

IMPLMENTING A INTERPRETER FOR A SCRIPTING LANAGUGE USING HASKELL

FINAL YEAR PROJECT REPORT

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Abstract

In this thesis,

 ${\bf Keywords:} programming \ language \ {\tt YUN}$

Declaration

I Zhen Lao hereby declare that the work described in this dissertation is, except where otherwise stated, entirely my own work and has not been submitted as an exercise for a degree at this or any other university.

Signed		
	Zhen Lao	

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Chapter 1

Introduction

1.1 Objective and Motivation

The objective of this project is to develop a dynamic and weak typing interpreted language using Haskell. This language is able to support the following features,

- basic for loop and while loop
- basic if-else statement
- functional invocation
- arbitrary dimension list
- polymorphic list

Furthermore, in this project, the monadic design approach is applied as Haskell is different from other object oriented language.

1.2 Benefits of using Haskell

Haskell is an advanced purely-functional programming language. By applying the used of Haskell to this project ,I have significantly reduce the coding time and spent most of my time to the design phrase.

A pure function is a function that accepts an input and produce an output. In Object-Oriented language, program is constructed using classes and instances which encapsulate computations and states. Haskell program is constructed by functions as function is the first class member in Haskell. Typically the

main function is defined in terms of other functions, which in turn are defined in terms of still more functions, until at the bottom level the functions are language primitives. All of these functions are much like ordinary mathematical functions. [Why Functional Programming Matters] [Functional Programming with Overloading and Higher-Order Polymorphism]

1.3 Development Methodology

Agile development methodology is used in the entire development process. This project has been initially identified to multiple iterations and each iteration contains three major phrases inducing research ,development and testing.

Researches have been done on investing some useful Haskell library like Parsec ,Happy,Alex and HUnit.

Eclipse with EclipseFP plugin provide support for source code and package management in Eclipse. To keep tract of the development process, I make use of **git** a source control tool to version all the source file.

1.4 Code Formats

In this thesis, two types of code will be listed in different formats.

Code listed without line numbers illustrates the design of the interpreter or other Haskell concept. Most of it are Haskell code, which looks like,

```
return a >>= k == k a
m >>= return == m
m >>= (\x -> k x >>= h) == (m >>= k) >>= h
```

Code listed with line numbers are example of **yun** ,the programming language designed in this project.It looks like,

```
program main () {
    result = fib (10);
    sys.printLn(result);

function fib (num) {
    if (num ==0) {
        return 1;
    }
    if (num == 1) {
    return 1;
}
```

```
part1 = fib (num-1);
part2 = fib (num-2);
return (part1+part2);
}
```

Chapter 2

Compiler and Interpreter Technologies

2.1 Parsing technologies

2.1.1 Formal Grammar

Mathematically, formal grammar consists of:

- a finite set of terminal symbols.
- a finite set of non-terminal symbols.
- a finite set of project rules.
- a start symbol.

[?] [Three Models for the Description of Language] From the formal grammar definition, legitimate production rules can be written as

$$S \mapsto aS \ and \ S \mapsto ab$$

In this example, we can assume that the grammar consists of two projection rules and the starting symbol is S. The terminal symbols are lower letters $\{a,b\}$. From this example, If we start from the either rule 1 or rule 2 ,we could derive a grammar of $\{a^nb|n>1\}$, which can be enumerate like $\{aab, aaab, aaaab, \cdots\}$.

2.1.2 Context-Free Grammar

Context-Free Grammar (CFG) A context-free grammar is has four component 1. A set of terminal symbols, sometimes referred to as "tokens." The

terminals are the elementary symbols of the language defined by the grammar. 2. A set of non-terminals, sometimes called "syntactic variables." Each non-terminal represents a set of strings of terminals, in a manner we shall describe. 3. A set of productions, which are rules for replacing (or rewriting) non-terminal symbols (on the left side of the production) in a string with other non-terminal or terminal symbols (on the right side of the production). 4. A start symbol, which is a special non-terminal symbol that appears in the initial string generated by the grammar. [?] Context-free grammar can be recognized by pushdown automaton.

2.1.3 The Hierarchy of Grammars

Noam Chomsky has describe three model of grammar ["Three models for the description of language"] and this grammar model has significantly effect the design of computer programming language.

