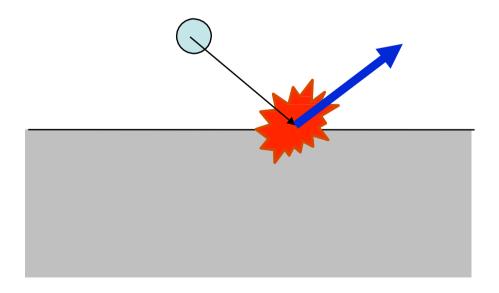
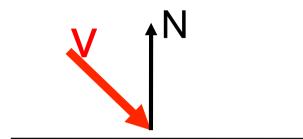


Collisions

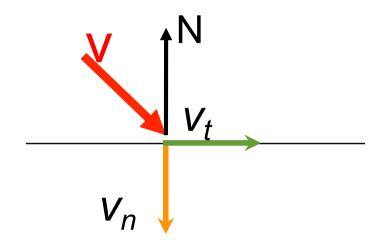
- Detection
- Response
- Overshooting problem (when we enter the solid)



Collision Response for Particles



Collision Response for Particles



$$V=V_n+V_t$$

normal component tangential component

Collision Response for Particles

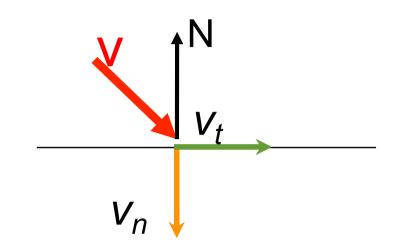
- Tangential velocity v_t often unchanged
- Normal velocity v_n reflects:

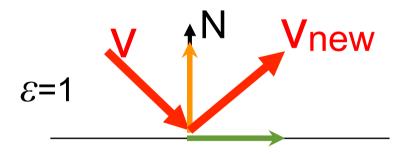
$$v = v_t + v_n$$

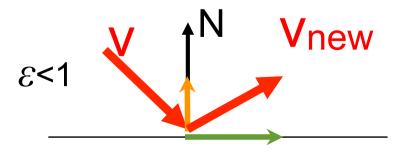
$$v \leftarrow v_t - \varepsilon v_n$$

• Coefficient of restitution ε

• When $\varepsilon = 1$, mirror reflection

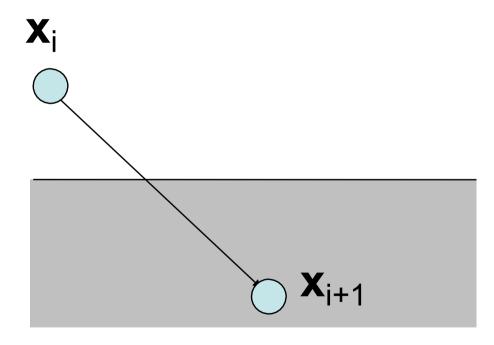






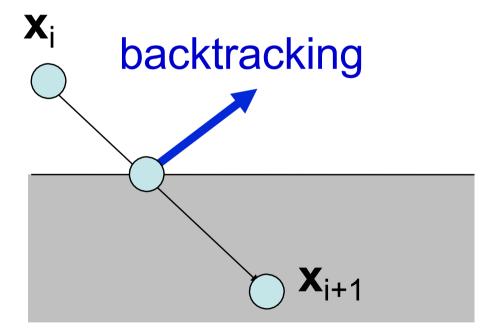
Collisions – Overshooting

• Usually, we detect collision when it is too late: we are already inside



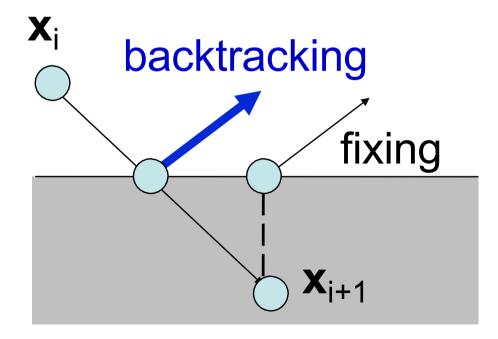
Collisions – Overshooting

- Usually, we detect collision when it is too late: we are already inside
- Solution: Back up
 - Compute intersection point
 - Ray-object intersection!
 - Compute response there
 - Advance for remaining fractional time step



Collisions – Overshooting

- Usually, we detect collision when it is too late: we are already inside
- Solution: Back up
 - Compute intersection point
 - Ray-object intersection!
 - Compute response there
 - Advance for remaining fractional time step
- Other solution:Quick and dirty hack
 - Just project back to object closest point



Questions?

