



Position Control and Variable-Height Trajectory Tracking of a Soft Pneumatic Legged Robot



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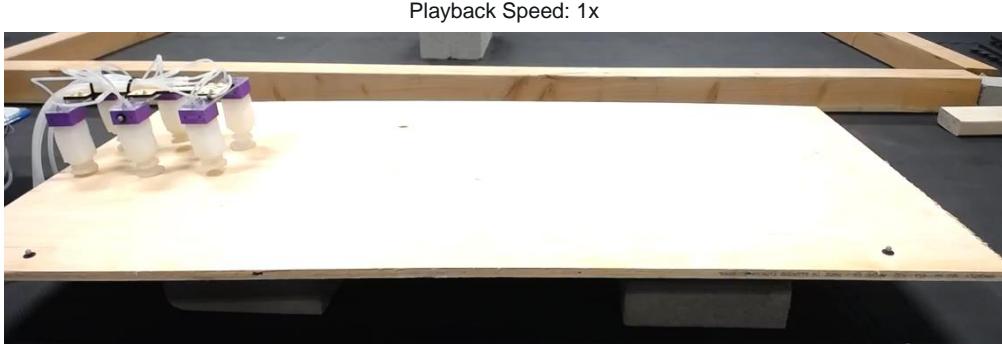
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Motivations

Soft Robotic heXapod (SoRX) [1]:

Previous work introduced a novel soft pneumatic legged robot SoRX, able to traverse rough, steep and unstable terrain



[1] Z. Liu *et al.* in IEEE ICRA, 2020

Objectives & Challenges

Objectives:

- ❖ Extending motion capabilities: feedforward position control and closed-loop trajectory tracking
- ❖ Preliminary feasibility test for outdoor operations (remote-controlled)

Challenges:

- ❖ Model-based motion control
- ❖ Feedback pressure control
- ❖ Closed-loop trajectory tracking

Related Work

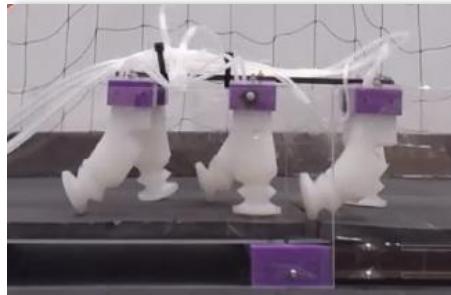
Existing work on soft pneumatic legged robots:



R.F. Shepherd *et al.*, 2011



D. Drotman *et al.*, 2017



Z. Liu *et al.*, 2020



D. Drotman *et al.*, 2021

Limitation: relying on empirically hand-tuned input sequences for open-loop control.

Related Work

Existing work on model-based motion control for pneumatically-actuated robots :

- Piecewise constant curvatures & variable curvature models
e.g., *A. D. Marchese et al. 2016, T. Mahl et al. 2014*
- Cosserat rod, mass-damper-spring-based, finite-element-method-based
e.g., *P. E. Dupont et al. 2019, Y. Guo et al. 2015, T. M. Bieze et al. 2018*
- PID, sliding mode control, MPC and learning-based methods
e.g., *T. M. Bieze et al. 2018, E. H. Skorina et al. 2015, C. M. Best et al. 2016, T. G. Thuruthel et al. 2018*

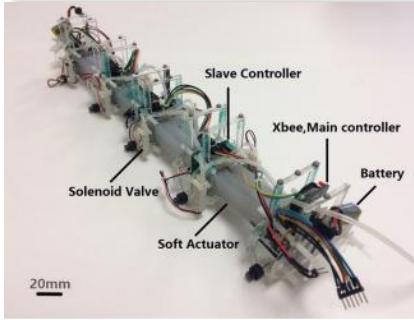
Methods are limited in the application to the control of soft pneumatically-actuated legged robots.

