

Simulation-Based Optimization of Highway Active Traffic Management Strategy Designs

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1 Appendix: Pseudocode for CTM

Algorithm 1 Cell Transmission Model

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1: For each time step  $k \in K$ :
2:   Compute mainline inlet flow  $\phi_{0,k}$  via Equation (18).
3:   For each mainline cell  $j \in J$ :
4:     If  $j = 1$  and  $k = 1$ , then compute density  $\rho_{j,k}$  via Equation (20).
5:     Else if  $k < j$ , then compute density  $\rho_{j,k}$  via Equation (21).
6:     Compute jam density  $\rho_{j,k}^{\text{jam}}$ , critical density  $\rho_{j,k}^{\text{cri}}$ , and capacity  $q_{j,k}^{\text{cap}}$  via Equations (14)-(16).
7:   End for
8:   For each mainline cell  $j \in J$ :
9:     If  $j \in J^*$ , then compute mainline outflow  $\phi_{j,k}^m$  via Equation (10).
10:    Else, compute mainline outflow  $\phi_{j,k}^m$  via Equation (11).
11:   End for
12:   For each on-ramp  $g \in G$ :
13:     If  $k = 1$ , then
14:       Compute queue length  $l_{g,k}$  via Equation (19).
15:       Compute on-ramp outflow  $\phi_{g,k}^r$  via Equation (13).
16:     End if
17:     If  $k \in K^*$ , then compute queue length  $l_{g,k+1}$  via Equation (12).
18:   End for
19:   For each mainline cell  $j \in J$ :
20:     If  $k \in K^*$ , then compute density  $\rho_{j,k+1}$  via Equation (9).
21:   End for
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2 Appendix: Pseudocode for AHA sampling

Algorithm 2 AHA sampling

1: **Initialization:**

2: Set iteration steps $u = 0$.

3: Set hyperbox parameters for on-ramp in-merge rates $\mathcal{H}_u^{RC} = \{0.15 \leq r_{g,t}^c \leq 1, \forall g \in G, \forall t \in T\}$.

4: Set hyperbox parameters for shoulder lane states $\mathcal{H}_u^{HSR} = \{h_{g,t}^{SR} \in \{0, 1\}, \forall g \in G, \forall t \in T\}$.

5: **Step 1: Sampling**

6: Uniformly sample within the hyperbox domain defined by Equations 43-44 to obtain ω solutions:

$$(\mathbf{r}_{sam,1,u}^c, \mathbf{h}_{sam,1,u}^{SR}), \dots, (\mathbf{r}_{sam,\omega,u}^c, \mathbf{h}_{sam,\omega,u}^{SR}).$$

7: **Step 2: Simulation**

8: Evaluate $(\mathbf{r}_{sam,1,u}^c, \mathbf{h}_{sam,1,u}^{SR}), \dots, (\mathbf{r}_{sam,\omega,u}^c, \mathbf{h}_{sam,\omega,u}^{SR})$ through microscopic simulations to obtain delays:

$$\hat{f}_{sam,1,u}, \dots, \hat{f}_{sam,\omega,u}.$$

9: Update simulation solution sets through Equations 38 and 42.

10: **Step 3: Updating hyperbox parameters**

11: Update hyperbox parameters through Equations 43-44.

12: Update iteration step $u = u + 1$.

13: Return to Step 1.
