

# Recommender Systems and DGL

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AWS Shanghai AI Lab

July 12, 2019

# Why Recommendation

## Why Recommendation

**We don't want our customers to think (hard).**

# Why Recommendation

Good relevant recommendations make the customers adhere to us.

**Added to Cart**  
Only 1 left in stock.

**Cart subtotal (1 item): \$523.01**  
Your order qualifies for **FREE Shipping!** Select this option at checkout. [Details](#)


Cart


Proceed to checkout (1 item)

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★★★★☆ 1


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Dell OptiPlex 9020 Small Form Factor Desktop, Intel Core i5-8500 3 GHz Hexa-Core, 8GB RAM,...

★★★★☆ 5


\$674.00



Dell OptiPlex 9020 Small Form Factor Desktop, Intel Core i7 4770, 16GB Ram,...

★★★★☆ 59


\$345.00



Dell CFC5C OptiPlex 3050 Micro Form Factor Desktop Computer, Intel Core i5-7500T, 8GB DDR4,...

★★★★☆ 38


13 offers from \$479.00



Acer Aspire TC-885-ACCFLU50 Desktop, 8th Gen Intel Core i5-8400, 8GB DDR4 + 16GB,...


★★★★☆ 59


\$499.99



Inspired by your browsing history

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★★★★☆ 34


\$129.99



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★★★★☆ 47


\$219.99



Silicon Power 256GB SSD 3D NAND A55 SLC Cache Performance Boost SATA III 2.5" 7mm (0.28")...

★★★★☆ 950


\$28.99



Ubiquiti Networks Unifi 802.11ac Dual-Radio PRO Access Point (UAP-AC-PRO-US)

★★★★☆ 1,385


\$134.26



AmazonBasics Wired Computer Keyboard and Mouse, 10-Pack

★★★★☆ 1,977

\$122.30



# Why Recommendation

Good relevant recommendations make the customers adhere to us.



# Recommender System: Problem Statement



Image source: Wikipedia

# Collaborative Filtering



# Collaborative Filtering





# Collaborative Filtering











Image source: Wikipedia

## Collaborative Filtering: Classical Methods

- **User-based:** Infer how a user  $i$  would act to an item  $j$  by looking at how users that have similar interactions to user  $i$  acted to item  $j$ .

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  - We have millions of customers.














# Collaborative Filtering: Classical Methods

- **User-based:** Infer how a user  $i$  would act to an item  $j$  by looking at how users that have similar interactions to user  $i$  acted to item  $j$ .
  - We have millions of customers.
  - User profiles change constantly and quickly, requiring frequent rebuilds (which are expensive already).












# Collaborative Filtering: Classical Methods

- **Item-based:** Infer how a user  $i$  would act to an item  $j$  by looking at how **items** that have similar interactions to **item  $j$**  were being acted by **user  $i$** .
  - Amazon used to have fewer items than users.


























				
				
				
				
				
				

# Collaborative Filtering: Classical Methods

- **Item-based:** Infer how a user  $i$  would act to an item  $j$  by looking at how items that have similar interactions to item  $j$  were being acted by user  $i$ .
  - Amazon used to have fewer items than users.
  - Now we also have millions of items.

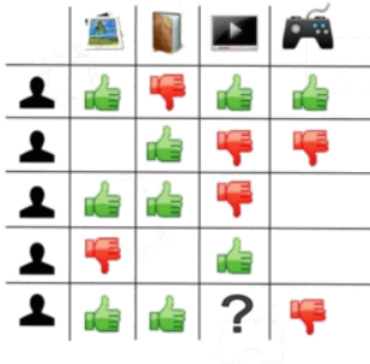
				
				
				
				
				
				

# Machine Learning Kicks In

We were "representing" users and items with the items/users that had interactions with them.

# Machine Learning Kicks In



	Feature 1	Feature 2
User 1	?	?
User 2	?	?
User 3	?	?
User 4	?	?
User 5	?	?

X

	Item 1	Item 2	Item 3	Item 4	Item 5
Feature 1	?	?	?	?	?
Feature 2	?	?	?	?	?