Related Work

Existing work on motion control of soft pneumatic mobile robots (soft robotic snakes):



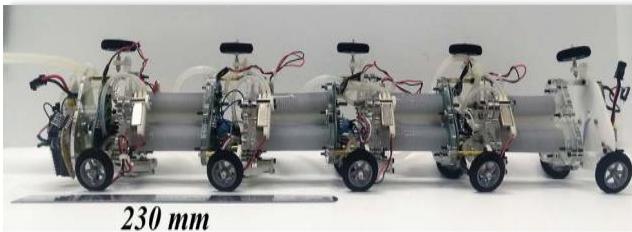
C. D. Onal *et al.*, 2013



M. Luo *et al.*, 2020



C. Della Santina, *et al.*, 2020



Y. Qin *et al.*, 2018

Limitations:

- Rigid parts for contacting with the surface
- Planar movements

Summary

In this work, we develop:

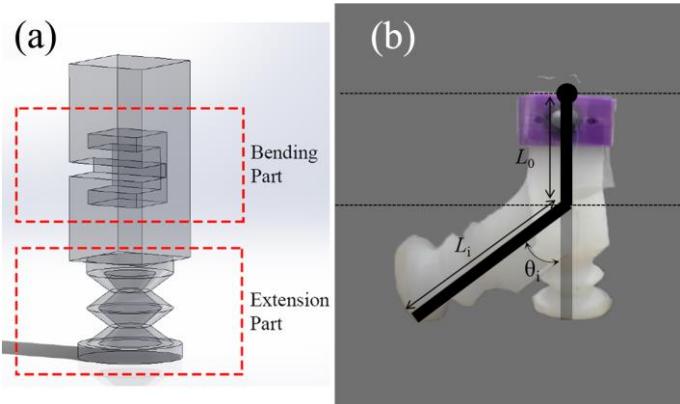
- ❖ A static model based on geometric constraints for feedforward position control (body height and orientation).
- ❖ A pressure feedback controller based on a custom low-cost pneumatic regulation board.
- ❖ A closed-loop trajectory control method to track variable-height trajectories.
- ❖ An experimental study on the robot's position control and trajectory tracking performance.



Static Model

Each leg consists of two actuation parts: bending and extension parts.

We use one revolute θ_i and one prismatic joint* L_i to model the bending and extension parts.

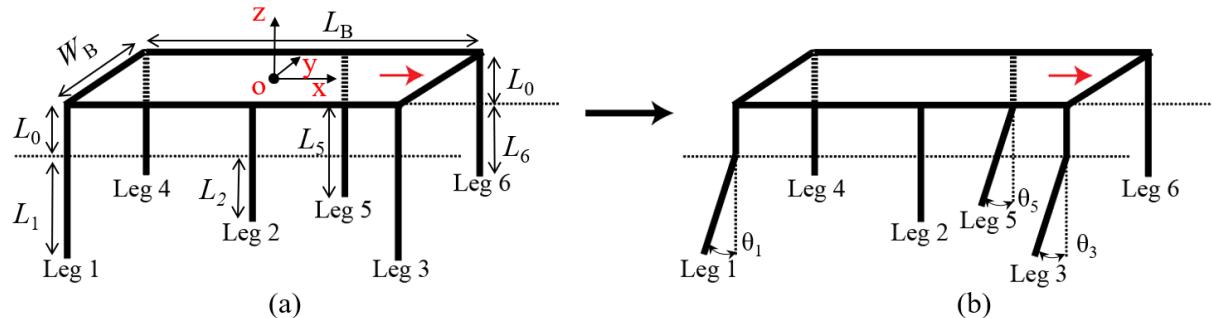


Playback Speed: 1x



* Includes both the length of the extension part and the distance to the cut of the bending part.

Static Model



- ❖ Two steady states for a tripod gait*:
 - (a) only the extension part actuated
 - (b) both parts actuated

❖ The height of the robot:

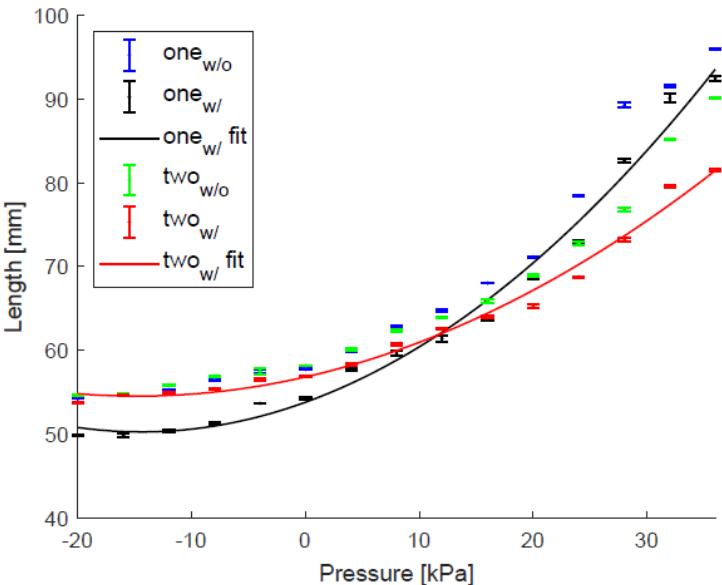
$$h = L_0 + \frac{L_1 + L_5}{2}$$

❖ The robot's roll angle along x axis:

$$\phi = \text{atan}\left(L_5 - L_1, \frac{W_B}{2}\right)$$

* The robot employs an alternating tripod gait.

