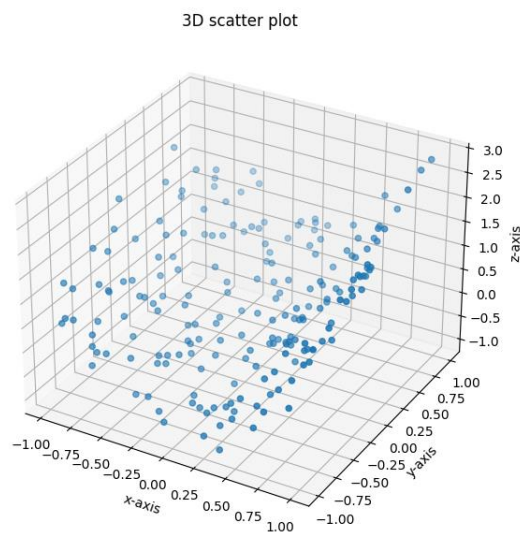


(i) (a)

The following is the picture drawn:



It looks like on a curved surface.

(b)

1. First we call:

```
polyFeatures = PolynomialFeatures(degree=5)
print(polyFeatures.get_feature_names())
```

2. We can get 21 features:

```
['1', 'x0', 'x1', 'x0^2', 'x0 x1', 'x1^2', 'x0^3', 'x0^2 x1', 'x0 x1^2', 'x1^3', 'x0^4', 'x0^3 x1', 'x0^2 x1^2', 'x0 x1^3', 'x1^4', 'x0^5', 'x0^4 x1', 'x0^3 x1^2', 'x0^2 x1^3', 'x0 x1^4', 'x1^5']
```

3. We use polynomial features to get new training set data:

```
X_Poly = polyFeatures.fit_transform(X_train)
```

According to the cost function of lasso regression in the sklearn document 1.0:

4. I use $\alpha=0.001$ $\alpha=0.1$ $\alpha=1$ and $\alpha=10$ to get the trained parameters of the lasso regression model:

$\alpha=0.001$:

coefficient(Corresponding to 21 features in step2):

```
[0.00000,-0.00201,0.92001,1.93782,0.06344,0.00000,-
0.02853,0.08028,0.00000,0.00000,0.07988,-0.00000,0.00000,0.00028,-0.00000,-
0.00000,0.00000,0.03607,0.00000,-0.00000,0.07060]
```

$\alpha=0.1$:

coefficient(Corresponding to 21 features in step2):

```
[0.00000,0.00000,0.57765,0.79780,0.00000,-  
0.00000,0.00000,0.00000,0.00000,0.00000,0.00000,0.00000,0.00000,0.00000,-  
0.00000,0.00000,0.00000,0.00000,0.00000,0.00000,0.00000]
```

alpha=1.0:

coefficient(Corresponding to 21 features in step2):

```
[0.00000,0.00000,0.00000,0.00000,0.00000,-  
0.00000,0.00000,0.00000,0.00000,0.00000,0.00000,0.00000,0.00000,0.00000,-  
0.00000,0.00000,0.00000,0.00000,0.00000,0.00000,0.00000]
```

alpha=10:

coefficient(Corresponding to 21 features in step2):

```
[0.00000,0.00000,0.00000,0.00000,0.00000,-  
0.00000,0.00000,0.00000,0.00000,0.00000,0.00000,0.00000,0.00000,0.00000,-  
0.00000,0.00000,0.00000,0.00000,0.00000,0.00000,0.00000]
```

We can see that as the alpha value increases, the coefficients of many features become 0,

When alpha=1 and 10, all coefficients are so small that they can only be displayed with 0 or are already 0.

According to the cost function of lasso regression in the sklearn 1.0 document:

$$\min_{\omega} \frac{1}{2n_{samples}} \|X\omega - y\|_2^2 + \alpha \|\omega\|_1$$

Alpha is a constant. The larger the number, the greater the penalty will be, so it may happen that the coefficient of some features becomes 0 quickly.

I used DummyRegressor as the baseline predictor to calculate Mean square error to compare with the model. Due to the relatively small amount of data, I ran 100 times to calculate the average. The results are as follows:

Alpha=0.001:

Mean square error: Lasso regression with alpha=0.001:0.035567000244699526
dummy:0.6239296864126294

Alpha=0.1:

square error: Lasso regression with alpha=0.1:0.21138985011189354
dummy:0.6357500355013349

Alpha=1:

square error: Lasso regression with alpha=1:0.6224942150003617
dummy:0.6224942150003617

Alpha=10:

square error: Lasso regression with $\alpha=10$:0.6385585924111834
dummy:0.6385585924111834