=

	Item 1	Item 2	Item 3	Item 4	Item 5
User 1	0?	3	0?	3	0?
User 2	4	0?	0?	2	0?
User 3	0?	0?	3	0?	0?
User 4	3	0?	4	0?	3
User 5	4	3	0?	4	0?

We were "representing" users and items with the items/users that had interactions with them.

Source: [Kat Bailey](#)

Can we represent users and items as a set of features?



# Latent Factor Model

- An item can be described with a set of features (e.g. how sweet some food is).

	Feature 1	Feature 2
User 1	?	?
User 2	?	?
User 3	?	?
User 4	?	?
User 5	?	?

X

	Item 1	Item 2	Item 3	Item 4	Item 5
Feature 1	?	?	?	?	?
Feature 2	?	?	?	?	?

	Item 1	Item 2	Item 3	Item 4	Item 5
User 1	0.?	3	0.?	3	0.?
User 2	4	0.?	0.?	2	0.?
User 3	0.?	0.?	3	0.?	0.?
User 4	3	0.?	4	0.?	3
User 5	4	3	0.?	4	0.?

Source: [Kat Bailey](#)

# Latent Factor Model

- An item can be described with a set of features (e.g. how sweet some food is).
- A user can be described with preferences of the same set of features (e.g. how much a user likes sweet food).

	Feature 1	Feature 2
User 1	?	?
User 2	?	?
User 3	?	?
User 4	?	?
User 5	?	?

X

	Item 1	Item 2	Item 3	Item 4	Item 5
Feature 1	?	?	?	?	?
Feature 2	?	?	?	?	?

	Item 1	Item 2	Item 3	Item 4	Item 5
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User 3	0.?	0.?	3	0.?	0.?
User 4	3	0.?	4	0.?	3
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Source: [Kat Bailey](#)

# Latent Factor Model

- An item can be described with a set of features (e.g. how sweet some food is).
- A user can be described with preferences of the same set of features (e.g. how much a user likes sweet food).
- The interaction is defined by how well the item features match the user preferences.

	Feature 1	Feature 2
User 1	?	?
User 2	?	?
User 3	?	?
User 4	?	?
User 5	?	?

X

	Item 1	Item 2	Item 3	Item 4	Item 5
Feature 1	?	?	?	?	?
Feature 2	?	?	?	?	?

	Item 1	Item 2	Item 3	Item 4	Item 5
User 1	0?	3	0?	3	0?
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User 3	0?	0?	3	0?	0?
User 4	3	0?	4	0?	3
User 5	4	3	0?	4	0?

Source: [Kat Bailey](#)

# Matrix Factorization (Explicit Feedback)

- An item can be described with a **vector  $v_j$** .
- A user can be described with preferences of the same set of features (e.g. how much a user likes sweet food).
- The interaction is defined by how well the item features match the user preferences.

	Feature 1	Feature 2
User 1	?	?
User 2	?	?
User 3	?	?
User 4	?	?
User 5	?	?

X

	Item 1	Item 2	Item 3	Item 4	Item 5
Feature 1	?	?	?	?	?
Feature 2	?	?	?	?	?

	Item 1	Item 2	Item 3	Item 4	Item 5
User 1	0?	3	0?	3	0?
User 2	4	0?	0?	2	0?
User 3	0?	0?	3	0?	0?
User 4	3	0?	4	0?	3
User 5	4	3	0?	4	0?

Source: [Kat Bailey](#)

# Matrix Factorization (Explicit Feedback)

- An item can be described with a vector  $v_j$ .
- A user can be described with **another vector  $u_i$**
- The interaction is defined by how well the item features match the user preferences.

	Feature 1	Feature 2
User 1	?	?
User 2	?	?
User 3	?	?
User 4	?	?
User 5	?	?

X

	Item 1	Item 2	Item 3	Item 4	Item 5
Feature 1	?	?	?	?	?
Feature 2	?	?	?	?	?

	Item 1	Item 2	Item 3	Item 4	Item 5
User 1	0?	3	0?	3	0?
User 2	4	0?	0?	2	0?
User 3	0?	0?	3	0?	0?
User 4	3	0?	4	0?	3
User 5	4	3	0?	4	0?