Pressure Model



TEST CASES FOR EXTENSION PART MODELING

one _{w/o}	Single-leg tripod side actuated, other side not actuated
one _{w/}	Single-leg tripod side actuated, other side pressurized (30 kPa)
two _{w/o}	Double-leg tripod side actuated, other side not actuated
two _{w/}	Double-leg tripod side actuated, other side pressurized (30 kPa)

POLYNOMIAL COEFFICIENTS FOR MODEL FITTING

Models	Polynomials	Units	Ranges
one _{w/}	$0.017p^2 + 0.492p + 53.801$	mm	[-20, 36] kPa
two _{w/}	$0.010p^2 + 0.309p + 56.821$	mm	[-20, 36] kPa
θ	$0.010p + 0.0153$	rad	[-20, 50] kPa

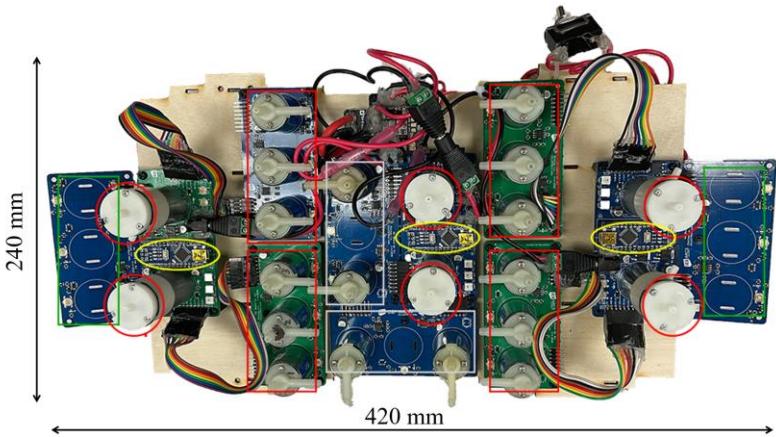
Bending angle model

$$R_{\text{one}_{w/}}^2 = 0.9877 \quad R_{\text{two}_{w/}}^2 = 0.9878 \quad R_\theta^2 = 0.9691$$

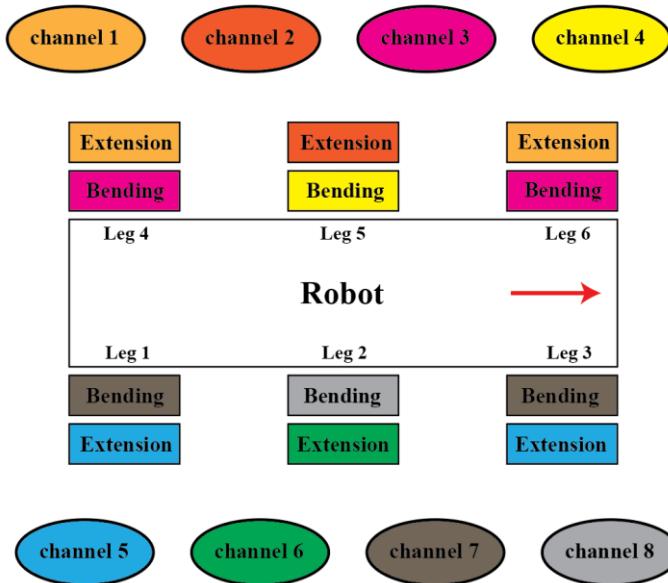
* Extension parts have higher risk to break when input pressure exceeds 36 kPa.

[1] Z. Liu *et al.* in IEEE ICRA, 2020

Pneumatic Regulation



- ❖ A custom low-cost pneumatic regulation board* that powers up to eight channels of pressurization / depressurization with pressure feedback.