Chomsky define a set of rule upon the formal grammar and categorize them into different levels.

The Chomsky hierarchy consists of the 4 levels:

- Type-0 grammars (unrestricted grammar). It is a unrestricted grammars that include all possible grammar that are possible to recognize by Turning machine.
- Type-1 grammars (context-sensitive grammar).if all rules are of the form $\alpha A\beta \to \alpha \gamma \beta$ where $\alpha \beta \gamma$ are terminal symbols and A is non-terminal symbol.
- Type-2 grammars (context-free grammar).
- Type-3 grammars (regular grammar).

2.1.4 Backus–Naur Form and Extended Backus–Naur Form

The Backus-Naur Form(BNF) is a metalanguage to write the production rule that expressing the type-2 grammar (context-free grammar). It restricts the appearance of terminal and non-terminal in each side of the production equation. A canonical BNF production rule may like follow,

$$< symbol > ::= _expression_$$

The left side of the equation can only be non-terminal thus enclosed with <> .The right hand side can be terminals and non-terminals, a vertical bar

'—' is used to represent choice between terminal and non-terminals.

The Extended Backus–Naur Form (EBNF) and extension upon the BNF. Three regular expression qualifier is added to simplified some expression, they are,

- ? : which means that the symbol (or group of symbols in parenthesis) to the left of the operator is optional (it can appear zero or one times)
- *: which means that something can be repeated any number of times (and possibly be skipped altogether)
- +: which means that something can appear one or more times

[?]

Recrusive rules of BNF like

$$1. < exp > := < exp > |sub$$
$$2. < exp > := sub$$

that expressing a sequence of a particular syntactic element can be simplified using quantifier in EBNF as $\langle exp \rangle := sub +$

2.2 Parser Generator Haskell Happy

Happy is a parser generator system for Haskell, similar to the tool 'yacc' for C. Like 'yacc', it takes a file containing an annotated BNF specification of a grammar and produces a Haskell module containing a parser for the grammar. [The Parser Generator for Haskell]

By using its own EBNF like syntax, used could write an parser description. The happy parser generator are able to recognize and compile it into Haskell source code.

2.3 Monadic Parsing using Parsec

In the early stage of this project, parse is build using parse C, Parsec is an industrial strength, monadic parser combinator library for Haskell. It can parse context-sensitive, infinite look-ahead grammars but it performs best on predictive (LL[Compilers: principles, techniques and tools.]) grammars. Combinator parsing is well known in the literature and offers several advantages to YACC or event-based parsing. [Parsec, a fast combinator parser]

Compared toe parser generator, monadic parsing has two major benifits 1. No need to learn additional parser generator grammar since parser combinator is written in the same language. 2.parser can be adjust easily.

2.4 Lexical analysis

Before parsing, the lexical analyser will scan the source code and generate a sequence of tokens. The tokens are often defined by regular expressions.

For example, the statement s3 = s1 + "a string" will be parse to tokens,

s3	identifier ,variable name
=	operator
s1	identifier, variable name
+	opeartor
"a string"	a string constant

The regular expression $[a-zA-Z]1[a-zA-Z \setminus 0-9]*$ can identify strings that begin will alphabetical character.

2.4.1 The Lexer Generator Alex

Alex is a tool for generating lexical analysers in Haskell, given a description of the tokens to be recognised in the form of regular expressions. It is similar to the tools lex and flex for C/C++.

Alex takes a description of tokens based on regular expressions and generates a Haskell module containing code for scanning text efficiently. Alex is designed to be familiar to exisiting lex users, although it does depart from lex in a number of ways. [Alex User Guide]

Chapter 3

Monads

- 3.1 Overview
- 3.1.1 Side effect
- **3.1.2** Monad

3.2 Haskell and Category Theory

Category theory is a general theory that examine and organize mathematical object like set ,function,function domains Cartesian-set.