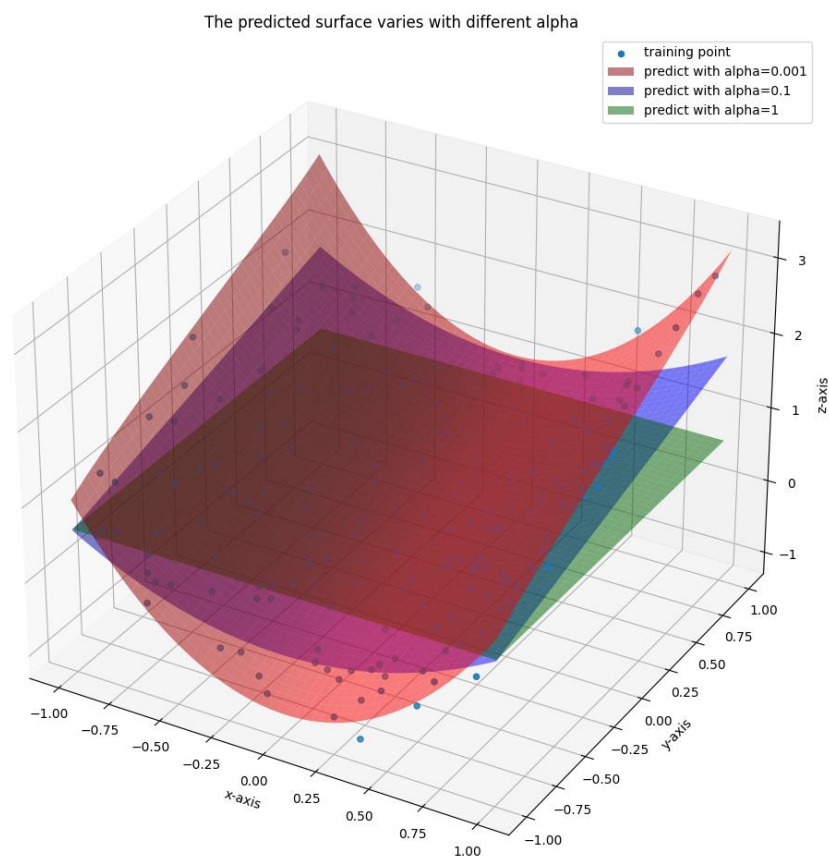
We can see that the error is the smallest when $\alpha=0.001$, which may be due to the data set being too small.

When $\alpha \geq 1$, lasso regression has the same performance as dummyRegressor

(c)

I use the following command to get the 3D picture below(Since all coefficients are displayed as 0 starting from $\alpha=1$, no graph with $\alpha=10$ is drawn):

```
ax.scatter(dataset[:, 0], dataset[:, 1], dataset[:, 2],  
label='training point')  
Curve1 = ax.plot_surface(Xitest, Yitest, Z_test, rstride=1,  
cstride=1, color='r', label='predict with alpha=0.001', alpha=0.5)  
Curve2 = ax.plot_surface(Xitest, Yitest, Z_test2, rstride=1,  
cstride=1, color='b', label='predict with alpha=0.1', alpha=0.5)  
Curve3 = ax.plot_surface(Xitest, Yitest, Z_test3, rstride=1,  
cstride=1, color='g', label='predict with alpha=1', alpha=0.5)
```



We can see from the figure that when $\alpha=1$, since all coefficients are almost 0, the predicted value (Z) is equal to the intercept, so it looks like a plane. When $\alpha=0.1$, only the two features coefficients x_1 and x_0^2 are not 0, so the predicted value looks like a curved surface. As the α becomes smaller and smaller, we see more and more coefficients acting on the curve. It gets steeper and steeper until the highest point in the upper right corner of the picture

(d)

Through the data of b and the picture of c , we can know that in Lasso regression, according to the formula:

Too large α value will cause all coefficient values to approach 0 or become 0, and all predictions will become a plane. This is under-fitting, while over-fitting is the opposite. Smaller α values will make a lot of The features are all involved in the calculation, which will make the prediction fit the training data very well, which will lead to overfitting. Both overfitting and underfitting can lead to inaccurate predictions.

At the moment, we can set a large α value and a small α value, and then adjust between the two to achieve a balance between over-fitting and under-fitting.

(e)

Ridge regression:

First, use the same α as the Lasso regression, and you can get the parameters and graphs as follows:

$\alpha=0.001$

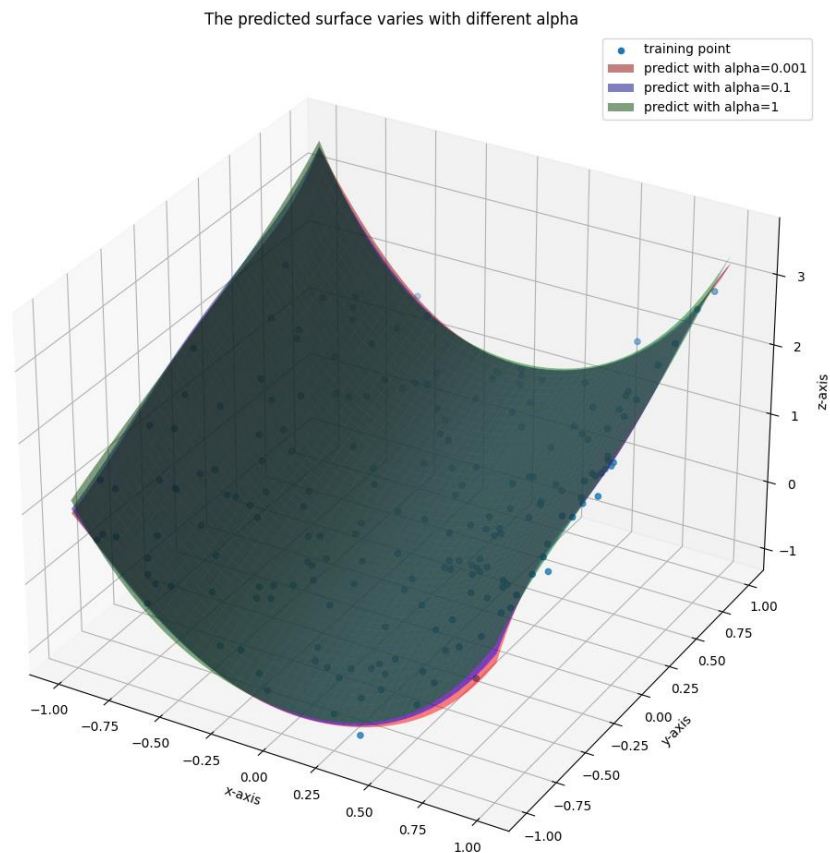
[0.00000,0.10403,0.95744,1.85515,0.11818,0.19266,-0.66558,-0.06472,0.56106,
-0.11089,0.21874,-0.11400,-0.01949,0.02830,-0.20109,0.46131,0.11628,0.22131,0.22534,
-0.78410,0.13251]