- ❖ A diagram of eight air output channels to drive 12 actuation parts. Actuation parts and air output channels of the same color are connected.

Pneumatic Regulation

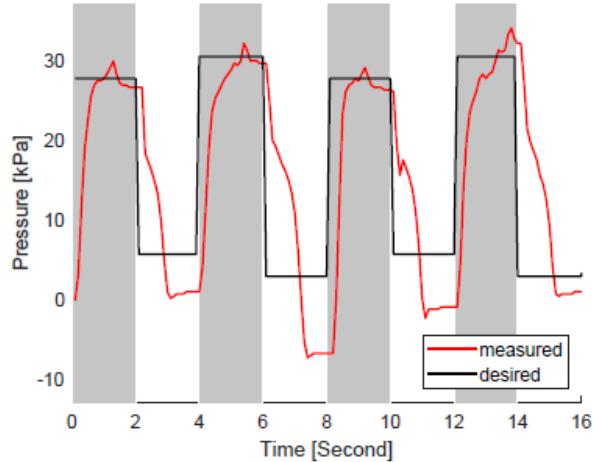
Algorithm 1: Pressure Feedback Controller

Given: total time T , threshold ϵ ;

Input: the desired trajectories ($mode_t$, $desired_t$),
pressure feedback values $real_t$ at time t ;

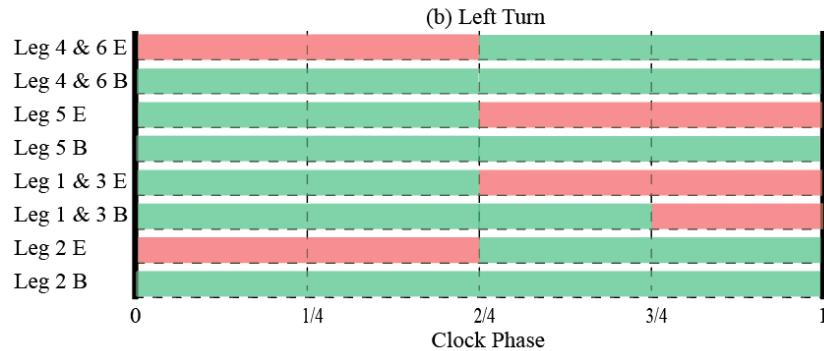
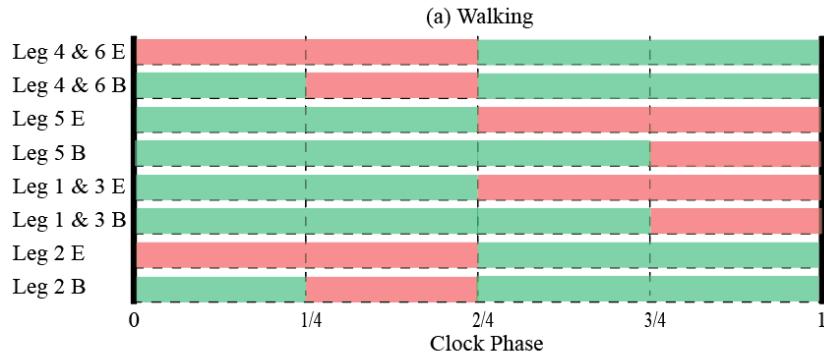
while $t \leq T$ **do**

- if** $mode_t == \text{pressurize}$ **then**
 - if** $real_t < desired_t - \epsilon$ and $Valve_1 == \text{closed}$ **then**
 - $Valve_1 \leftarrow \text{open};$
 - $Pump_1 \leftarrow \text{on};$
 - if** $real_t \geq desired_t$ and $Valve_1 == \text{on}$ **then**
 - $Valve_1 \leftarrow \text{closed};$
 - $Pump_1 \leftarrow \text{off};$
- else**
 - if** $real_t > desired_t + \epsilon$ and $Valve_2 == \text{closed}$ **then**
 - $Valve_2 \leftarrow \text{open};$
 - $Pump_2 \leftarrow \text{on};$
 - if** $real_t \leq desired_t$ and $Valve_2 == \text{on}$ **then**
 - $Valve_2 \leftarrow \text{closed};$
 - $Pump_2 \leftarrow \text{off};$



- ❖ Step response for the proposed pressure feedback controller.