A Category C in category theory is defined below:

- 1. a collection of objects
- 2. a collection of arrows (often call morphism)
- 3. operations assigning to each arrow f an object $dom\ f$, its domain , and an object $cod\ f$, its co domain.
- 4. a composition operator assigning to each pair of arrows fandg,with $cod\ f = dom\ g$,a composite arrow $g \circ f: dom\ f \to cod\ g$, satisfying the following associative law:

For any arrow $f: A \to B, g: B \to C, and h: C \to D$ (with A,B,C and D not necessarily distinct),

$$h \circ (g \circ f) = (h \circ g) \circ f$$

5. for each object A, an identify arrow $id_a: A \to A$ satisfying the following identity law:

For any arrow $f: A \to B$,

$$id_a \circ f = f \text{ and } f \circ id_a = f.$$

[?]

Category in Haskell

In Haskell, all the type in can be view as objects and all the function can be view as arrows.id function has been defined as follow.

It can be viewed as an identify arrow of all objects(types).

Functor in Haskell

Some high order function like fmap can be view as a functor.

From its signature we know that fmap maps arrows in category to another category.f a is the type constructor that takes a as its parameter an generate f a as a new type.So it maps the arrow from a - > b to f a - > f b.

Its instances types like Maybe and ReadP satisfy the functor law:

Functions are the first member of the program in functional programming, since no size affect is not allow , there should be a way to combine the all kinds of functions to from a new function instead of just simply chain the input output of each function as the former will generate intermediate output.

For instance, counting the file of java source code in current directory can be written as follow:

$$ls - al. | arep * .txt | wc - l$$

To substantiate the this concept , let's use the map/fold fusion technique of Haskell as an example.

If we want to calculate the sum of the square of each element of a list eg. [1,3,4,6,7,9], the result of it is $1^2 + 3^2 + 4^2 + 6^2 + 7^2 + 9^2 = 192$. In Haskell ,we could use map and fold to address problem.

To avoid generating intermediate output from the first function to second function, the could rewite the hold function using a single fold

```
The all map/fusion is is equivalent to foldrfe.mapg = foldr(xy->f(gx)y)e
therefore, the sum_o f_s quare = foldr(xy->x^2+y)0
```

3.3 Monadic Function

3.3.1 Data Type Constructor

3.3.2 Monadic Function

A monadic function is function that produce, however, monadic function like putStr :: String -> IO () can not be combined using (.) :: (b -> c) -> (a -> b) -> a -> c. Monadic class constructor has tag

3.4 Monads

In Haskell, monad is used an abstract data type constructor to represent multiple kinds of computation such as a computation that will do IO action, or a computation that has state. Those computations are in-pure because that manipulate the outside world. In Haskell. Mathematically, monads are governed by set of laws that should hold for the monadic operations [A Gentle Introduction to Haskell, Version 98]. There are two basic law in monads , they are bind return . The Monad class is defined as follow:

```
class Monad m where
  (>>=) :: m a -> (a -> m b) -> m b
  (>>) :: m a -> m b -> m b
  return :: a -> m a
  fail :: String -> m a
```

The return function can inject a value into monadic type. The bind function can combine two monadic function, one should be of type ${\bf m}$ a and another should be of type ${\bf a}$ -> ${\bf m}$ ${\bf b}$.

Beside this two function, Haskell also provide other monadic operator which all derive from **return** and **bind**, they are:

```
liftM :: (Monad m) => (a1 \rightarrow r) \rightarrow m \ a1 \rightarrow m \ r
liftM2 :: (Monad m) => (a1 \rightarrow a2 \rightarrow r) \rightarrow m \ a1 \rightarrow m \ a2 \rightarrow m \ r
```

```
ap :: (Monad m) => m (a -> b) -> m a -> m b
(=<<) :: (Monad m) => (a -> m b) -> m a -> m b
\$ ::(m a -> m b) -> m a -> m b
```

These monadic operation is define using the bind and return. For example ,liftM is defined by bind and return like

```
liftM f m1 = do \{ x1 \leftarrow m1; return (f x1) \}
```

Therefore, when defining a monad, only bind and return need to be specified.

Monadic Characteristic

For all monad instance ,beside define three monadic operator ,they must apply three compulsory monad laws:

```
"Left identity": return a >>= f \equiv f a "Right identity": m >>= return \equiv m "Associativity": (m >>= f) >>= g \equiv m >>= (\x -> f x >>= g)
```

In monad instance ,these monad laws will become a restriction of the operation when combining monadic function using monadic operation, these restriction will be discussed in following sections.