$\alpha=0.1$

[0.00000,0.05874,0.90504,1.73928,0.11819,0.15725,
-0.35788,0.01209,0.33811,0.03052,0.33383,-0.13157,0.02844,0.03206,
-0.17726,0.18456,0.12399,0.21060,0.10150,-0.51752,0.04219]

$\alpha=1$

0.00000,0.01628,0.82104,1.34114,0.08438,0.04200,
-0.08823,0.11966,0.07914,0.14773,0.64801,-0.08052,0.20422,0.01449,-0.11256,
-0.00504,0.08470,0.07817,0.01128,-0.15145,0.01271



We can see that the coefficient of each feature has a value, and the predicted surface is similar.

So we based on the cost function of ridge regression in the sklearn document:

$$\min_w \|Xw - y\|_2^2 + \alpha \|w\|_2^2$$

We need a larger alpha and a larger interval to change the coefficients of the model, so we reset the parameters to get:

Alpha=1

[0.00000,0.01628,0.82104,1.34114,0.08438,0.04200,-
0.08823,0.11966,0.07914,0.14773,0.64801,-0.08052,0.20422,0.01449,-0.11256,-
0.00504,0.08470,0.07817,0.01128,-0.15145,0.01271]

Alpha=50

[0.00000,0.02062,0.37686,0.40346,0.05398,-0.03087,0.06037,0.07134,-
0.01392,0.19637,0.34309,0.04032,0.10295,0.04486,-
0.03318,0.07309,0.01914,0.00598,0.03749,-0.01228,0.12984]

Alpha=1000

[0.00000,0.01008,0.04740,0.03093,0.00518,-
0.00489,0.01169,0.01196,0.00131,0.02832,0.02728,0.00373,0.00654,0.00415,-
0.00438,0.01139,0.00545,0.00273,0.00749,0.00082,0.02038]

I still use dummyRegressor and model to find mean square error:

Alpha=1

square error: Ridge regression with alpha=1:0.03881332342730842
dummy:0.6073408329876667

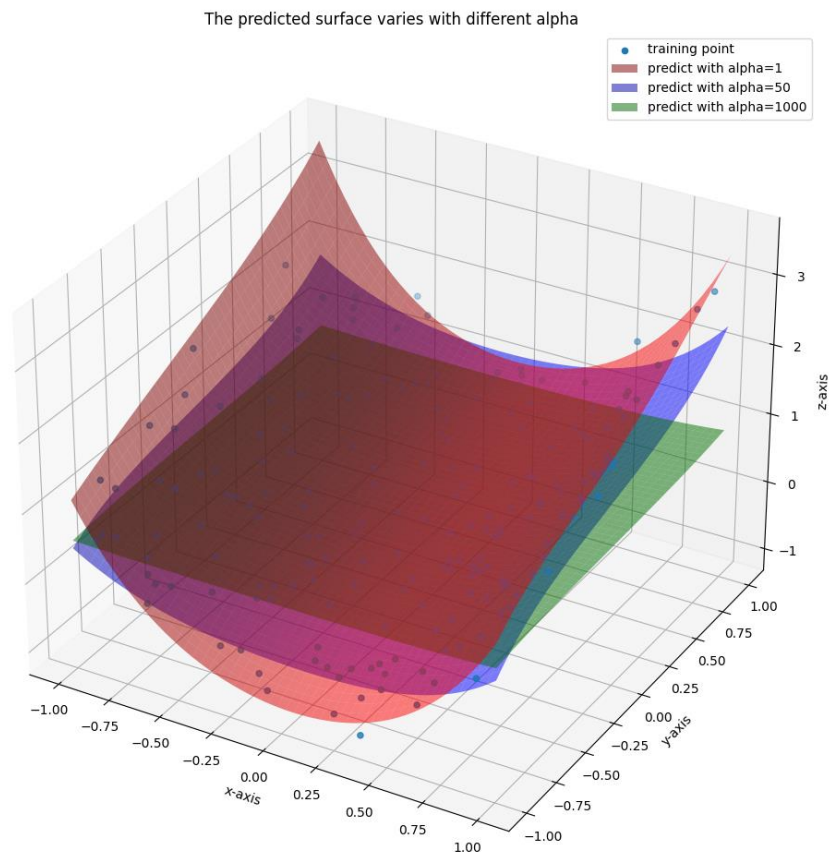
Alpha=50

square error: Ridge regression with alpha=1:0.23864386320786657
dummy:0.6208646774111177