Source: [Kat Bailey](#)

# Matrix Factorization (Explicit Feedback)

- An item can be described with a vector  $v_j$ .
- A user can be described with another vector  $u_i$
- The **rating on item  $j$  by user  $i$**  is defined by  $u_i^\top v_j$ .

	Feature 1	Feature 2
User 1	?	?
User 2	?	?
User 3	?	?
User 4	?	?
User 5	?	?

X

	Item 1	Item 2	Item 3	Item 4	Item 5
Feature 1	?	?	?	?	?
Feature 2	?	?	?	?	?

	Item 1	Item 2	Item 3	Item 4	Item 5
User 1	0.?	3	0.?	3	0.?
User 2	4	0.?	0.?	2	0.?
User 3	0.?	0.?	3	0.?	0.?
User 4	3	0.?	4	0.?	3
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Source: [Kat Bailey](#)

# Matrix Factorization (Explicit Feedback)

- An item can be described with a vector  $v_j$ .
- A user can be described with another vector  $u_i$
- The rating on item  $j$  by user  $i$ . is defined by  $u_i^\top v_j$ .
- We minimize

$$\sum_{i,j} \left( r_{i,j} - \left( u_i^\top v_j \right) \right)^2$$

	Feature 1	Feature 2
User 1	?	?
User 2	?	?
User 3	?	?
User 4	?	?
User 5	?	?

X

	Item 1	Item 2	Item 3	Item 4	Item 5
Feature 1	?	?	?	?	?
Feature 2	?	?	?	?	?

	Item 1	Item 2	Item 3	Item 4	Item 5
User 1	0?	3	0?	3	0?
User 2	4	0?	0?	2	0?
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Source: [Kat Bailey](#)

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- An item can be described with a vector  $v_j$ .
- A user can be described with another vector  $u_i$
- The rating on item  $j$  by user  $i$ . is defined by  $u_i^\top v_j$ .
- We minimize

$$\sum_{i,j} \left( r_{i,j} - \left( u_i^\top v_j + b_{u_i} + b_{v_j} \right) \right)^2$$

	Feature 1	Feature 2
User 1	?	?
User 2	?	?
User 3	?	?
User 4	?	?
User 5	?	?

X

	Item 1	Item 2	Item 3	Item 4	Item 5
Feature 1	?	?	?	?	?
Feature 2	?	?	?	?	?

	Item 1	Item 2	Item 3	Item 4	Item 5
User 1	0?	3	0?	3	0?
User 2	4	0?	0?	2	0?
User 3	0?	0?	3	0?	0?
User 4	3	0?	4	0?	3
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Source: [Kat Bailey](#)



# Matrix Factorization (Explicit Feedback)

- We minimize

$$\sum_{i,j} \left( r_{i,j} - \left( u_i^\top v_j + b_{u_i} + b_{u_j} \right) \right)^2$$

- What if the vectors are of **very** high dimensions?

	Feature 1	Feature 2
User 1	?	?
User 2	?	?
User 3	?	?
User 4	?	?
User 5	?	?

X

	Item 1	Item 2	Item 3	Item 4	Item 5
Feature 1	?	?	?	?	?
Feature 2	?	?	?	?	?

	Item 1	Item 2	Item 3	Item 4	Item 5
User 1	0?	3	0?	3	0?
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Source: [Kat Bailey](#)

# Matrix Factorization (Explicit Feedback)

- We minimize

$$\sum_{i,j} \left( r_{i,j} - \left( u_i^\top v_j + b_{u_i} + b_{u_j} \right) \right)^2$$

- What if the vectors are of **very** high dimensions?
  - Use low-dimensional  $u_i$  and  $v_j$ .

	Feature 1	Feature 2
User 1	?	?
User 2	?	?
User 3	?	?
User 4	?	?
User 5	?	?

X

	Item 1	Item 2	Item 3	Item 4	Item 5
Feature 1	?	?	?	?	?
Feature 2	?	?	?	?	?

	Item 1	Item 2	Item 3	Item 4	Item 5
User 1	0?	3	0?	3	0?
User 2	4	0?	0?	2	0?
User 3	0?	0?	3	0?	0?
User 4	3	0?	4	0?	3
User 5	4	3	0?	4	0?