3.4.1 IO Monad

Haskell use IO monad to limit the IO sequence. Monadic operation are used to represent IO processing pipeline, One significant different between IO monad an other monad is that it does not provide escape function like

```
IO String ->String
```

3.4.2 State Monad

The State Monad is defined as follow

```
newtype State s a = State {runState :: s -> (a, s)}
```

3.4.3 List Monad

Haskell try to use list monad to represent a calculation that return multiple result.

3.5 Using Monad Operator to Combine Monadic Function

3.6 Type system in Haskell

3.7 Do Notation

The do notation is a syntax sugar to write monadic operation especially bind in a imperative way ,to be more specified, only monadic function with the same return type can write together. An IO action that return ${\bf IO}$ () can not put with and state monadic function that return ${\bf State}\ {\bf s}\ {\bf a}$.

To write a get line and put line logic using bind, the sequence of IO is guaranteed by monad laws.

```
getLine >>= (\x -> putStrLn x)
```

Following code shows that the same functionalities are written using donotation, which shows a strong similarity to a imperative language.

```
do line <- getLine
  putStrLn line</pre>
```

Chapter 4

Monad Transformers

Monad transformers offer an additional benefit to monadic programming: by providing a library of different monads and types and functions for combining these monads, it is possible to create custom monads simply by composing the necessary monad transformers. [Monad Transformers Step by Step]

4.1 State Transformer

A value of type (ST a s) is a computation which transforms a state index by type s ,and delivers a value of type a ,You can think of it as a box ,like this

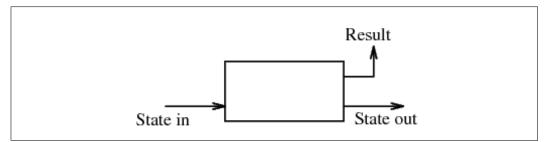


Figure 4.1: Diagram illustrating a state monad

[lazy functional state thread]

4.2 Error Transformer

4.3 Putting All Together

Chapter 5

Language Interpreter Design

5.1 Architecture

the interpreter contains two part, the parser and the execution engine. the parser will parse the source code into a parser tree, the execution engine will then execute the code according to the parser tree.

5.1.1 Parser

the parser that the source code as input and generate a tree structure as output.

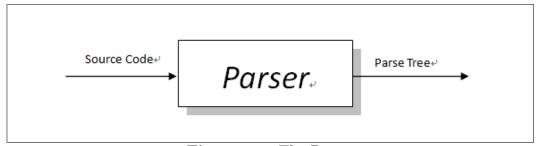


Figure 5.1: The Parser

the parser will contains different type of automata so that it could recognize different types of grammar.the grammar using to design the language is content-free grammar. the parser was build by combine simple and atomic parsers. The parser can be view as a function that a parser is a function that takes a string of characters as its argument, and returns a list of results. [?]

5.1.2 The Execution Engine

The execution engine of the parser is basic on Haskell.the execution engine will accept a parse tree and execute the command basic on this parse tree.

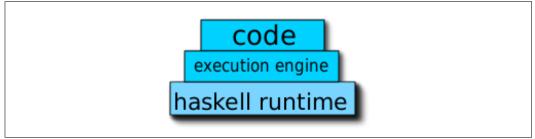


Figure 5.2: The Parser

5.2 Imperative and Declarative language

5.3 Type System

5.3.1 Dynamic Typing and Static Typing

A programming language is said to use static typing when type checking is performed during compile-time as opposed to run-time. For example, you have to specify the type explicitly and the compile will the type correctness of a variable. A variable of a specified type can not assign to another value of other type.

outer to the control of por	
Static Typing	Dynamic Typing
int $a = 1$;	a=1;
/*a is of type int */	/* does not need to
int a="a string";	specified a type for this
/* its not valid to as-	variable */
sign a string to a vari-	a ="a string";
able that has type int $*/$	/* it valid to change the
	type of the variable */

In my project, I used the dynamic typing scheme, which is ,does not need to specify any type of variable and able to assign any type of primitives to a variable.

5.3.2 Strong Typing and Weak Typing

a language is said to be strong typing is that it place restriction in operation where data type can not be intermix.