Collision Detection in Big Scenes

- Imagine we have *n* objects. Can we test all pairwise intersections?
 - Quadratic cost $O(n^2)$!

- Simple optimization: separate static objects
 - But still O(static × dynamic+ dynamic²)

Collision Detection in Big Scenes

How to speed up the process?

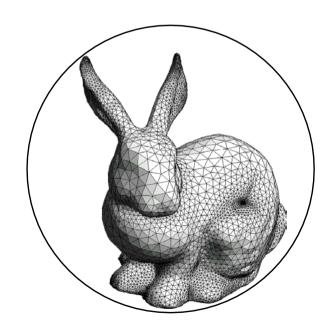
Hierarchical Collision Detection

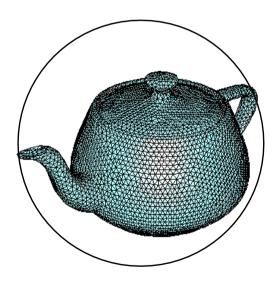
 Use simpler conservative proxies (e.g. bounding spheres)

- Recursive (hierarchical) test
 - Spend time only for parts of the scene that are close
- Many different versions, we will cover only one

Bounding Spheres

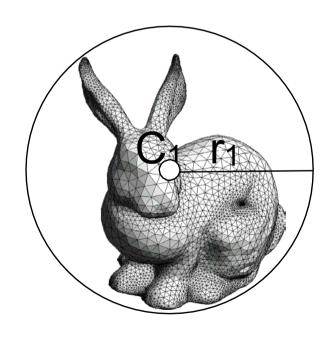
- Place spheres around objects
- If spheres do not intersect, neither do the objects!
- Sphere-sphere collision test is easy.

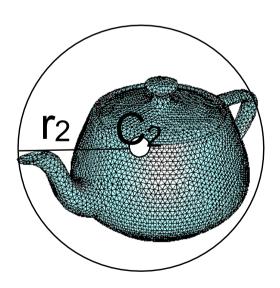




Sphere-Sphere Collision Test

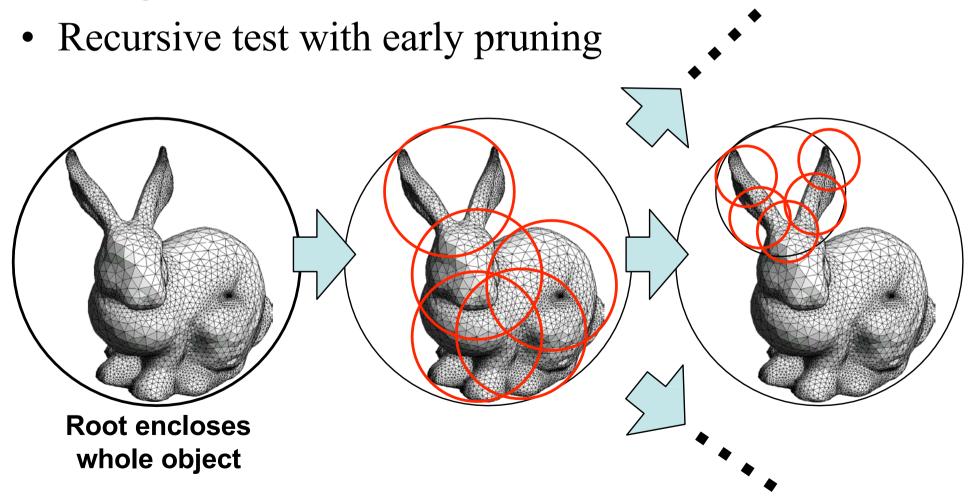
- Two spheres, centers C_1 and C_2 , radii r_1 and r_2
- Intersect only if $||C_1C_2|| < r_1 + r_2$