Alpha=1000

square error: Ridge regression with alpha=1:0.598390552836333
dummy:0.6498425837571997

Finally drew a 3D picture



We can see that the predicted surface has changed, resulting in over-fitting and under-fitting, but all the other 20 features except the first feature (1) have values. With the change of C , the proportion of each feature has produced Variety. This shows that Lasso regression focuses on removing useless features, while ridge regression focuses on extracting every feature.

(ii) Using the Lasso model with polynomial features from (i) you'll now look at using cross-validation to select C .

(a)

According to the further experiments of the 3D graphs in (i)(c), when $\alpha < 0.001$, the curve cannot become more tortuous, and when $\alpha > 0.4$, the prediction has become a plane. So I use 0.001 as the start of the error bar and 0.4 as the end.

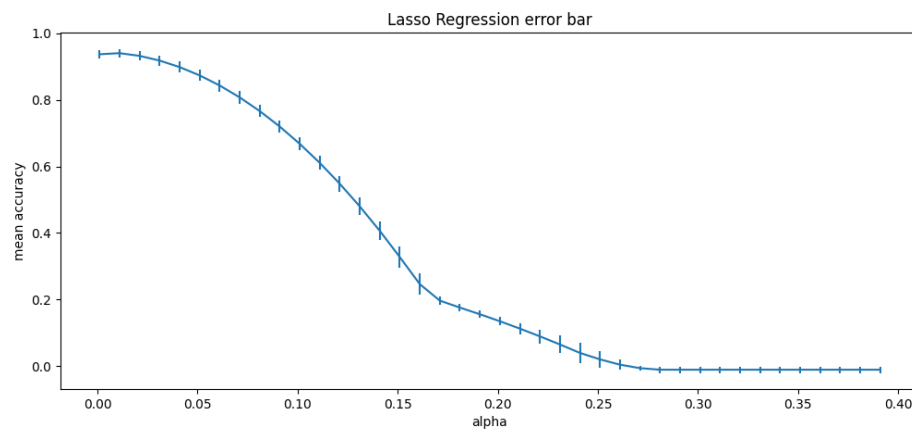
First set the alpha value to 0.001, judge that it is less than 0.4 and stop the while loop. Each time the loop alpha value is increased by 0.01, a new model is generated according to the alpha value in each loop, and use 5-fold cross-validation to obtain mean accuracy and standard deviation of the prediction error.

```

alpha = 0.001
alphas, means, stds = [], [], []
while alpha < 0.4:
    LassoR = Lasso(alpha=alpha)
    scores = cross_val_score(LassoR, Xtrain_poly, y_train, cv=5)
    alphas.append(alpha)
    means.append(scores.mean())
    stds.append(scores.std())
    alpha = alpha + 0.01

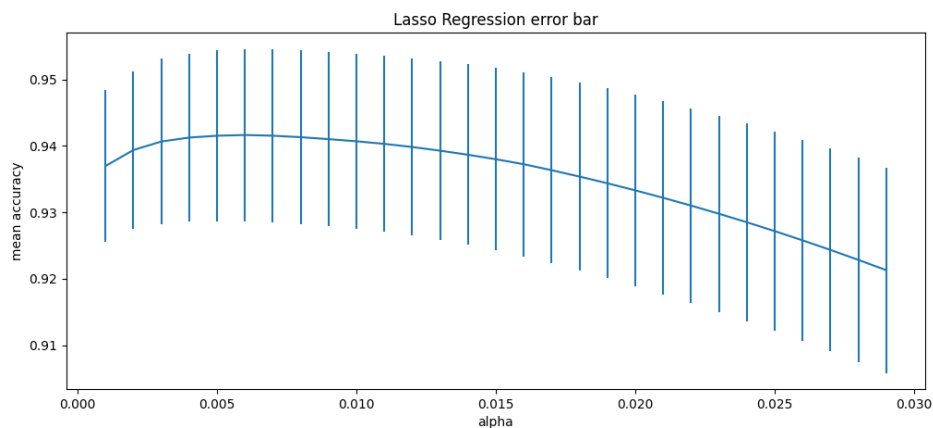
```

Draw the error bar chart according to the above code, the x-axis is the value of alpha, the y-axis is the mean accuracy, and the vertical line on each point is the standard deviation of the prediction error:



(b)

According to the figure in (ii)(a), we can see that the best value may be between 0.001 and 0.03, so we further draw the errorbar, starting from 0.001 to ending at 0.03, and increasing by 0.001 at each step, we get the following figure:



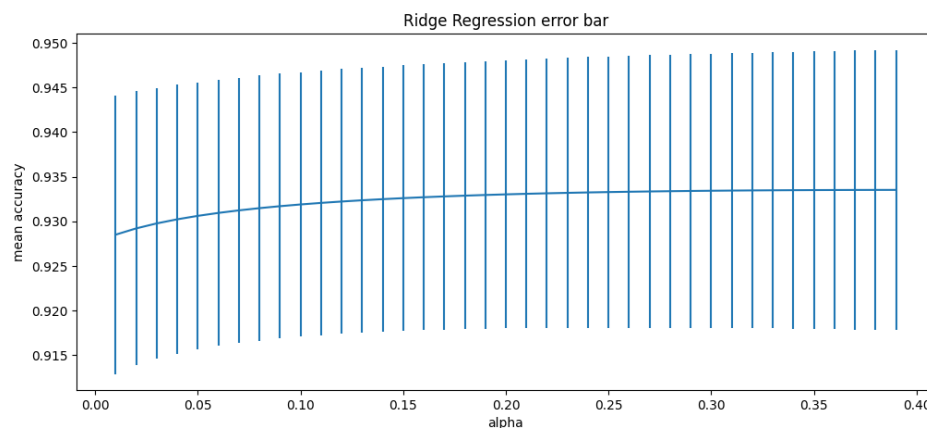
According to the figure, and the formula:

$$\min_{\omega} \frac{1}{2n_{\text{samples}}} \|X\omega - y\|_2^2 + \alpha \|\omega\|_1$$

I might choose $\alpha=0.005$ as the best C, Because when $\alpha=0.005$, the accuracy of the model is the highest and the standard deviation of the prediction error is the smallest

(c)

According to the same steps of (ii)(a)-(ii)(b) (just replacing the model), we can get the errorbar of the ridge regression:



I might choose $\alpha=0.3$ as the best C because the accuracy is high and the standard deviation of the prediction error is the smallest

Appendix

code

i-a

```
1. import numpy as np
2. import matplotlib.pyplot as plt
3.
4. #Get data from file
5. data = str(open("data").read()).split('\n')
6. dataset = []
7. for d in data[1:]:
8.     nums = d.split(',')
9.     dxy = []
10.    dxy.append(float(nums[0]))
11.    dxy.append(float(nums[1]))
12.    dxy.append(float(nums[2]))
13.    dataset.append(dxy)
14. dataset = np.array(dataset)
15. x = dataset[:, 0]
```

```

16. y = dataset[:, 1]
17. z = dataset[:, 2]
18.
19. #Draw a 3D scatter plot
20. fig = plt.figure(figsize=(12, 12))
21. ax = fig.add_subplot(projection='3d')
22. ax.scatter(dataset[:,0],dataset[:,1],dataset[:,2])
23. ax.set_xlabel('x-axis')
24. ax.set_ylabel('y-axis')
25. ax.set_zlabel('z-axis')
26. ax.set_title('3D scatter plot' )
27. plt.show()

```

ib-ic

```

1. import numpy as np
2. from scipy.interpolate import griddata
3. import matplotlib.pyplot as plt
4. from sklearn.preprocessing import PolynomialFeatures
5. from sklearn.linear_model import Lasso
6.
7. #Get data from file
8. data = str(open("data").read()).split('\n')
9. dataset = []
10. for d in data[1:]:
11.     nums = d.split(',')
12.     dxy = []
13.     dxy.append(float(nums[0]))
14.     dxy.append(float(nums[1]))
15.     dxy.append(float(nums[2]))
16.     dataset.append(dxy)
17. dataset = np.array(dataset)
18.
19. #Get an array of x, y, z
20. x = dataset[:, 0]
21. y = dataset[:, 1]
22. z = dataset[:, 2]
23.
24. #Generate training data and training target array
25. X_train = dataset.take([0, 1], axis=1)
26. y_train = dataset[:, 2]
27.
28. #Add polynomial
29. polyFeatures = PolynomialFeatures(degree=5)
30. print(polyFeatures.get_feature_names())
31. X_Poly = polyFeatures.fit_transform(X_train)
32. print(polyFeatures.get_feature_names())
33.
34. #Generate Lasso regression model and train the model
35. LassoR = Lasso(alpha=0.001)
36. LassoR.fit(X_Poly, y_train)
37.
38. #Generate test set and add polynomial
39. Xtest = []
40. grid = np.linspace(-1, 1)
41. for i in grid:
42.     for j in grid:
43.         Xtest.append([i, j])
44. Xtest = np.array(Xtest)
45. Xtest_poly = polyFeatures.fit_transform(Xtest)
46.
47. #Use the test set to predict and get the target
48. X_pre = LassoR.predict(Xtest_poly)
49.
50. Xtest_x = Xtest[:, 0]

