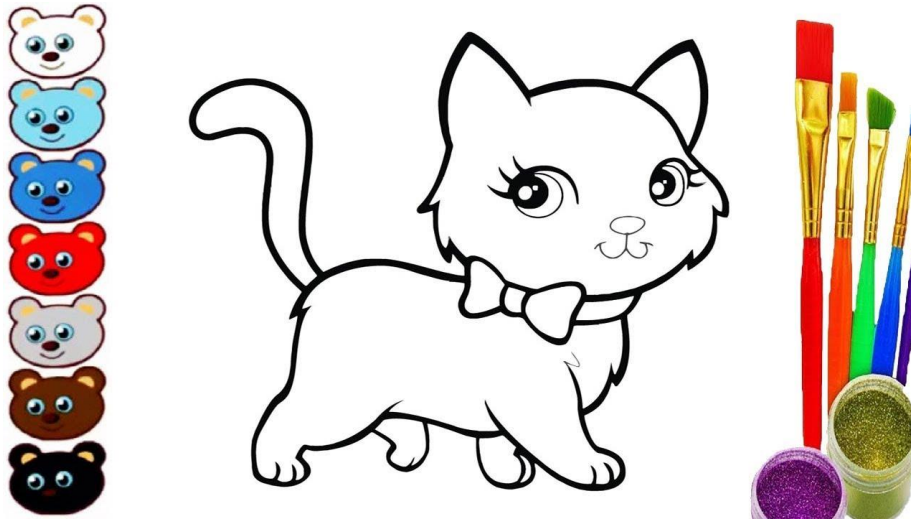


**1. The two input images are:**

(1) 1280x720.jpg

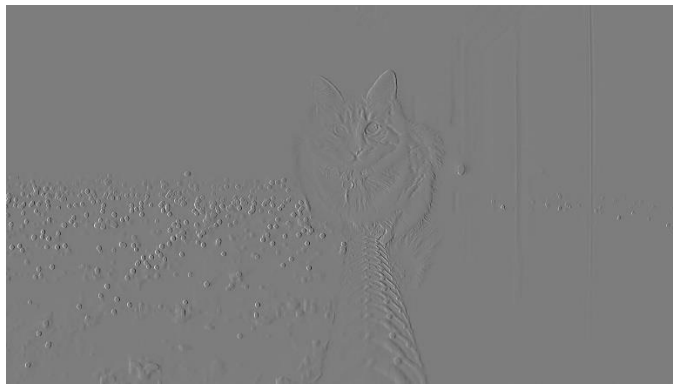
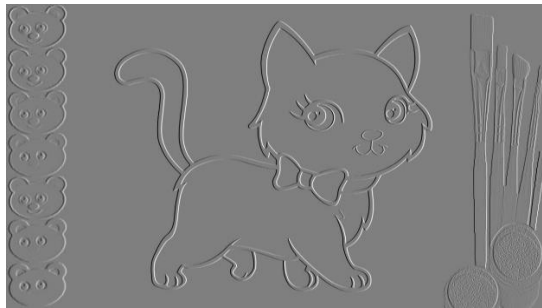


(2) 1920x1080.jpg



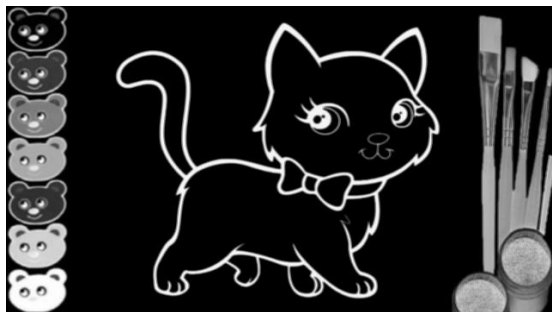
**2. Part A.**

(1) Results of task 1.