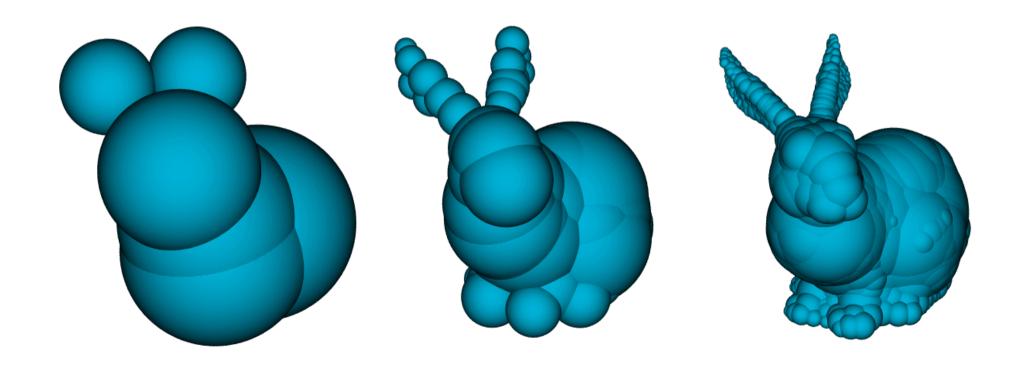
Hierarchical Collision Test

- Hierarchy of bounding spheres
 - Organized in a tree



Examples of Hierarchy

• http://isg.cs.tcd.ie/spheretree/



Pseudocode (simplistic version)

```
boolean intersect (node1, node2)
   // no overlap? ==> no intersection!
   if (!overlap(node1->sphere, node2->sphere)
      return false
   // recurse down the larger of the two nodes
   if (node1->radius()>node2->radius())
      for each child c of node1
         if intersect(c, node2) return true
   else
      for each child c of node2
        if intersect(c, node1) return true
   // no intersection in the subtrees? ==> no intersection!
   return false
```

```
if (!overlap(node1->sphere, node2->sphere)
    return false
if (node1->radius()>node2->radius())
```

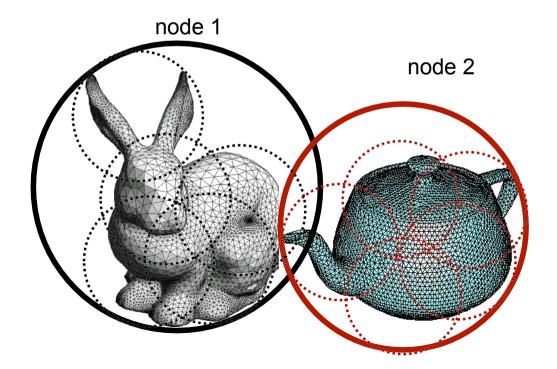
for each child c of nodel

if intersect(c, node2) return true
else

for each child c f node2

if intersect(c, node1) return true

return false

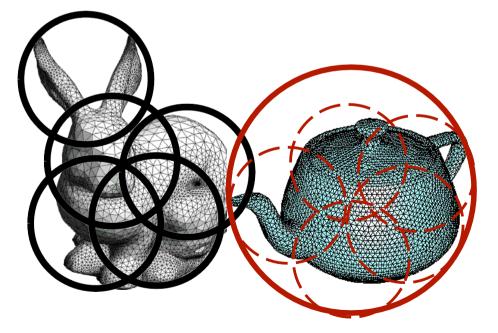


```
boolean intersect(node1, node2)
  if (!overlap(node1->sphere, node2->sphere)
    return false
  if (node1->radius()>node2->radius())
```