```

```

51. Xtest_y = Xtest[:, 1]
52.
53. #Generate plot_surface data
54. xi = np.linspace(min(x), max(x))
55. yi = np.linspace(min(y), max(y))
56. X, Y = np.meshgrid(xi, yi)
57. Z = griddata((x, y), z, (X, Y), 'nearest')
58. xitest = np.linspace(min(Xtest_x), max(Xtest_x))
59. yitest = np.linspace(min(Xtest_y), max(Xtest_y))
60. Xitest, Yitest = np.meshgrid(xitest, yitest)
61. Z_test = griddata((Xtest_x, Xtest_y), X_pre, (Xitest, yitest), 'nearest')
62.
63. #Create 3D canvas
64. fig = plt.figure(figsize=(12, 12))
65. ax = fig.add_subplot(projection='3d')
66.
67. #Draw the first 3D surface
68. ax.scatter(dataset[:, 0], dataset[:, 1], dataset[:, 2], label='training point')
69. Curve1 = ax.plot_surface(Xitest, Yitest, Z_test, rstride=1, cstride=1, color='r', label='predict with alpha=0.001', alpha=0.5)
70. Curve1._facecolors2d = Curve1._facecolor3d
71. Curve1._edgecolors2d = Curve1._edgecolor3d
72.
73. #Generate the second model and draw the surface
74. LassoR2 = Lasso(alpha=0.1)
75. LassoR2.fit(X_Poly, y_train)
76. X_pre2 = LassoR2.predict(Xtest_poly)
77. Z_test2 = griddata((Xtest_x, Xtest_y), X_pre2, (Xitest, yitest), 'nearest')
78. Curve2 = ax.plot_surface(Xitest, Yitest, Z_test2, rstride=1, cstride=1, color='b', label='predict with alpha=0.1', alpha=0.5)
79. Curve2._facecolors2d = Curve2._facecolor3d
80. Curve2._edgecolors2d = Curve2._edgecolor3d
81.
82. #Generate the third model and draw the surface
83. LassoR3 = Lasso(alpha=1)
84. LassoR3.fit(X_Poly, y_train)
85. X_pre3 = LassoR3.predict(Xtest_poly)
86. Z_test3 = griddata((Xtest_x, Xtest_y), X_pre3, (Xitest, yitest), 'nearest')
87. Curve3 = ax.plot_surface(Xitest, Yitest, Z_test3, rstride=1, cstride=1, color='g', label='predict with alpha=1', alpha=0.5)
88. Curve3._facecolors2d = Curve3._facecolor3d
89. Curve3._edgecolors2d = Curve3._edgecolor3d
90.
91. #Set picture parameters and draw 3D pictures flatly
92. ax.legend()
93. ax.set_xlabel('x-axis')
94. ax.set_ylabel('y-axis')
95. ax.set_zlabel('z-axis')
96. ax.set_title('The predicted surface varies with different alpha')
97. plt.show()

```

ib for compare

```

1. import numpy as np
2. from sklearn.model_selection import train_test_split
3. from sklearn.preprocessing import PolynomialFeatures
4. from sklearn.linear_model import Lasso
5. from sklearn.dummy import DummyRegressor
6. from sklearn.metrics import mean_squared_error
7.
8. #Get data from file
9. data = str(open("data").read()).split('\n')

```

```

10. dataset = []
11. for d in data[1:]:
12.     nums = d.split(',')
13.     dxy = []
14.     dxy.append(float(nums[0]))
15.     dxy.append(float(nums[1]))
16.     dxy.append(float(nums[2]))
17.     dataset.append(dxy)
18. dataset = np.array(dataset)
19.
20. x = dataset[:, 0]
21. y = dataset[:, 1]
22. z = dataset[:, 2]
23. X_train = dataset.take([0, 1], axis=1)
24. y_train = dataset[:, 2]
25.
26. times = 100
27. modelSq, dummySq = 0, 0
28. for i in range(0, times):
29.     Xtrain, Xtest, ytrain, ytest = train_test_split(X_train, y_train, test_s
        ize=0.2)
30.     Xtrain_poly = PolynomialFeatures(degree=5).fit_transform(Xtrain)
31.     Xtest_poly = PolynomialFeatures(degree=5).fit_transform(Xtest)
32.     lassoModel = Lasso(alpha=0.01).fit(Xtrain_poly, ytrain)
33.     dummy = DummyRegressor(strategy='mean').fit(Xtrain_poly, ytrain)
34.     ypred = lassoModel.predict(Xtest_poly)
35.     ydummy = dummy.predict(Xtest_poly)
36.     modelSq1 = mean_squared_error(ytest, ypred)
37.     dummySq1 = mean_squared_error(ytest, ydummy)
38.     print(modelSq1)
39.     print(dummySq1)
40.     modelSq = modelSq+modelSq1
41.     dummySq = dummySq+dummySq1
42.
43. print('square error: Lasso regression with alpha=10:'+str(modelSq/times)+' d
    ummy:'+str(dummySq/times))

```

ie

```

1. import numpy as np
2. from scipy.interpolate import griddata
3. import matplotlib.pyplot as plt
4. from sklearn.preprocessing import PolynomialFeatures
5. from sklearn.linear_model import Ridge
6.
7. #Code function is the same as (i)(b-c)
8. data = str(open("data").read()).split('\n')
9. dataset = []
10. for d in data[1:]:
11.     nums = d.split(',')
12.     dxy = []
13.     dxy.append(float(nums[0]))
14.     dxy.append(float(nums[1]))
15.     dxy.append(float(nums[2]))
16.     dataset.append(dxy)
17. dataset = np.array(dataset)
18.
19. x = dataset[:, 0]
20. y = dataset[:, 1]
21. z = dataset[:, 2]
22.
23. X_train = dataset.take([0, 1], axis=1)
24. y_train = dataset[:, 2]
25.
26. polyFeatures = PolynomialFeatures(degree=5)