Source: [Kat Bailey](#)

# Matrix Factorization (Explicit Feedback)

- We minimize

$$\sum_{i,j} \left( r_{i,j} - \left( u_i^\top v_j + b_{u_i} + b_{u_j} \right) \right)^2$$

- What if the vectors are of **very** high dimensions?
  - Use low-dimensional  $u_i$  and  $v_j$ .
- What if one product receives only one but very high rating?

	Feature 1	Feature 2
User 1	?	?
User 2	?	?
User 3	?	?
User 4	?	?
User 5	?	?

X

	Item 1	Item 2	Item 3	Item 4	Item 5
Feature 1	?	?	?	?	?
Feature 2	?	?	?	?	?

	Item 1	Item 2	Item 3	Item 4	Item 5
User 1	0?	3	0?	3	0?
User 2	4	0?	0?	2	0?
User 3	0?	0?	3	0?	0?
User 4	3	0?	4	0?	3
User 5	4	3	0?	4	0?

Source: [Kat Bailey](#)

# Matrix Factorization (Explicit Feedback)

- We minimize

$$\sum_{i,j} \left( r_{i,j} - \left( u_i^\top v_j + b_{u_i} + b_{u_j} \right) \right)^2 + \alpha \left( \|U\|_F^2 + \|V\|_F^2 \right)$$

- What if the vectors are of **very** high dimensions?
  - Use low-dimensional  $u_i$  and  $v_j$ .
- What if one product receives only one but very high rating?
  - Penalize the magnitude of parameters.

	Feature 1	Feature 2
User 1	?	?
User 2	?	?
User 3	?	?
User 4	?	?
User 5	?	?

X

	Item 1	Item 2	Item 3	Item 4	Item 5
Feature 1	?	?	?	?	?
Feature 2	?	?	?	?	?

	Item 1	Item 2	Item 3	Item 4	Item 5
User 1	0.?	3	0.?	3	0.?
User 2	4	0.?	0.?	2	0.?
User 3	0.?	0.?	3	0.?	0.?
User 4	3	0.?	4	0.?	3
User 5	4	3	0.?	4	0.?

Source: [Kat Bailey](#)

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- We minimize

$$\sum_{i,j} \left( r_{i,j} - \left( u_i^\top v_j + b_{u_i} + b_{u_j} \right) \right)^2 + \alpha \left( \|U\|_F^2 + \|V\|_F^2 \right)$$

	Feature 1	Feature 2
User 1	?	?
User 2	?	?
User 3	?	?
User 4	?	?
User 5	?	?

X

	Item 1	Item 2	Item 3	Item 4	Item 5
Feature 1	?	?	?	?	?
Feature 2	?	?	?	?	?

	Item 1	Item 2	Item 3	Item 4	Item 5
User 1	0?	3	0?	3	0?
User 2	4	0?	0?	2	0?
User 3	0?	0?	3	0?	0?
User 4	3	0?	4	0?	3
User 5	4	3	0?	4	0?

Source: [Kat Bailey](#)

# Matrix Factorization (Explicit Feedback)

- We minimize

$$\sum_{(i,j) \in \mathcal{B}} \left( r_{i,j} - \left( u_i^\top v_j + b_{u_i} + b_{u_j} \right) \right)^2 + \alpha \left( \|U\|_F^2 + \|V\|_F^2 \right)$$

- Optimize with Stochastic Gradient Descent
  - Each time we sample a minibatch of interactions, and compute the gradient from this minibatch only.

	Feature 1	Feature 2
User 1	?	?
User 2	?	?
User 3	?	?
User 4	?	?
User 5	?	?

X

	Item 1	Item 2	Item 3	Item 4	Item 5
Feature 1	?	?	?	?	?
Feature 2	?	?	?	?	?

	Item 1	Item 2	Item 3	Item 4	Item 5
User 1	0?	3	0?	3	0?
User 2	4	0?	0?	2	0?
User 3	0?	0?	3	0?	0?
User 4	3	0?	4	0?	3
User 5	4	3	0?	4	0?