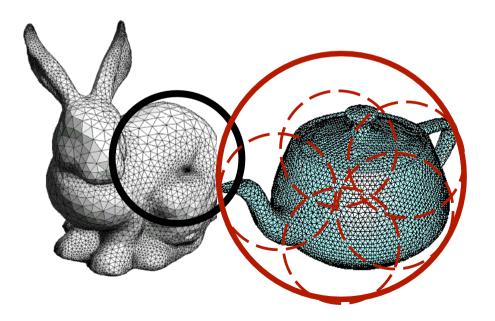
for each child c of node1
 if intersect(c, node2) return true

else

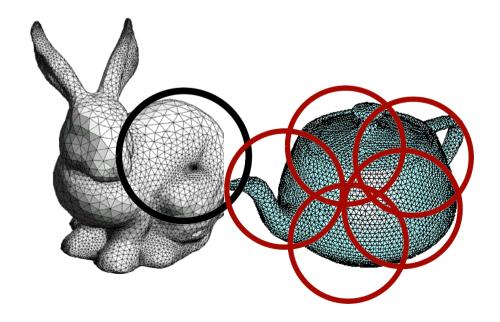
for each child c f node2
 if intersect(c, node1) return true
return false



```
if (!overlap(node1->sphere, node2->sphere)
    return false
if (node1->radius()>node2->radius())
```

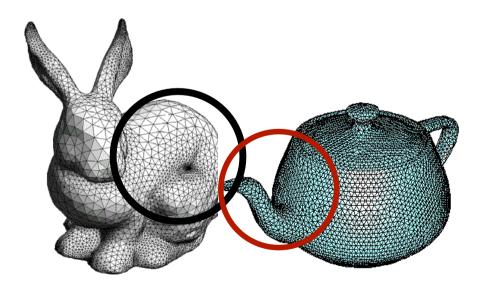


```
if (!overlap(node1->sphere, node2->sphere)
    return false
if (node1->radius()>node2->radius())
```



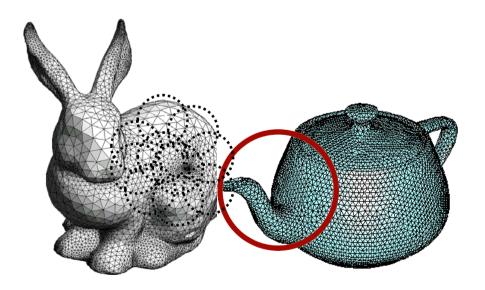
```
if (!overlap(node1->sphere, node2->sphere)
    return false
if (node1->radius()>node2->radius())
```

for each child c of hodel



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if (!overlap(node1->sphere, node2->sphere)
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```

for each child c of hodel

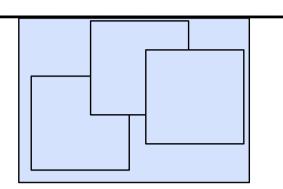


Pseudocode (with leaf case)

```
boolean intersect (node1, node2)
   if (!overlap(node1->sphere, node2->sphere)
      return false
   // if there is nowhere to go, test everything
   if (node1->isLeaf() && node2->isLeaf())
      perform full test between all primitives within nodes
   // otherwise go down the tree in the non-leaf path
   if ( !node2->isLeaf() && !node1->isLeaf() )
      // pick the larger node to subdivide, then recurse
   else
      // recurse down the node that is not a leaf
   return false
```

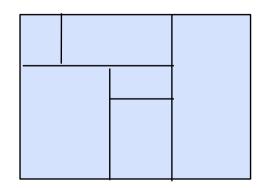
Other Options

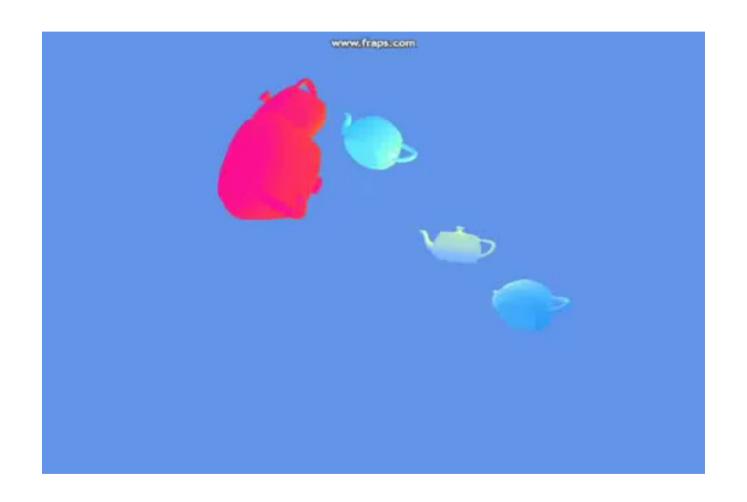
- Axis Aligned Bounding Boxes
 - "R-Trees"