Walking & Turning

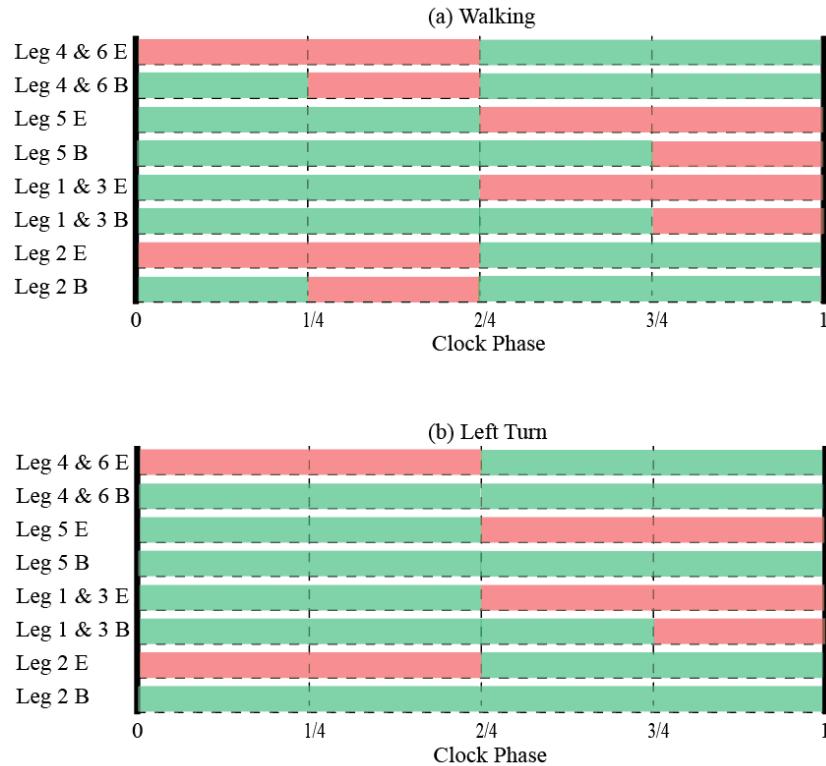


Playback Speed: 4x



- ❖ Actuation sequences for (a) walking and (b) left turn.
- ❖ Notations E and B represent extension and bending parts, respectively.
- ❖ Red boxes are used to represent pressurization, while the green ones stand for depressurization
- ❖ A full actuation sequence enables the robot to turn by approximately 10°.

Velocities

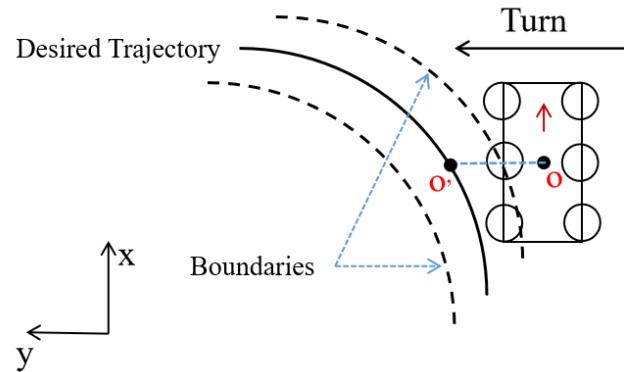


	Clock Phase [s]	Velocities [mm/s]	Velocities [BL/s]
Open-loop pressure control ^[1]	1.6	101	0.44
Closed-loop pressure control	6.6	24	0.11

- ❖ When turning, the speed of the robot is further slowed down as the robot moves forward during only half of the clock phase.