=

Source: [Kat Bailey](#)

## What if we don't have ratings?



	Item 1	Item 2	Item 3	Item 4	Item 5
User 1		3	0		0
User 2	4			2	0
User 3	0			0	0
User 4		0	4		3
User 5	4	3	0	4	0

	$i_1$	$i_2$	$i_3$	$i_4$	
$u_1$	?	+	+	?	user ↑ ↓
$u_2$	+	?	?	+	
$u_3$	+	+	?	?	
$u_4$	?	?	+	+	
$u_5$	?	?	+	?	
	← item →				

Source: BPR: Bayesian Personalized Ranking from

*Implicit Feedback*, Rendle et al. 2012

# Matrix Factorization (Implicit Feedback)

- For a given user  $i$ , an item being interacted  $j$  should have a higher score than another item  $k$  which was never being interacted.

	$i_1$	$i_2$	$i_3$	$i_4$	
$u_1$	?	+	+	?	user ↑ ↓
$u_2$	+	?	?	+	
$u_3$	+	+	?	?	
$u_4$	?	?	+	+	
$u_5$	?	?	+	?	
	← item →				

Source: *BPR: Bayesian Personalized Ranking*  
from *Implicit Feedback*, Rendle et al. 2012



# Matrix Factorization (Implicit Feedback)

- For a given user  $i$ , an item being interacted  $j$  should have a higher score than another item  $k$  which was never being interacted.
- We maximize

$$\sum_{i,j,k \in I \setminus I_{u_i}} \log \frac{1}{1 + \exp(u_i^\top v_k - u_i^\top v_j)}$$

	$i_1$	$i_2$	$i_3$	$i_4$	
$u_1$	?	+	+	?	user ↑ ↓
$u_2$	+	?	?	+	
$u_3$	+	+	?	?	
$u_4$	?	?	+	+	
$u_5$	?	?	+	?	
	← item →				

Source: *BPR: Bayesian Personalized Ranking*  
from *Implicit Feedback*, Rendle et al. 2012

# Matrix Factorization (Implicit Feedback)

- For a given user  $i$ , an item being interacted  $j$  should have a higher score than another item  $k$  which was never being interacted.
- We maximize

$$\sum_{i,j,k \in I \setminus I_{u_i}} \log \frac{1}{1 + \exp(u_i^\top v_k - u_i^\top v_j)}$$

- We usually *sample* one or multiple  $k$  when computing gradients (**negative sampling**).
  - Commonly uniformly, but adaptive sampling often helps.

	$i_1$	$i_2$	$i_3$	$i_4$	
$u_1$	?	+	+	?	user ↑ ↓
$u_2$	+	?	?	+	
$u_3$	+	+	?	?	
$u_4$	?	?	+	+	
$u_5$	?	?	+	?	
	← item →				

Source: *BPR: Bayesian Personalized Ranking from Implicit Feedback*, Rendle et al. 2012

## Other Meaningful Aspects to Consider

- **Cold-start:** What if we have *new* users and items coming in, with few to no historical interactions?

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- **Cold-start:** What if we have *new* users and items coming in, with few to no historical interactions?
- **Bias correction:** The training dataset usually comes from the result of a *previous recommender system*. How to mitigate the bias?

## Other Meaningful Aspects to Consider

- **Cold-start:** What if we have *new* users and items coming in, with few to no historical interactions?
- **Bias correction:** The training dataset usually comes from the result of a *previous recommender system*. How to mitigate the bias?
- **Diversity:** Always recommending the same items (or even the same kind of item) to a user would make him/her feel *bored*.

## Other Meaningful Aspects to Consider

- **Cold-start:** What if we have *new* users and items coming in, with few to no historical interactions?
- **Bias correction:** The training dataset usually comes from the result of a *previous recommender system*. How to mitigate the bias?
- **Diversity:** Always recommending the same items (or even the same kind of item) to a user would make him/her feel *bored*.
- **Fraud:** How to detect and deal with fabricated explicit feedbacks (e.g. fake ratings and reviews)?