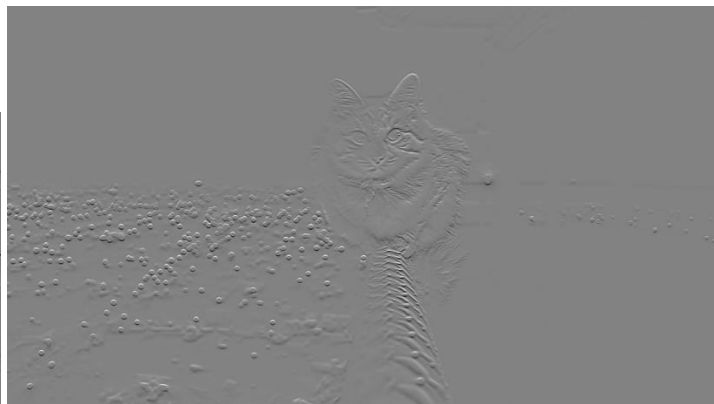


(2) Results of task 2

K4

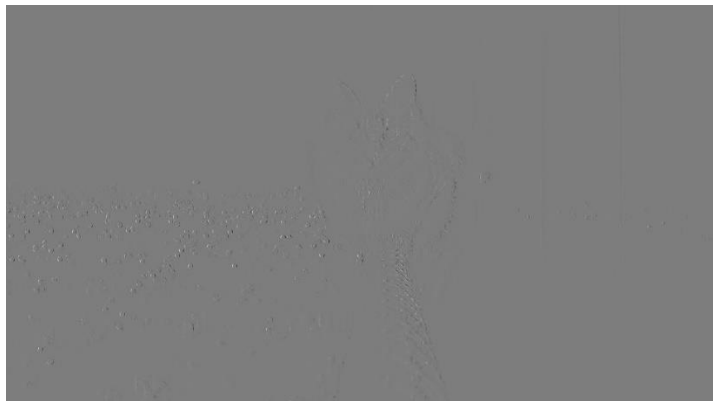
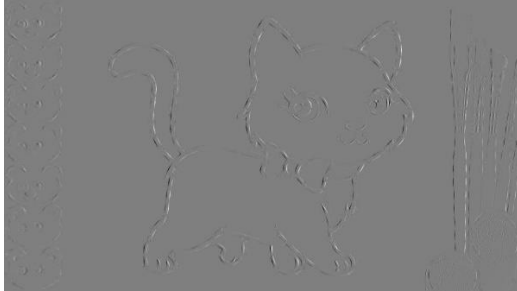