```

```

27. print(polyFeatures.get_feature_names)
28. X_Poly = polyFeatures.fit_transform(X_train)
29. print(polyFeatures.get_feature_names())
30. ridgeR = Ridge(alpha=1)
31. ridgeR.fit(X_Poly, y_train)
32.
33. Xtest = []
34. grid = np.linspace(-1, 1)
35. for i in grid:
36.     for j in grid:
37.         Xtest.append([i, j])
38. Xtest = np.array(Xtest)
39. Xtest_poly = polyFeatures.fit_transform(Xtest)
40.
41. X_pre = ridgeR.predict(Xtest_poly)
42.
43. Xtest_x = Xtest[:, 0]
44. Xtest_y = Xtest[:, 1]
45.
46. xi = np.linspace(min(x), max(x))
47. yi = np.linspace(min(y), max(y))
48. X, Y = np.meshgrid(xi, yi)
49. Z = griddata((x, y), z, (X, Y), 'nearest')
50.
51. xitest = np.linspace(min(Xtest_x), max(Xtest_x))
52. yitest = np.linspace(min(Xtest_y), max(Xtest_y))
53. Xitest, Yitest = np.meshgrid(xitest, yitest)
54. Z_test = griddata((Xtest_x, Xtest_y), X_pre, (Xitest, yitest), 'nearest')
55.
56. fig = plt.figure(figsize=(12, 12))
57. ax = fig.add_subplot(projection='3d')
58.
59. ax.scatter(dataset[:, 0], dataset[:, 1], dataset[:, 2], label='training point')
60. Curve1 = ax.plot_surface(Xitest, Yitest, Z_test, rstride=1, cstride=1, color='r', label='predict with alpha=0.001', alpha=0.5)
61. Curve1._facecolors2d = Curve1._facecolor3d
62. Curve1._edgecolors2d = Curve1._edgecolor3d
63.
64. ridgeR2 = Ridge(alpha=50)
65. ridgeR2.fit(X_Poly, y_train)
66. X_pre2 = ridgeR2.predict(Xtest_poly)
67. Z_test2 = griddata((Xtest_x, Xtest_y), X_pre2, (Xitest, yitest), 'nearest')
68.
69. Curve2 = ax.plot_surface(Xitest, Yitest, Z_test2, rstride=1, cstride=1, color='b', label='predict with alpha=0.1', alpha=0.5)
70. Curve2._facecolors2d = Curve2._facecolor3d
71. Curve2._edgecolors2d = Curve2._edgecolor3d
72.
73. ridgeR3 = Ridge(alpha=1000)
74. ridgeR3.fit(X_Poly, y_train)
75. X_pre3 = ridgeR3.predict(Xtest_poly)
76. Z_test3 = griddata((Xtest_x, Xtest_y), X_pre3, (Xitest, yitest), 'nearest')
77.
78. Curve3 = ax.plot_surface(Xitest, Yitest, Z_test3, rstride=1, cstride=1, color='g', label='predict with alpha=1', alpha=0.5)
79. Curve3._facecolors2d = Curve3._facecolor3d
80. Curve3._edgecolors2d = Curve3._edgecolor3d
81.
82. ax.legend()
83. ax.set_xlabel('x-axis')
84. ax.set_ylabel('y-axis')
85. ax.set_zlabel('z-axis')
86. ax.set_title('The predicted surface varies with different alpha')
87. plt.show()

```

ie for compare

```
1. import numpy as np
2. from sklearn.model_selection import train_test_split
3. from sklearn.preprocessing import PolynomialFeatures
4. from sklearn.linear_model import Ridge
5. from sklearn.dummy import DummyRegressor
6. from sklearn.metrics import mean_squared_error
7.
8. data = str(open("data").read()).split('\n')
9.
10. dataset = []
11. for d in data[1:]:
12.     nums = d.split(',')
13.     dxy = []
14.     dxy.append(float(nums[0]))
15.     dxy.append(float(nums[1]))
16.     dxy.append(float(nums[2]))
17.     dataset.append(dxy)
18. dataset = np.array(dataset)
19.
20. x = dataset[:, 0]
21. y = dataset[:, 1]
22. z = dataset[:, 2]
23. X_train = dataset.take([0, 1], axis=1)
24. y_train = dataset[:, 2]
25.
26.
27.
28.
29. times = 100
30. modelSq, dummySq = 0, 0
31. for i in range(0, times):
32.     Xtrain, Xtest, ytrain, ytest = train_test_split(X_train, y_train, test_s
        ize=0.2)
33.     Xtrain_poly = PolynomialFeatures(degree=5).fit_transform(Xtrain)
34.     Xtest_poly = PolynomialFeatures(degree=5).fit_transform(Xtest)
35.     ridgeR = Ridge(alpha=1000).fit(Xtrain_poly, ytrain)
36.     dummy = DummyRegressor(strategy='mean').fit(Xtrain_poly, ytrain)
37.     ypred = ridgeR.predict(Xtest_poly)
38.     ydummy = dummy.predict(Xtest_poly)
39.     modelSq1 = mean_squared_error(ytest, ypred)
40.     dummySq1 = mean_squared_error(ytest, ydummy)
41.     print(modelSq1)
42.     print(dummySq1)
43.     modelSq = modelSq+modelSq1
44.     dummySq = dummySq+dummySq1
45.
46. print('square error: Ridge regression with alpha=1:'+str(modelSq/times)+' du
    mmy:'+str(dummySq/times))
```