Strong Typing	Weak Typing
a=123;	a = 123;
/* a is a number */	b = "123";
b="123"	c = a+b;
/* b is a string */	a = 123; b = "123"; c = a+b; /* either a will be convert to
c=a+b /* return type error */	a string or b will be convert
	to a number */

In my project, I have implemented a weak typing system . I have design an statement call generic expression, which allow different kinds of value to intermix with each other. An expression like "12343" + 1232 -324 can be parse as follow syntax tree.

5.4 Problem and resolution in writing BN-F/EBNF rules

For a parser, there are four operation it will do when encounters a terminal/non-terminal symbol. They are,

- Shift push token onto stack
- Reduce remove handle from stack and push on corresponding nonterminal
- Accept recognize sentence when stack contains only the distinguished symbol and input is empty
- Error happens when none of the above is possible; means original input was not a sentence

Conflicts arise from ambiguities in the grammar when two or more operations and rules that apply to the same sequence of input.[A final solution to the Dangling else of ALGOL 60 and related languages]

5.4.1 Shift//Reduce Problem

A shift conflict occurs if there are two or more rules that apply to the same sequence of input for the same operation reduce. This usually indicates a serious error in the grammar.

5.4.2 Reduce//Reduce Problem

A reduce/reduce conflict occurs if there are two or more rules that apply to the same sequence of input for the same operation reduce. This usually indicates a serious error in the grammar.

5.5 Syntax Design

5.5.1 The Main Structure

A module is the minimum executable unit in **yun**.It is composed by one main function and serveral functions. The main function is a entry point, it may invoke other functions.

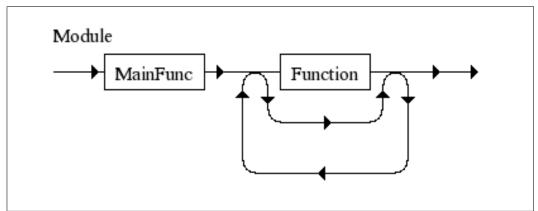


Figure 5.3: Module Syntax Diagram

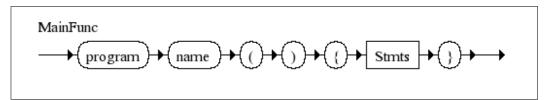


Figure 5.4: Main Function Syntax Diagram

Possible program code may looks like follow,

```
program main ()

result = sum(1,2,3);

main ()

result = code

main ()

result = sum(1,2,3);

main ()

main ()

result = sum(1,2,3);

main ()

main ()

result = sum(1,2,3);

main ()

main ()

main ()

result = sum(1,2,3);

main ()

main ()

main ()

result = sum(1,2,3);

main ()

main ()
```

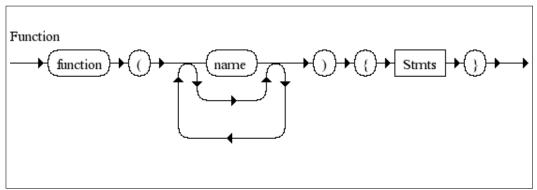


Figure 5.5: Function Syntax Diagram

5.5.2 Statements

Statements comprise the body of a function. A statement may be a assignment, break and continue sentence, return sentence. WhileBlocks, IfBlocks, ForBlocks are all statements. What's more, WhileBlock, IfBlock, ForBlock are recursively defined by statements as well. This allow nested for loop, nested while loop and etc.

The following code can be consider as a statement of the language

```
1 while
2 {
3 } /* the while statement */
4
5 if ()
6 {
7 }
8 else
9 {
10 } // the if else statement
11
12 for ()
```

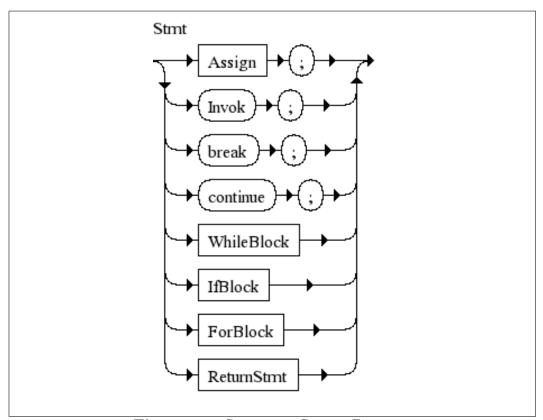


Figure 5.6: Statement Syntax Diagram

Assignment

There are three type of assignment in the language .They are ,

• Function invocation assignment. Assign the return result to a variable.

