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CSC410, Fall 2016 - Homework 3

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Lecture: Tuesday

I am the sole author of this homework. Signature: *Siyuan Zheng*

Grace day tokens usage: **1**

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Problem 1,

(a) Four.

(1) 1, 2, 3, 6, 7, 8, 11

(2) 1, 2, 3, 6, 9, 10, 11

(3) 1, 4, 5, 6, 7, 8, 11

(4) 1, 4, 5, 6, 9, 10, 11

(b)(c)(d)

(1)

Statements

PV

PC

$X \leftarrow x, Y \leftarrow y$

true

1,2,3

$X \leftarrow x-1, Y \leftarrow -y + 2$

$x+y > 10 \ \&\& \text{true}$   
 $= x+y > 10$

6,7,8,11

$X < -2(x-1) = 2x-2$

$2(x-1+y+2) < 20$

$Y < -2(y+2) = 2y+4$

$\&\& x + y > 10$

$= x + y + 1 < 10 \ \&\& x + y > 10$

$= x+y < 9 \ \&\& x + y > 10$

$P = 1,2,3,6,7,8,11$

$D[P] = \{(x,y) | x + y < 9 \text{ and } x + y > 10\}$

$C[P] = \{\}$

Infeasible

(2)

Statements

PV

PC

$X < -x, Y < -y$

true

1,2,3

$X = x - 1, Y < -y + 2$

$\text{true} \ \&\& \ x + y > 10$   
 $= x + y > 10$

6,9,10,11

$X < -4(x-1) = 4x-4$   
 $Y < -4(y+2) = 4y+8$

$2(x-1+y+2) \geq 20 \ \&\& \ x + y > 10$   
 $= x + y + 1 \geq 10 \ \&\& \ x + y > 10$   
 $= x + y \geq 9 \ \&\& \ x + y > 10$   
 $= x + y > 10$

$P = 1,2,3,6,9,10,11$

$D[P] = \{(x,y) \mid x + y > 10\}$

$C[P] = \{\}$

Feasible

Example :  $x = 1, y = 10$

(3)

Statements

PV

PC

$X < -x, Y < -y$

true

1,4,5

$Y < -y-1, X < -x+2$

$\text{true} \ \&\& \ x + y \leq 10$   
 $= x + y \leq 10$

6,7,8,11

$X < -2(x+2) = 2x+4$   
 $Y < -2(y-1) = 2y-2$

$2(x+2+y-1) < 20$   
 $\ \&\& \ x + y \leq 10$   
 $= 2(x+y+1) < 20 \ \&\& \ x + y \leq 10$   
 $= x + y < 9 \ \&\& \ x + y \leq 10$

$$=x+y < 9$$

$P=1,4,5,6,7,8,11$

$D[P] = \{(x,y) \mid x+y < 9\}$

$C[P] = \{\}$

Feasible

Example:  $x=1, y=2$

(4)

Statements

PC

PV

$X < -x, Y < -y$

true

1,4,5

$Y < -y - 1$

$\text{true} \ \&\& \ x + y < = 10$

$X < -x + 2$

$= x + y < = 10$

6,9,10,11

$Y < -4(y-1) = 4y-4$

$2(y-1+x+2) > = 20$

$X < -4(x+2) = 4x + 8$

$\&\& \ x + y < = 10$

$= 2(x+y+1) > = 20$

$\&\& \ x + y < = 10$

$= x + y > = 9 \ \&\& \ x + y < = 10$

$P=1,4,5,6,9,10,11$

$D[P] = \{(x,y) \mid x+y > = 9 \text{ and } x+y < = 10\}$

$C[P] = \{\}$

Feasible

Example:  $x=1, y=9$

## Problem 2

### (a) Path 1

Statements

PV

PC

$A \leftarrow a, X \leftarrow x$

true

1,2

$\text{found} \leftarrow \text{false}, i \leftarrow \text{a.length} - 1$

$\text{true} \ \&\& \ \text{true} = \text{true}$

3,4,5,6

$\text{found} \leftarrow \text{true}, i \leftarrow \text{a.length} - 2$

$\text{!false} \ \&\& \ \text{a.length} - 1 \geq 0$   
 $\&\& \ \text{a}[\text{a.length} - 1] == x$   
 $= \text{a.length} \geq 1 \ \&\&$   
 $\text{a}[\text{a.length} - 1] == x$

