

Problem 1

```
def minimum_gas_price(tank_capacity, distance, gas_location, gas_price):
    current_location = 0
    current_gas = tank_capacity
    total_cost = 0

    gas_location_price = []
    index = gas_location[0]

    for i in range(distance):
        if index < len(gas_location) and i == gas_location[index]:
            gas_location_price.append(gas_price[index])
            index += 1
        else:
            gas_location_price.append(-1)

    while current_location < distance:

        if current_location + current_gas >= distance - 1:
            # break if gas is enough.
            break
        if gas_location_price[current_location] == -1 or current_gas == tank_capacity:
            # move to next location if no gas station here or tank is full
            current_location += 1
            current_gas -= 1
            continue
        min_price = gas_location_price[current_location]
        min_gas_location = current_location

        #Following loop is to find the minimum gas to achieve to
        #another cheaper gas station
        for m in range(1, current_gas):
            if m + current_location < distance
                and gas_location_price[m + current_location] > 0:

                if min_price >= gas_location_price[m + current_location]:
                    min_price = gas_location_price[m + current_location]
                    min_gas_location = m + current_location
        if current_location == min_gas_location:
            total_cost += min_price
            #add only 1 unit gas each time then ckeck again whether can arrive
            #to next target location
            current_gas += 1
        else:
            current_gas = current_gas - (min_gas_location - current_location)
            current_location = min_gas_location

    return total_cost
```

The complexity is $O(\text{tank_capacity} * \text{distance})$

Outer loop complexity is $O(\text{distance})$

Inner loop complexity is $O(\text{tank_capacity})$

Problem 2

```
def adjacentlist(G)

    # define a dictionary to contain the adjacent list of each vertice
    neighbor = dict()

    for i in range(0, len(G.E))
        # x is the "from" node of each Edge and y is the "to" node of each Edge
        # assign adjacent node to corresponding list
        x = G.E.(i,0)
        y = G.E.(i,1)
        neighbor[x].append(y)

    return neighbor

def best_distance(G, current, t, distance, to_vertice)
    if current == t
        distance[current] = 0
        return (distance, to_vertice)
    else if to_vertice[current] < 0
        to_vertice[current] = 0
    #find the best distance with current location
    for vertx in neighbor[current]
        (distance, to_vertice) = best_distance(G, vertx, t, distance, to_vertice)
        if weights(current, vertx) + distance[vertx] > distance[current]
            distance[current] = weights(current, vertx) + distance[vertx]
            to_vertice[current] = vertx
    else
        return (distance, to_vertice)

    return (distance, to_vertice)

def longest_distance(G(V,E), s, t)

    distance = []
    to_vertice = []
    adjacentlist(G)
    for i in range(1,len(G.V))
        distance[i] = -infinity
        to_vertice[i] = -1
        (distance[i], to_vertice[i]) = best_distance(G, s, t, distance[i], to_vertice[i])

    print "The longest path weight is" distance[s]
    print "The longest path is" to_vertice[]
```

The complexity is $O(V+E)$

Find the neighbor is $O(E)$ since we go through each edge only once.

It is difficult for me to code the adjacent-vertices list as $O(E)$ at very beginning.

My method is really similar to the online resource. Online code considers the "no path condition".

Problem 3

```
def fibonacci(num):  
    fib[0] = 0  
    fib[1] = 1  
    for i in range(2, num):  
        fib[i] = fib[i - 1] + fib[i - 2]  
    return fib[num]
```

The solution was almost the same as the solution provided online. The only difference is that `fib[0] = 0` and `fib[1] = 1` in my solution. But the online solution declares `fib[0] = fib[1] = 1`.

Problem 4

```
Def rod_cutting(p,c) :  
    size = len(p)  
    m = [0] * (size + 1)  
    for i in range(1, size) :  
        n = p[i]  
        for j in range(1, i) :  
            n = max(n, p[i] + m[i-j]-c )  
        m[i] = n  
    return m[size]
```

The solution was almost the same as the solution provided online. The difference is that `size = len(p)` in my solution instead of direct declaring. The online solution declares `n` directly. Also my solution uses `m, n` instead of `r` and `q`. For the inner loop, my solution makes `j` changes from 1 to `i`, but the online solution makes `i` change from 1 to `j-1`. The range is a little different.