- Generic expression assignment. Assign the result of an expression to a variable.
- List assignment. Assign a list to a variable.

As **yun** is an imperative language, the right side of the assignment operator will be evaluation immediately. In other word, the language is strict.

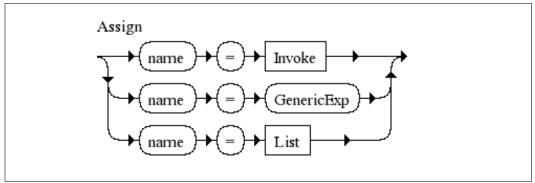


Figure 5.7: Assign Statement Syntax Diagram

5.5.3 Generic Expression

Generic expression represent the computation between primitives. As mention above, **yun** is a weak typing and dynamic typing language, the generic expression accepts variant types of primitive and will do the conversion internally.

Valid expression could be ,

```
1 "string"
2 1
3 -10
4 1.1
5 True
6 False
7 True
8 False // primitives
9
10 1 + "a string"
11 1 * 2 + 1
12 a && b
13 a || b
14 ! a
15 a[2] //get the third element of a list
```

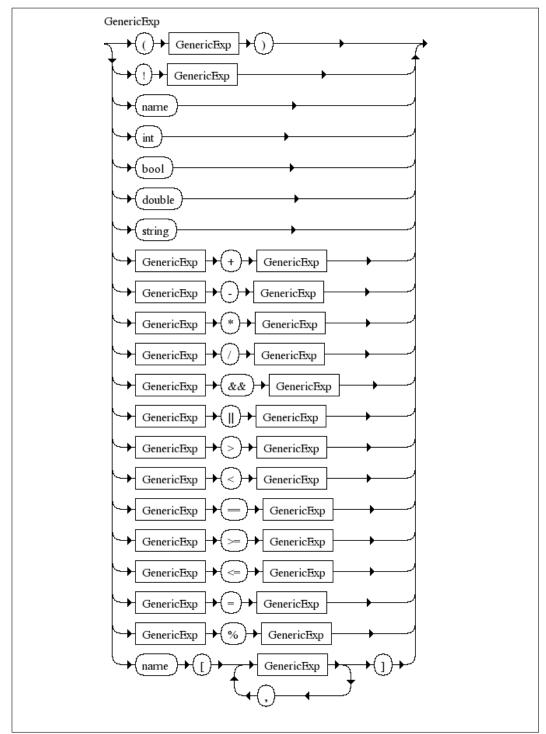


Figure 5.8: Expression Syntax Diagram

```
16 {f a}[1,2] // get the element in a multi dimension list 17 18 {f (a+b)+c} // operation between variables 19 {f a}[{f num}]
```

List

The language support polymorphic list, the element of a list can be an expression or an list, thus the list support multi dimension list. If the element is an expression, the interpreter will evaluate it and store its result value in its internal format.

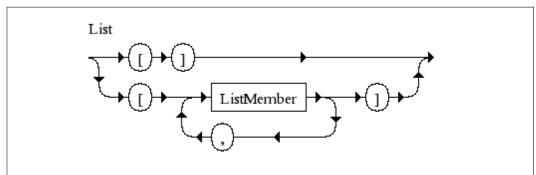


Figure 5.9: Expression Syntax Diagram

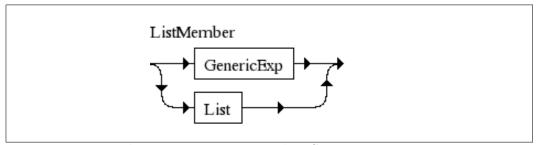


Figure 5.10: List Member Syntax Diagram

Code Example

```
1 a = [1,2,3];
2 a = ["string",1,2,3];
3 a = [var1,var2,"other",var1+var2,True&&False];
4 a = [[1,2,3,4,5,6,7] , 1, 23.32, 5];
5 a = [1,2,3,4,5],[1,2,3,4],[3,45,43]]; // declare a multi dimension list
6
7 member = a[1] // get the second element of a list
```

5.5.4 Code Block

Code blocks including if block, while block and for block are statements. Code block may contains other statements which allow nested code block to be defined.