- Oriented bounding boxes
 - S. Gottschalk, M. Lin, and D. Manocha. "OBBTree: A hierarchical Structure for rapid interference detection," Proc. Siggraph 96. ACM Press, 1996

• Binary space partitioning trees; kd-trees





• http://www.youtube.com/watch?v=b_cGXtc-nMg



• http://www.youtube.com/watch?v=nFd9BIcpHX4&f eature=related

Questions?



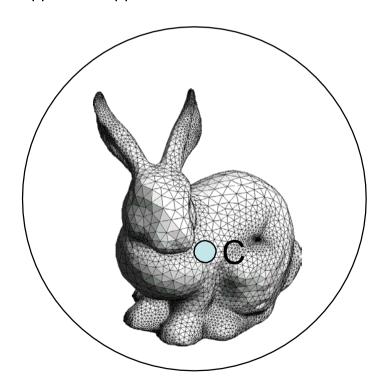
• http://www.youtube.com/watch?v=2SXixK7yCGU

Hierarchy Construction

- Top down
 - Divide and conquer
- Bottom up
 - Cluster nearby objects
- Incremental
 - Add objects one by one, binary-tree style.

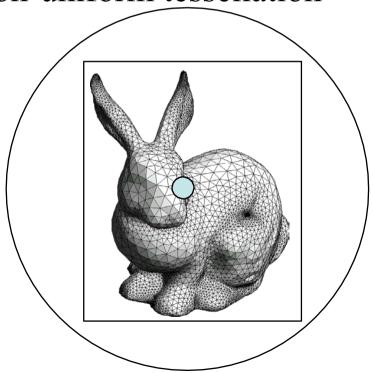
Bounding Sphere of a Set of Points

- Trivial given point set center *C*
 - $\text{ radius} = \max_{i} ||C-P_i||$



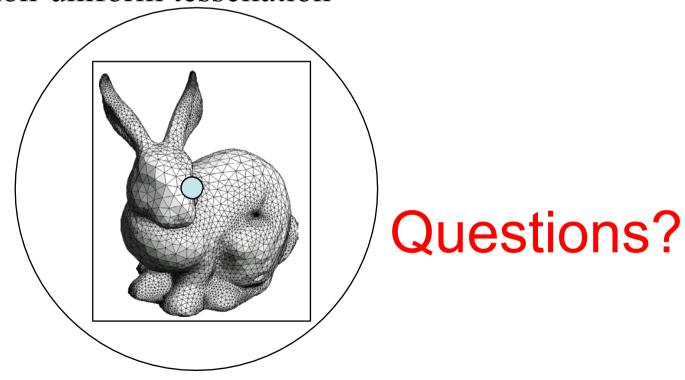
Bounding Sphere of a Set of Points

- Using axis-aligned bounding box
 - center= $((x_{min}+x_{max})/2, (y_{min}+y_{max})/2, (z_{min}, z_{max})/2)$
 - Better than the average of the vertices because does not suffer from non-uniform tessellation



