ECOM20001 Econometrics 1

Tutorial 8 (Week 8 - Thursday)

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This slides helps us to develop a transformed regression that allows us to use an individual hypothesis test to represent joint hypothesis test.

The null hypothesis: the sum of the coefficients on alcohol and unmarried equals the coefficient on smoker against the alternative that the equality does not hold.

Given the initial regression:

$$\mathsf{Birthweight}_i = \beta_0 + \beta_1 \; \mathsf{Smoker}_i + \beta_2 \; \mathsf{Alcohol}_i + \beta_3 \; \mathsf{Unmarried}_i + X_i + u_i$$

where X_i includes all other non-listed regressor.

We are trying to test:

$$H_0: \beta_1 = \beta_2 + \beta_3$$

$$\mathsf{H}_1:\ \beta_1\neq\beta_2+\beta_3$$

 $\mathsf{Birthweight}_i = \beta_0 + \beta_1 \mathsf{Smoker}_i + \beta_2 \mathsf{Alcohol}_i + \beta_3 \mathsf{Unmarried}_i + X_i + u_i$

Birthweight_i =
$$\beta_0 + \beta_1$$
Smoker_i + β_2 Alcohol_i + β_3 Unmarried_i + $X_i + u_i$
= $\beta_0 + \beta_1$ Smoker_i + β_2 Alcohol_i + β_3 Unmarried_i + $X_i + u_i$

$$\begin{aligned} \mathsf{Birthweight}_i &= \beta_0 + \beta_1 \mathsf{Smoker}_i + \beta_2 \mathsf{Alcohol}_i + \beta_3 \mathsf{Unmarried}_i + X_i + u_i \\ &= \beta_0 + \beta_1 \mathsf{Smoker}_i + \beta_2 \mathsf{Alcohol}_i + \beta_3 \mathsf{Unmarried}_i + X_i + u_i \\ &+ \beta_2 \mathsf{Smoker}_i - \beta_2 \mathsf{Smoker}_i + \beta_3 \mathsf{Smoker}_i - \beta_3 \mathsf{Smoker}_i \end{aligned}$$

$$\begin{split} \mathsf{Birthweight}_i &= \beta_0 + \beta_1 \mathsf{Smoker}_i + \beta_2 \mathsf{Alcohol}_i + \beta_3 \mathsf{Unmarried}_i + X_i + u_i \\ &= \beta_0 + \beta_1 \mathsf{Smoker}_i + \beta_2 \mathsf{Alcohol}_i + \beta_3 \mathsf{Unmarried}_i + X_i + u_i \\ &+ \beta_2 \mathsf{Smoker}_i - \beta_2 \mathsf{Smoker}_i + \beta_3 \mathsf{Smoker}_i - \beta_3 \mathsf{Smoker}_i \\ &= \beta_0 + (\beta_1 - \beta_2 - \beta_3) \mathsf{Smoker}_i + \beta_2 (\mathsf{Alcohol}_i + \mathsf{Smoker}_i) \end{split}$$

Birthweight_i =
$$\beta_0 + \beta_1 \text{Smoker}_i + \beta_2 \text{Alcohol}_i + \beta_3 \text{Unmarried}_i + X_i + u_i$$

= $\beta_0 + \beta_1 \text{Smoker}_i + \beta_2 \text{Alcohol}_i + \beta_3 \text{Unmarried}_i + X_i + u_i$
+ $\beta_2 \text{Smoker}_i - \beta_2 \text{Smoker}_i + \beta_3 \text{Smoker}_i - \beta_3 \text{Smoker}_i$
= $\beta_0 + (\beta_1 - \beta_2 - \beta_3) \text{Smoker}_i + \beta_2 (\text{Alcohol}_i + \text{Smoker}_i)$
+ $\beta_3 (\text{Unmarried}_i + \text{Smoker}_i) + X_i + u_i$

$$\begin{aligned} \text{Birthweight}_i &= \beta_0 + \beta_1 \text{Smoker}_i + \beta_2 \text{Alcohol}_i + \beta_3 \text{Unmarried}_i + X_i + u_i \\ &= \beta_0 + \beta_1 \text{Smoker}_i + \beta_2 \text{Alcohol}_i + \beta_3 \text{Unmarried}_i + X_i + u_i \\ &+ \beta_2 \text{Smoker}_i - \beta_2 \text{Smoker}_i + \beta_3 \text{Smoker}_i - \beta_3 \text{Smoker}_i \\ &= \beta_0 + (\beta_1 - \beta_2 - \beta_3) \text{Smoker}_i + \beta_2 (\text{Alcohol}_i + \text{Smoker}_i) \\ &+ \beta_3 (\text{Unmarried}_i + \text{Smoker}_i) + X_i + u_i \\ &= \beta_0 + (\beta_1 - \beta_2 - \beta_3) \text{Smoker}_i + \beta_2 (W_i) + \beta_3 (Z_i) + X_i + u_i \end{aligned}$$

Birthweight_i =
$$\beta_0 + \beta_1 \text{Smoker}_i + \beta_2 \text{Alcohol}_i + \beta_3 \text{Unmarried}_i + X_i + u_i$$

= $\beta_0 + \beta_1 \text{Smoker}_i + \beta_2 \text{Alcohol}_i + \beta_3 \text{Unmarried}_i + X_i + u_i$
+ $\beta_2 \text{Smoker}_i - \beta_2 \text{Smoker}_i + \beta_3 \text{Smoker}_i - \beta_3 \text{Smoker}_i$
= $\beta_0 + (\beta_1 - \beta_2 - \beta_3) \text{Smoker}_i + \beta_2 (\text{Alcohol}_i + \text{Smoker}_i)$
+ $\beta_3 (\text{Unmarried}_i + \text{Smoker}_i) + X_i + u_i$
= $\beta_0 + (\beta_1 - \beta_2 - \beta_3) \text{Smoker}_i + \beta_2 (W_i) + \beta_3 (Z_i) + X_i + u_i$
= $\beta_0 + \gamma \text{Smoker}_i + \beta_2 (W_i) + \beta_3 (Z_i) + X_i + u_i$