K5

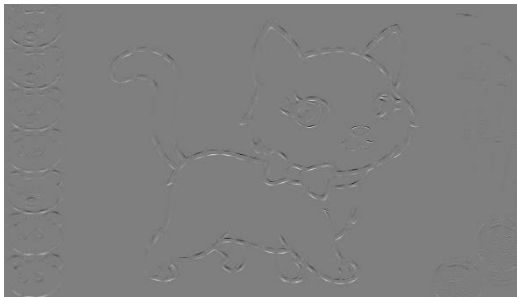


### (3) Results of task 3

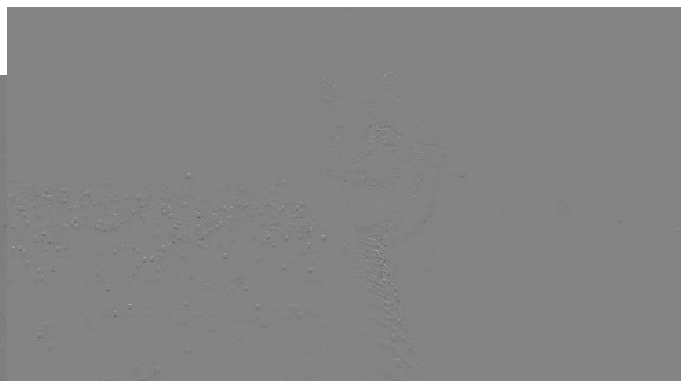
K1



K2

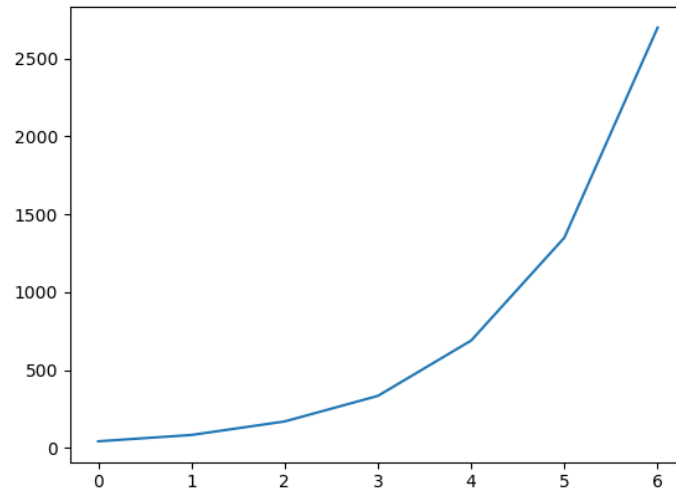


K3



### 3. Part B

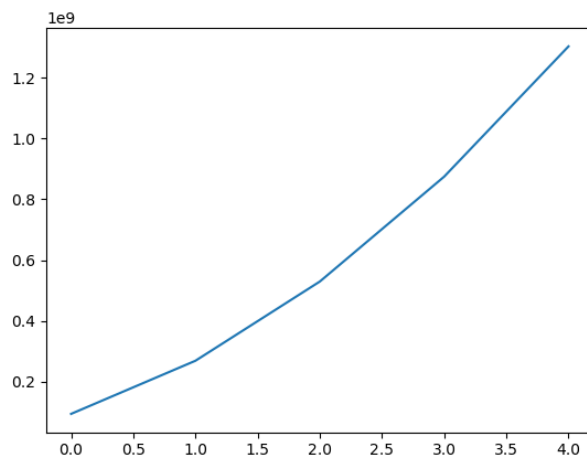
The time taken for performing each *forward()* as a function of  $i$  is shown as



Here,  $x$ -axis represents  $i$ ,  $y$ -axis represents the time taken (in seconds). Here only shows  $i \leq 6$  because  $i=7$  takes more than 1 hour to process (CPU only). We can see that with the increase of  $i$ , the time taken has improved a lot.

### 4. Part C

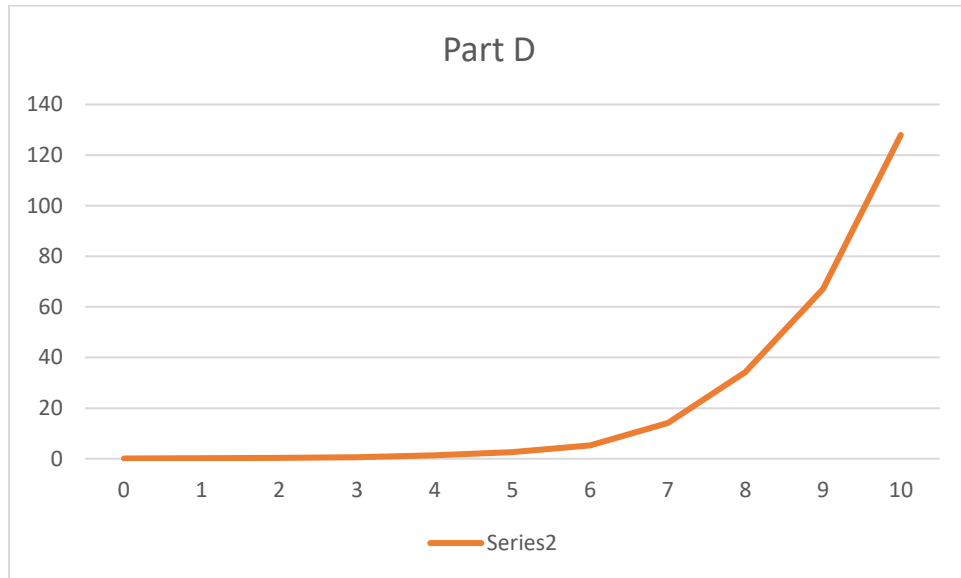
The number of operations used to perform convolution as a function of  $kernel\_size$  is



Here,  $x$ -axis should be 3, 5, ..., 11, representing  $kernel\_size$ ,  $y$ -axis represents the number of operations. We can see that with the increase of  $i$ , the time taken has improved a lot. In the code, each convolution operation has  $kernel\_size * kernel\_size$  of multiplications, and  $kernel\_size * kernel\_size - 1$  of additions.