3,4,5

$\text{found} \leftarrow \text{true}$

$\text{! true} \ \&\& \ \text{a.length} - 2 \geq 0$   
 $\&\& \ \text{a}[\text{a.length} - 2] == x$   
 $= \text{false}$

$P = 1, 2, 3, 4, 5, 6, 3, 4, 5$

$D[P] = \{(a, x) | \text{false}\}$

$C[P] = \{\}$

Infeasible

### Path 2

Statements

PV

PC

$A \leftarrow a, X \leftarrow x$

true

1,2

$\text{found} \leftarrow \text{false}, i \leftarrow \text{a.length} - 1$

$\text{true} \ \&\& \ \text{true} = \text{true}$

3,4,6

$i \leftarrow \text{a.length} - 2$

$\text{!false} \ \&\& \ \text{a.length} - 1 \geq 0$   
 $\&\& \ \text{a}[\text{a.length} - 1] != x$   
 $= \text{a.length} \geq 1 \ \&\& \ \text{a}[\text{a.length} - 1] != x$

3,7

```
!(true && a.length -2 >=0) && a.length >=1
&&a[a.length-1] != x
=false &&a.length>=2 && a.length >=1 &&
a[a.length-1]!=x
OR = false && a.length <2 && a.length >= 1 &&
a[a.length-1]!=x
OR=true && a.length<2 &&a.length >=1
&&a[a.length-1]!=x
= false OR false OR a.length<2 && a.length>=1
&&a[a.length -1 ]!= x
=a.length == 1&& a[a.length-1] != x
= a.length == 1 && a[0] != x
```

P = 1,2,3,4,6,3,7

D[P] = {(a,x)|a.length ==1 && a[0] != x}

C[P] = {}

Feasible

Example: a = [5] , x = 1

Path 3

Statements

PV

PC

A <- a, X<-x

true

1,2

found<-false, i <- a.length -1

true && true = true

3,4,5,6

found<-true , i <-a.length-2

```
!false && a.length -1 >= 0
&& a[a.length -1 ] ==x
= true && a.length >=1
&&a[a.length-1] ==x
=a.length >=1 &&
```

a[a.length-1] ==x

3,7

a[a.length-1] ==x &&  
a.length >=1 &&  
!(false && a.length-2>=0)  
=a[a.length-1] ==x&&  
a.length > =1 &&  
true && a.length >=2  
OR = a[a.length -1]==x  
&& a.length >= 1  
&& true && a.length <2  
Or = a[a.length-1]==x  
&7a.length>=1  
&&false && a.length<2  
=a[a.length-1] ==x &&  
a.length >= 2  
OR a[a.length-1] ==x &&  
a.length == 1  
=a[a.length-1] == x && a.length >= 1

P = 1,2,3,4,5,6,3,7

D[P]= {(a,x)|a.length >=1 , a[a.length-1] ==x}

C[P] = {}

Feasible

Example: a = [2,3,4] ,x =4

Path 4

Statements

PV

PC

A<-a , X <- x

true

1,2

found<-false, i<-a.length-1

true && true = true

3,7

true && !(true && a.length-1>=0)

=(true && a.length >=1)

=false && a.length >=1

OR false && a.length < 1

OR true && a.length < 1

= a.length < 1

P= 1,2,3,7

D[P]={ (a,x) | a.length<1 }

C[P] = { }

Feasible

Example : a = [ ], x = 5