Simulation-Based Optimization of Highway Active Traffic Management Strategy Designs-Appendix

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1 Overview of the proposed SBO method

The overviwe of the proposed SBO method is shown in Figure 1.

2 Pseudocode for CTM

The pseudocode for CTM is shown in Algorithm 1

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Algorithm 1 Cell Transmission Model
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1: For each time step k \in K:
       Compute mainline inlet flow \phi_{0,k} via Equation (18).
       For each mainline cell j \in J:
 3:
         If j = 1 and k = 1, then compute density \rho_{j,k} via Equation (20).
 4:
         Else if k < j, then compute density \rho_{j,k} via Equation (21).
Compute jam density \rho_{j,k}^{\text{jam}}, critical density \rho_{j,k}^{\text{cri}}, and capacity q_{j,k}^{\text{cap}} via Equations (14)-(16).
 5:
 6:
       End for
 7:
 8:
       For each mainline cell j \in J:
         If j \in J^*, then compute mainline outflow \phi_{j,k}^m via Equation (10).
 9:
          Else, compute mainline outflow \phi_{j,k}^m via Equation (11).
10:
11:
       For each on-ramp g \in G:
12:
         If k = 1, then
13:
             Compute queue length l_{g,k} via Equation (19).
14:
            Compute on-ramp outflow \phi_{q,k}^r via Equation (13).
15:
16:
         If k \in K^*, then compute queue length l_{g,k+1} via Equation (12).
17:
       End for
18:
       For each mainline cell j \in J:
19:
          If k \in K^*, then compute density \rho_{j,k+1} via Equation (9).
20:
       End for
21:
```

3 Pseudocode for AHA sampling

The pseudocode for CTM is shown in Algorithm $2\,$

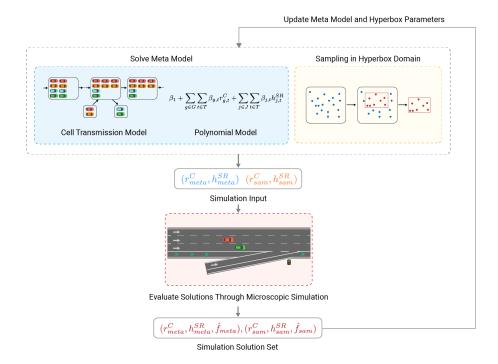


Figure 1: Overview of the SBO technique for determining the highway management strategies.

Algorithm 2 AHA sampling

- 1: Initialization:
- 2: Set iteration steps u = 0.
- 2: Set heration steps u=0.
 3: Set hyperbox parameters for on-ramp in-merge rates $\mathcal{H}_u^{RC}=\{0.15\leq r_{g,t}^c\leq 1, \forall g\in G, \forall t\in T\}$.
 4: Set hyperbox parameters for shoulder lane states $\mathcal{H}_u^{HSR}=\{h_{g,t}^{SR}\in\{0,1\}, \forall g\in G, \forall t\in T\}$.
- 5: Step 1: Sampling
- 6: Uniformly sample within the hyperbox domain defined by Equations 43-44 to obtain ω solutions:

$$(\mathbf{r}^c_{sam,1,u},\mathbf{h}^{SR}_{sam,1,u}),\dots,(\mathbf{r}^c_{sam,\omega,u},\mathbf{h}^{SR}_{sam,\omega,u}).$$

- 7: Step 2: Simulation
- 8: Evaluate $(\mathbf{r}_{sam,1,u}^c, \mathbf{h}_{sam,1,u}^{SR}), \dots, (\mathbf{r}_{sam,\omega,u}^c, \mathbf{h}_{sam,\omega,u}^{SR})$ through microscopic simulations to obtain delays:

$$\hat{f}_{sam,1,u},\ldots,\hat{f}_{sam,\omega,u}.$$

- 9: Update simulation solution sets through Equations 38 and 42.
- 10: Step 3: Updating hyperbox parameters
- 11: Update hyperbox parameters through Equations 43-44.
- 12: Update iteration step u = u + 1.
- 13: Return to Step 1.