### 5. Part D

Using C code, the time taken for performing each *forward()* as a function of  $i$  is shown as (plotted in excel)



We can see that it has the same trending as Part C. But much faster.

```

main.py

# perform 2d convolution

import torch

from PIL import Image

import torchvision.transforms as transforms

import torchvision

import matplotlib.pyplot as plt

import time


from conv import Conv2D


# convert PIL to tensor

pil2tensor = transforms.ToTensor()

tensor2pil = transforms.ToPILImage()


img_pil = Image.open('1280x720.jpg')

img = pil2tensor(img_pil) # convert JpegImageFile object to tensor


# task1

conv2d = Conv2D(in_channel=3, o_channel=1, kernel_size=3, stride=1, mode='known')

[numOperates, outImg] = conv2d.forward(img)

print(numOperates)

torchvision.utils.save_image(outImg, 'task1_1280x720.jpg', padding = 0, normalize = True)


if False:

    # task2

    conv2d = Conv2D(in_channel=3, o_channel=2, kernel_size=5, stride=1, mode='known')

    [numOperates, outImg] = conv2d.forward(img)

```

```

print(numOperates)

torchvision.utils.save_image(outImg[0], 'task2_1280x720_K4.jpg', padding = 0, normalize = True)

torchvision.utils.save_image(outImg[1], 'task2_1280x720_K5.jpg', padding = 0, normalize = True)

if False:

    # task3

    conv2d = Conv2D(in_channel=3, o_channel=3, kernel_size=3, stride=2, mode='known')

    [numOperates, outImg] = conv2d.forward(img)

    print(numOperates)

    torchvision.utils.save_image(outImg[0], 'task3_1920x1080_K1.jpg', padding = 0, normalize =
True)

    torchvision.utils.save_image(outImg[1], 'task3_1920x1080_K2.jpg', padding = 0, normalize =
True)

    torchvision.utils.save_image(outImg[2], 'task3_1920x1080_K3.jpg', padding = 0, normalize =
True)


# Part B

if False:

    timeB = torch.zeros([11, 1], dtype = torch.float64)

    for i in range(0,11):

        a = time.time()

        conv2d = Conv2D(in_channel=3, o_channel= 2**i, kernel_size=3, stride=1, mode='rand')

        [numOperates, outImg] = conv2d.forward(img)

        timeB[i] = time.time() - a

        print( str(i) + ': ' + str(timeB[i]) )


plt.plot(timeB)

plt.show()

```

# Part C

if False:

```
    numC = torch.zeros([5, 1], dtype = torch.int32)

    for i in range(0, 5):

        i

        a = time.time()

        conv2d = Conv2D(in_channel=3, o_channel= 2, kernel_size=(i+1)*2+1, stride=1,
mode='rand')

        [numOperates, outImg] = conv2d.forward(img)

        print('time is ' + str(time.time() - a) )

        numC[i] = numOperates

        print(numOperates)


plt.plot(numC)

plt.show()
```



```

conv.py

# perform 2d convolution

import torch

from PIL import Image

import torchvision.transforms as transforms

import matplotlib.pyplot as plt

import numpy as np


#Conv2D(in_channel, o_channel, kernel_size, stride, mode)


class Conv2D(object):

    def __init__(self, in_channel, o_channel, kernel_size, stride, mode):

        self.in_channel = in_channel

        self.o_channel = o_channel

        self.kernel_size = kernel_size

        self.stride = stride

        self.mode = mode


    def forward(self, input_image):

        def out_image(K, imgR, imgG, imgB, kernel_size, stride):

            [r, c] = imgR.size()

            d = int(kernel_size / 2)

            outR = torch.zeros([r-kernel_size+1, c-kernel_size+1], dtype = torch.float64)

            outG = torch.zeros([r-kernel_size+1, c-kernel_size+1], dtype = torch.float64)