ii-a-ii-b

```
1. import numpy as np
2. from sklearn.linear_model import Lasso
3. from sklearn.model_selection import cross_val_score
4. from sklearn.preprocessing import PolynomialFeatures
5. import matplotlib.pyplot as plt
6.
7. #Get data from file
8. data = str(open("data").read()).split('\n')
9. dataset = []
10. for d in data[1:]:
11.     nums = d.split(',')
12.     dxy = []
13.     dxy.append(float(nums[0]))
14.     dxy.append(float(nums[1]))
15.     dxy.append(float(nums[2]))
16.     dataset.append(dxy)
17. dataset = np.array(dataset)
18.
19. x = dataset[:, 0]
20. y = dataset[:, 1]
21. z = dataset[:, 2]
22. X_train = dataset.take([0, 1], axis=1)
23. y_train = dataset[:, 2]
24.
25.
26.
27.
28.
29. times = 100
30. modelSq, dummySq = 0, 0
31. for i in range(0, times):
32.     Xtrain, Xtest, ytrain, ytest = train_test_split(X_train, y_train, test_s
        ize=0.2)
33.     Xtrain_poly = PolynomialFeatures(degree=5).fit_transform(Xtrain)
34.     Xtest_poly = PolynomialFeatures(degree=5).fit_transform(Xtest)
35.     lassoR = Lasso(alpha=1000).fit(Xtrain_poly, ytrain)
36.     dummy = DummyRegressor(strategy='mean').fit(Xtrain_poly, ytrain)
37.     ypred = lassoR.predict(Xtest_poly)
38.     ydummy = dummy.predict(Xtest_poly)
39.     modelSq1 = mean_squared_error(ytest, ypred)
40.     dummySq1 = mean_squared_error(ytest, ydummy)
41.     print(modelSq1)
42.     print(dummySq1)
43.     modelSq = modelSq+modelSq1
44.     dummySq = dummySq+dummySq1
45.
46. print('square error: Lasso regression with alpha=1:'+str(modelSq/times)+' du
    mmy:'+str(dummySq/times))
```

```

12.     dxy = []
13.     dxy.append(float(nums[0]))
14.     dxy.append(float(nums[1]))
15.     dxy.append(float(nums[2]))
16.     dataset.append(dxy)
17. dataset = np.array(dataset)
18.
19. #Get an array of x, y, z
20. x = dataset[:, 0]
21. y = dataset[:, 1]
22. z = dataset[:, 2]
23.
24. #Generate training data and training target array
25. X_train = dataset.take([0, 1], axis=1)
26. y_train = dataset[:, 2]
27.
28. #Add polynomial
29. Xtrain_poly = PolynomialFeatures(degree=5).fit_transform(X_train)
30.
31. #Draw out the error bar
32. alpha = 0.001
33. alphas, means, stds = [], [], []
34. while alpha < 0.03:
35.     LassoR = Lasso(alpha=alpha)
36.     scores = cross_val_score(LassoR, Xtrain_poly, y_train, cv=5)
37.     alphas.append(alpha)
38.     means.append(scores.mean())
39.     stds.append(scores.std())
40.     alpha = alpha + 0.001
41.
42. plt.figure(figsize=(12,5))
43. plt.title('Lasso Regression error bar')
44. plt.xlabel('alpha')
45. plt.ylabel('mean accuracy')
46. plt.errorbar(alphas, means, stds, mfc='red')
47. plt.show()

```

ii-c

```

1. import numpy as np
2. from sklearn.linear_model import Ridge
3. from sklearn.model_selection import cross_val_score
4. from sklearn.preprocessing import PolynomialFeatures
5. import matplotlib.pyplot as plt
6.
7. #Code function is the same as (ii)(a)
8. data = str(open("data").read()).split('\n')
9. dataset = []
10. for d in data[1:]:
11.     nums = d.split(',')
12.     dxy = []
13.     dxy.append(float(nums[0]))
14.     dxy.append(float(nums[1]))
15.     dxy.append(float(nums[2]))
16.     dataset.append(dxy)
17. dataset = np.array(dataset)
18.
19. x = dataset[:, 0]
20. y = dataset[:, 1]
21. z = dataset[:, 2]
22.
23. X_train = dataset.take([0, 1], axis=1)
24. y_train = dataset[:, 2]
25. Xtrain_poly = PolynomialFeatures(degree=5).fit_transform(X_train)
26.

```

```
27.  
28. alpha = 0.01  
29. alphas, means, stds = [], [], []  
30. while alpha < 0.4:  
31.     RidgeR = Ridge(alpha=alpha)  
32.     scores = cross_val_score(RidgeR, Xtrain_poly, y_train, cv=5)  
33.     alphas.append(alpha)  
34.     means.append(scores.mean())  
35.     stds.append(scores.std())  
36.     alpha = alpha + 0.01  
37.  
38. plt.figure(figsize=(12, 5))  
39. plt.title('Ridge Regression error bar')  
40. plt.xlabel('alpha')  
41. plt.ylabel('mean accuracy')  
42. plt.errorbar(alphas, means, stds, mfc='red')  
43. plt.show()
```