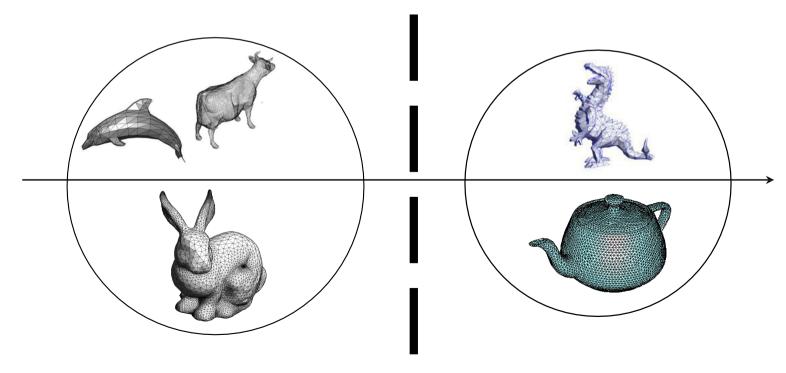
Bounding Sphere of a Set of Points

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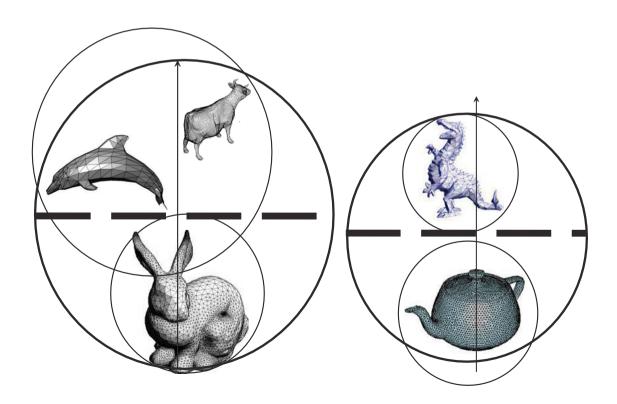
Top-Down Construction

- Take longest scene dimension
- Cut in two in the middle
 - assign each object or triangle to one side
 - build sphere around it



Top-Down Construction - Recurse

- Take longest scene dimension
- Cut in two in the middle
 - assign each object or triangle to one side
 - build sphere around it

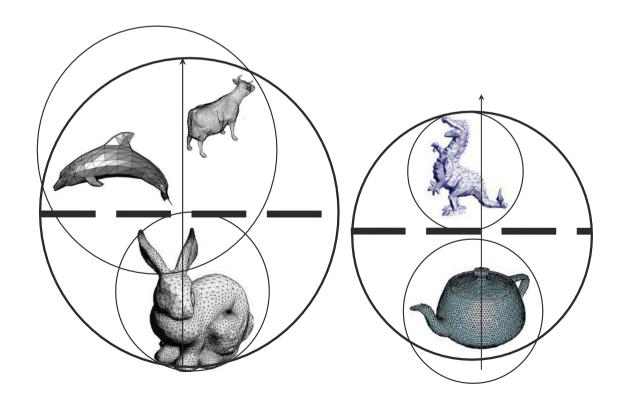


Top-Down Construction - Recurse

- Take longest scene dimension
- Cut in two in the middle

Questions?

- assign each object or triangle to one side
- build sphere around it



Reference



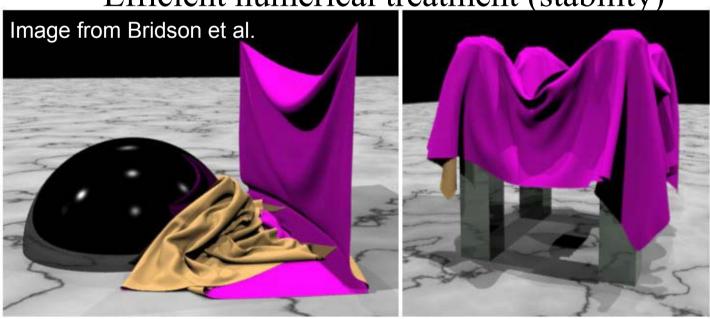
"Real Time Collision Detection," by Christer Ericson http://realtimecollisiondetection.net/

The Cloth Collision Problem

• A cloth has many points of contact

- Stays in contact
- Requires
 - Efficient collision detection

Efficient numerical treatment (stability)



Robust Treatment of Simultaneous Collisions

David Harmon, Etienne Vouga, Rasmus Tamstorf, Eitan Grinspun



David Harmon

Columbia University

Etienne Vouga

Columbia University

Rasmus Tamstorf
Walt Disney Animation Studios

Eitan Grinspun Columbia University