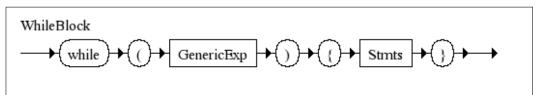


Figure 5.11: While Block Syntax Diagram

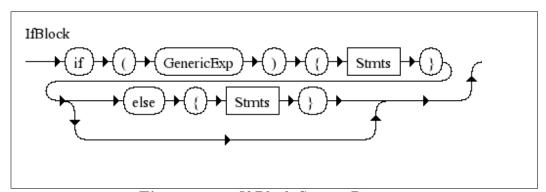


Figure 5.12: If Block Syntax Diagram

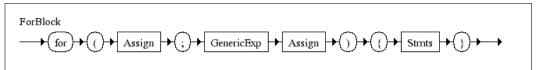


Figure 5.13: for Block Syntax Diagram

Code Example,

Chapter 6

Language Implementation

6.1 Data Type

6.1.1 Tokenizer Type

All tokens are define using the Haskell Lexer Generator Alex. Tokens will be recognized and converted to Haskell data types. For example , a valid variable is comprised with one or more alphabetic characters and digit and the first character must be an alphabetic characters. This rule can be defined as ,

The variable var1 will be parse into Haskell data type TName "var1"

By using the lexer, all the code will be generated into tokens streams.

```
\begin{array}{lll} & \text{program myProgram ()} \\ & & \\ & 2 & \\ & 3 & & \mathbf{var1} = 1; \\ & & & \mathbf{result} = \mathbf{var1} \, + \, \texttt{"a string"}; \\ & & 5 & \end{array}
```

The following codes show the invocation of the lexer and the returned tokens stream.

```
1 lexer "program myProgram() { var1 = 1; result = var1 +
False; return 0; }"
2 [TProgram,TName "myProgram",TOPB,TCPB,TOCB,TName
    "var1",TAssign,TInt 1,TSC,TName "result",TAssign,TName
    "var1",TPlus,TBool False,TSC,TReturn,TInt 0,TSC,TCCB]
```

6.1.2 Parser internal data type

The Parser internal data type typically represents a parse tree. To represent a generic expression, we can define data type as follow,

 $_{1}$ (a +1) /= 3 $_{2}$ myArray [1+1,2]

are parsed into Haskell data structure,

```
NotEq (Brack ( Plus (Var "a") (Int 1))) (Int 3) ListIndex "myIndex" [ Plus (Int 1) (Int 1) , Int 2 ]
```

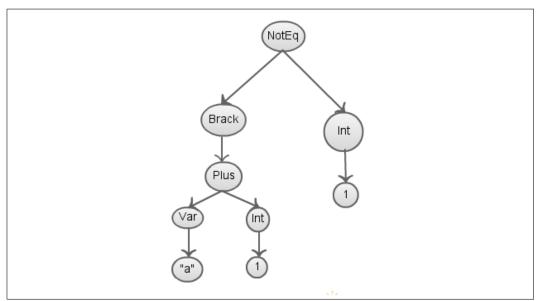


Figure 6.1: Diagram illustrating a parse tree of a generic expression

In Haskell, a parse tree data structure that support polymorphic list can be defined using recursive data type as follow,

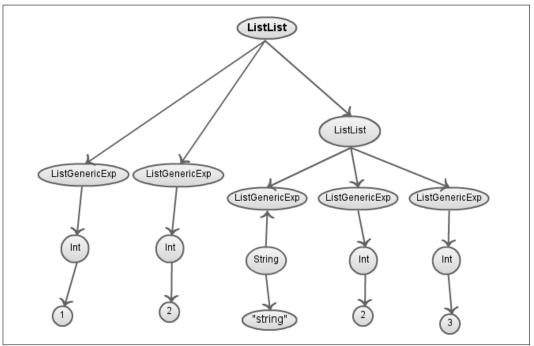


Figure 6.2: Diagram illustrating a parse tree of a list expression

- 6.1.3 Interpreter internal data type
- 6.2 Statement Interpreter
- 6.3 Symbol Table and Parse Tree
- 6.4 Generic Expression Interpreter
- 6.4.1 Function Invocation

Chapter 7 Summary and Analysis