## Extensions of Matrix Factorization

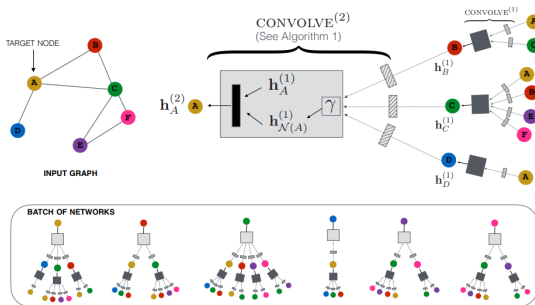
- The score function of vanilla MF:  $u_i^\top v_j$  where user and item representations are static and independent of each other (fixing the model).
- RNN To integrate user history,  $u_i = f(v_{u,1}, v_{u,2}, \dots, v_{u,n})$ 
  - The user representation now depends on his/her previously interacted items.
- Graph-based models to integrate neighboring items/users (in the next slide).
  - The user representation could also depend on behaviors of other users/items.
- Can combine with content-based recommendation (i.e. with user and item features).
- Can combine both explicit and implicit feedbacks.

# Extensions of Matrix Factorization (with Graph-based Models)

- Graph Convolutional Networks on an item copurchase graph
  - When new interactions are added, the copurchase graph and the item representation would also change as well.
  - GCN can also be replaced with other models such as GraphSAGE or PinSAGE (*Hierarchical Temporal Convolutional Networks for Dynamic Recommender Systems*, You et al., 2019)
- GCN on the user-item bipartite graph itself
  - With one layer, becomes GCMC (van den Berg et al., 2017)
  - With neighbor sampling, becomes GraphSAGE.
  - Latest work include STAR-GCN (Zhang et al., 2019) which also deal with cold start problems.



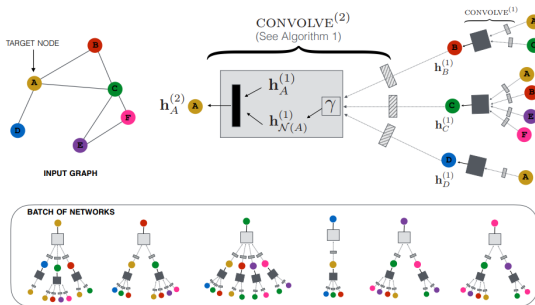
# Learning Item Representations with GCN



Source: *Graph Convolutional Neural Networks for Web-Scale Recommender Systems*, Ying et al. 2018

- The graph is a copurchase graph.

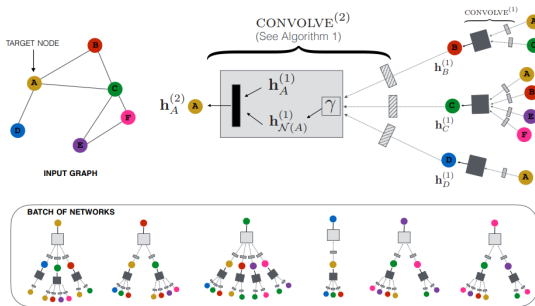
# Learning Item Representations with GCN



Source: *Graph Convolutional Neural Networks for Web-Scale Recommender Systems*, Ying et al. 2018

- The graph is a copurchase graph.
- Item features can be projected before GCN.

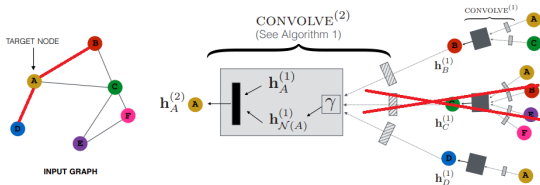
# Learning Item Representations with GCN



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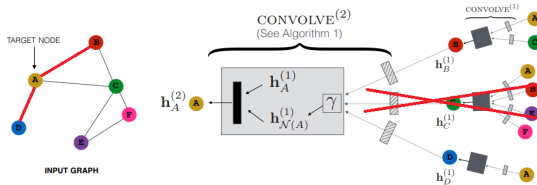
- The graph is a copurchase graph.
- Item features can be projected before GCN.
- During inference, when new copurchases/items appear, we can just recompute the embeddings on the new graph with trained parameters.