```

```
outB = torch.zeros([r-kernel_size+1, c-kernel_size+1], dtype = torch.float64)
```

```
numCalulates = 0
```

```
for i in range(d, r-d, stride):
```

```
    for j in range(d, c-d, stride):
```

```
        blkR = imgR[i-d: i+d+1, j-d: j+d+1]
```

```
        outR[i-d, j-d] = (blkR * K).sum()
```

```
        blkG = imgG[i-d: i+d+1, j-d: j+d+1]
```

```
        outG[i-d, j-d] = (blkG * K).sum()
```

```
        blkB = imgB[i-d: i+d+1, j-d: j+d+1]
```

```
        outB[i-d, j-d] = (blkB * K).sum()
```

```
numCalulates = numCalulates + (K.size())[0] * K.size()[1]*2 -1)*3
```

```
outImg = (outR + outG + outB) / 3.0
```

```
return numCalulates, outImg
```

```
print(input_image.size())
```

```
imgR = input_image[0]
```

```
imgG = input_image[1]
```

```
imgB = input_image[2]
```

```
[r, c] = imgR.size()
```

```
# output image
```

```
        outImg = torch.zeros(self.o_channel, r-self.kernel_size+1, c-self.kernel_size+1) # output
        grayscale image
```

```
    # Part B
```

```
    if(self.kernel_size == 3 and self.mode == 'rand' and self.stride == 1):
```

```
        numOperates = 0
```

```
        for i in range(0, self.o_channel):
```

```
            Kb = torch.rand(3,3) *2 -1 # in range [-1, 1]
```

```
            [numCalulates, outImg1] = out_image(Kb, imgR, imgG, imgB,
self.kernel_size, self.stride)
```

```
            numOperates = numOperates + numCalulates
```

```
            outImg[i] = outImg1
```

```
        return numOperates, outImg
```

```
    # Part C
```

```
    #if False:
```

```
    elif(self.o_channel == 2 and self.mode == 'rand' and self.stride == 1):
```

```
        Kc1 = torch.rand(self.kernel_size, self.kernel_size) *2 -1
```

```
        Kc2 = torch.rand(self.kernel_size, self.kernel_size) *2 -1
```

```
        numOperates = 0
```

```
        [numCalulates, outImg1] = out_image(Kc1, imgR, imgG, imgB, self.kernel_size,
self.stride)
```

```
        outImg[0] = outImg1
```

```
        numOperates = numOperates + numCalulates
```

```
        [numCalulates, outImg1] = out_image(Kc2, imgR, imgG, imgB, self.kernel_size,
self.stride)
```

```
outImg[1] = outImg1  
numOperates = numOperates + numCalulates
```

```
return numOperates, outImg
```

```
# task 1
```

```
elif(self.o_channel == 1 and self.kernel_size == 3 and self.mode == 'known' and  
self.stride == 1):
```

```
numOperates = 0
```

```
K1 = torch.tensor([[-1., -1., -1.], [0., 0., 0.], [1., 1., 1.]])
```

```
K1 = K1.transpose(0, 1)
```

```
[numOperates, outImg1] = out_image(K1, imgR, imgG, imgB, self.kernel_size,  
self.stride)
```

```
outImg = outImg1
```

```
return numOperates, outImg
```

```
# task 2
```

```
#if False:
```

```
elif(self.o_channel == 2 and self.kernel_size == 5 and self.mode == 'known' and  
self.stride == 1):
```

```
K4 = torch.tensor([[-1., -1., -1., -1., -1.], [-1., -1., -1., -1., -1.], [0., 0., 0., 0., 0.], [-1.,  
-1., -1., -1., -1.], [-1., -1., -1., -1., -1.]])
```

```
K4 = K4.transpose(0, 1)
```

```
K5 = torch.tensor([[-1., -1., 0., 1., 1.], [-1., -1., 0., 1., 1.], [-1., -1., 0., 1., 1.], [-1., -  
1., 0., 1., 1.], [-1., -1., 0., 1., 1.]])
```

```
K5 = K5.transpose(0, 1)
```

```

numOperates = 0

self.stride)
[numCalulates, outImg1] = out_image(K4, imgR, imgG, imgB, self.kernel_size,

outImg[0] = outImg1
numOperates = numOperates + numCalulates

self.stride)
[numCalulates, outImg1] = out_image(K5, imgR, imgG, imgB, self.kernel_size,

outImg[1] = outImg1
numOperates = numOperates + numCalulates

return numOperates, outImg

```

# task 3

#if False:

```

elif(self.o_channel == 3 and self.kernel_size == 3 and self.mode == 'known' and
self.stride == 2):

```

```

K1 = torch.tensor([[-1., -1., -1.], [0., 0., 0.], [1., 1., 1.]])

