259
NewHope1024	3680	1824	2208	129,670	210,092	220,864	233
Kyber1024	3168	1568	1568	88,568	115,952	99,764	230
LAC-256	2080	1056	1424	135,780	207,938	359,209	290

sk secret key

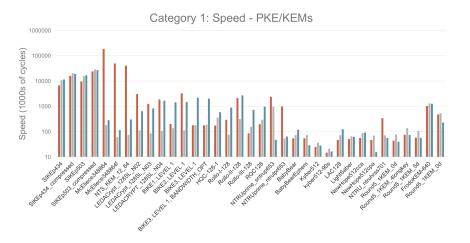
pk public keygen key generation

ct ciphertextenc encryption or encapsulation

dec decryption or decapsulation

Table 1. Comparison of NewHope, Kyber and LAC

Performance [Dus19]



A positive note

- LAC trials with a new direction to improve performance:
 - super small q + heavy error corrections;
 - c.f. different rings, lattice structures, etc.
- LAC has sparked a lot of new cryptanalysis technique.

Future work

- Improve error correction performance
- ullet Almost constant time o constant-time implementation
- Re-write ring multiplication with Assembly
- Improve m4 and FPGA implementation

Alperin-Sheriff.

Official comment: Lac.

NIST PQC Forum, 2018.

Alperin-Sheriff.

Official comment: Lac.

NIST PQC Forum, 2018.

Jan-Pieter D'Anvers, Marcel Tiepelt, Frederik Vercauteren, and Ingrid Verbauwhede.

Timing attacks on error correcting codes in post-quantum secure schemes.

IACR Cryptology ePrint Archive, 2019:292, 2019.

Dustin Moody.

Opening remarks.

The 2nd Round of the NIST PQC Standardization Process, 2019.

Jan-Pieter D'Anvers, Frederik Vercauteren, and Ingrid Verbauwhede.
The impact of error dependencies on ring/mod-lwe/lwr based schemes.

In Post-Quantum Cryptography - 10th International Conference, PQCrypto 2019, Chongqing, China, May 8-10, 2019 Revised Selected Papers, pages 103–115, 2019.



Qian Guo, Thomas Johansson, and Jing Yang. A novel cca attack using decryption errors against lac. *Asiacrypt*, 2019.



Yongha Son.

A note on parameter choices of round5.

Cryptology ePrint Archive, Report 2019/949, 2019. https://eprint.iacr.org/2019/949.