# Learning Item Representations with GCN



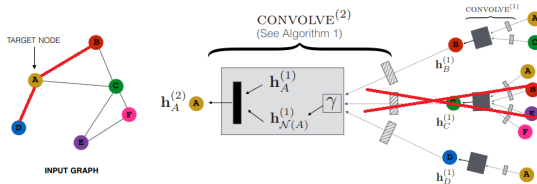
- GraphSAGE - neighbor sampling

# Learning Item Representations with GCN



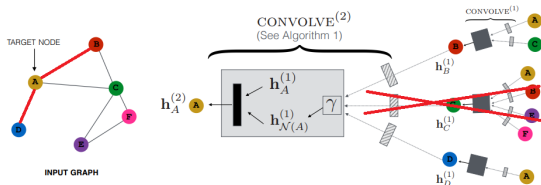
- GraphSAGE - neighbor sampling
- PinSAGE - Neighbors determined by "top-K most frequent nodes visited by random walk with restarts"

# Learning Item Representations with GCN



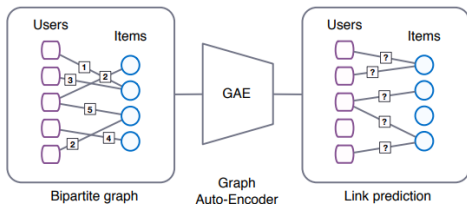
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  - In the example: if  $K = 2$ , then **B** could also be a neighbor of **D**.

# Learning Item Representations with GCN



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  - For concrete details of the random walk algorithm, please refer to *Pixie: A System for Recommending 3+ Billion Items to 200+ Million Users in Real-Time*, Eksombatchai et al., 2017

# Learning Both User and Item Representations with GCMC

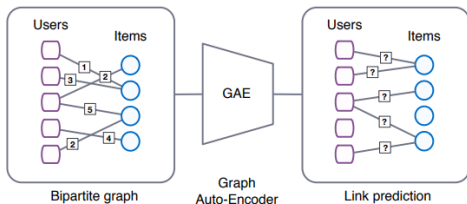


Source: *Graph Convolutional Matrix Completion*, van den Berg et al. 2017

$$\mu_{j \rightarrow i, r} = \frac{1}{c_{ij}} W_r x_j$$
$$h_i = \sigma \left[ \text{accum} \left( \sum_{j \in \mathcal{N}_{i,1}} \mu_{j \rightarrow i,1}, \dots, \sum_{j \in \mathcal{N}_{i,R}} \mu_{j \rightarrow i,R} \right) \right]$$
$$u_i = \sigma(W h_i)$$
$$p(\hat{M}_{ij} = r) = \text{softmax}(u_i^\top Q_r v_j)$$



# Learning Both User and Item Representations with GCMC



Source: *Graph Convolutional Matrix Completion*, van den Berg et al. 2017

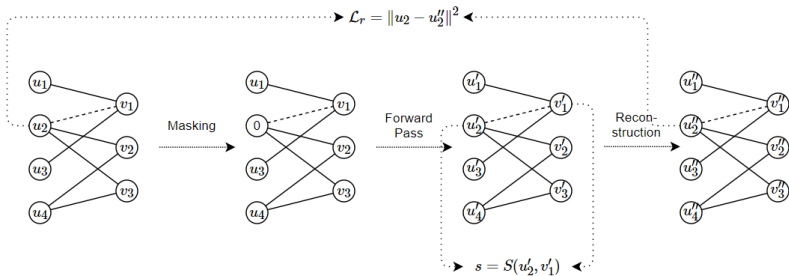
$$\mu_{j \rightarrow i, r} = \frac{1}{c_{ij}} W_r x_j$$

$$h_i = \sigma \left[ \text{accum} \left( \sum_{j \in \mathcal{S}(\mathcal{N}_{i,1})} \mu_{j \rightarrow i, 1}, \dots, \sum_{j \in \mathcal{S}(\mathcal{N}_{i,R})} \mu_{j \rightarrow i, R} \right) \right]$$

$$u_i = \sigma(W h_i)$$

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# Learning Both User and Item Representations with Star-GCN



- Vanilla GCMC can't deal with new users/items without features and with a few interactions.
- STAR-GCN
  - "Mask" the user/item embedding to 0 as if it is new.
  - Reconstruct the embedding after the forward pass and reconstruction pass.

# Coding Session

GraphSAGE on bipartite user-item graph.