```

```

K1 = K1.transpose(0, 1)

```

```

K2 = torch.tensor([[-1., 0., 1.], [-1., 0., 1.], [-1., 0., 1.]])

```

```

K2 = K1.transpose(0, 1)

```

```

K3 = torch.tensor([[1., 1., 1.], [1., 1., 1.], [1., 1., 1.]])

```

```

K3 = K1.transpose(0, 1)

```

```

numOperates = 0

```

```
self.stride)    [numCalulates, outImg1] = out_image(K1, imgR, imgG, imgB, self.kernel_size,

outImg[0] = outImg1

numOperates = numOperates + numCalulates

self.stride)    [numCalulates, outImg1] = out_image(K2, imgR, imgG, imgB, self.kernel_size,

outImg[1] = outImg1

numOperates = numOperates + numCalulates

self.stride)    [numCalulates, outImg1] = out_image(K3, imgR, imgG, imgB, self.kernel_size,

outImg[2] = outImg1

numOperates = numOperates + numCalulates

return numOperates, outImg
```

main.c

// perform 2d convolution. Output channel  $2^i$  ( $i=0,1,\dots,10$ )

#include <stdio.h>

#include <time.h>

#include <math.h>

int c\_conv(int in\_channel, int o\_channel, int kernel\_size, int stride)

{

int height = 1280;

int width = 720;

size\_t nbytes = height \* width \* in\_channel \* sizeof(char);

int i, j, k, m, n, p;

double val;

long int row;

int num = 0;

// simulate input image as all black

char \*input\_img = (char\*)malloc(nbytes);

memset(input\_img, 0, nbytes);

char \*out\_img = (char \*)malloc((height - 1) \* (width - 1) \* sizeof(char));

memset(out\_img, 0, (height - 1) \* (width - 1) \* sizeof(char));

double \*k1 = (double\*)malloc(kernel\_size\*kernel\_size\*sizeof(double));

for (m = 0; m < o\_channel; m++)

{

```

// randomly generate kernel
for (p = 0; p < kernel_size * kernel_size; p++)
    k1[p] = rand() / (2.0) - 1;

for (i = 1; i < height - 1; i++)
    for (j = 1; j < width - 1; j++)
    {
        val = 0.0;
        row = i * width + j;

        for (n = 0; n < in_channel; n++)
        {
            val += input_img[(row - width - 1) * in_channel + n] * k1[0] + input_img[(row - width) *
in_channel + n] * k1[1] + input_img[(row - width + 1) * in_channel + n] * k1[2] +
            input_img[(row - 1) * in_channel + n] * k1[3] + input_img[(row) * in_channel + n] * k1[4] +
input_img[(row + 1) * in_channel + n] * k1[5] +
            input_img[(row + width - 1) * in_channel + n] * k1[6] + input_img[(row + width) *
in_channel + n] * k1[7] + input_img[(row + width + 1) * in_channel + n] * k1[8];
        }

        out_img[(i - 1) * (width - 1) + j - 1] = val / (double)in_channel;
        num += (kernel_size * kernel_size * 2 - 1) * in_channel;
    }
}

return num;
}

```

```

void main()
{
    int o_channel[11]; // output channels

```



```

        clock_t t;

        double times[11];

        double val; // value storing convolution results
int in_channel = 3, kernel_size = 3, stride = 1;
int numOperates;
int num;
int k;


        for (k = 0; k < 11; k++)
        {
                o_channel[k] = pow(2, k); // # of output channels
printf("%d: ", o_channel[k]);
numOperates = 0;


                // do 2d convolution
                t = clock();
num = c_conv(in_channel, o_channel[k], kernel_size, stride);
numOperates += num;


                times[k] = (clock() - t) / (double)CLOCKS_PER_SEC;


                printf("%f\n", times[k]);
        }
}

```