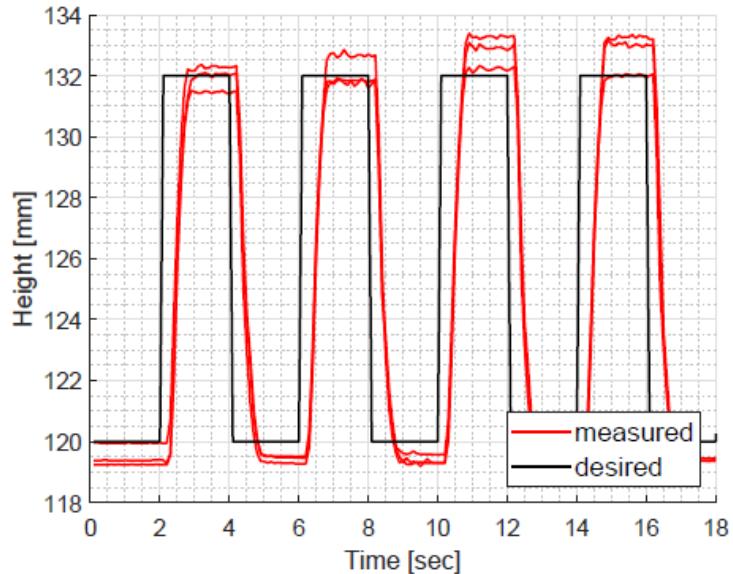
Trajectory Tracker

- Inputs: 3D position from motion capture and desired one.
- A 2D corridor (black dashed lines) with user-defined distance from the desired trajectory.
- Turning gaits triggered when the robot's center lies outside the corridor.
- Desired height (z values) is tracked for variable-height trajectories.



Experiment

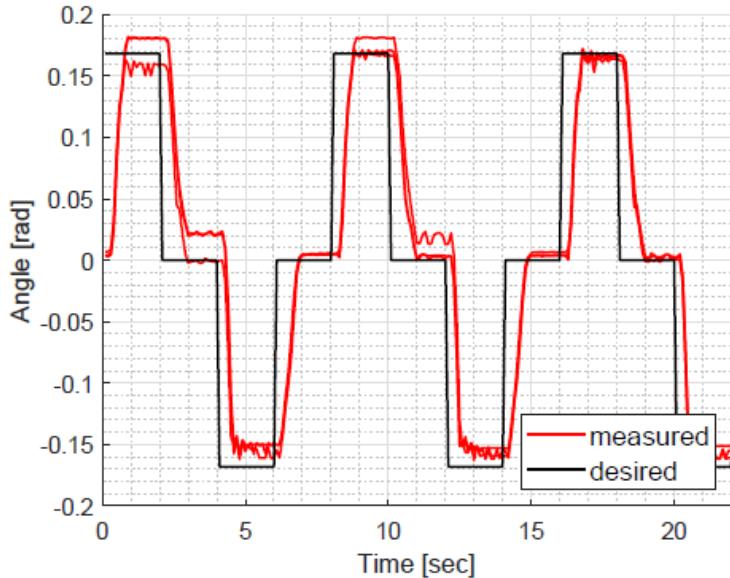
Position Control - Height



- ❖ Desired heights: 132 and 120mm
- ❖ Desired pressures:
 - Double-leg side: 19.75 and -8.11 kPa
 - Single-leg side: 16.93 and 2.26 kPa
- ❖ 3 consecutive trials

Experiment

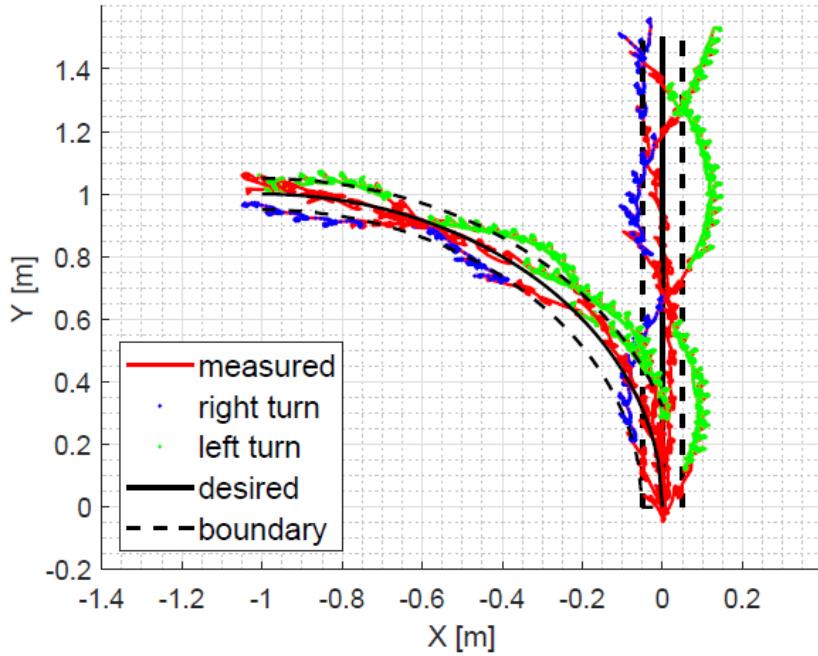
Position Control - Orientation



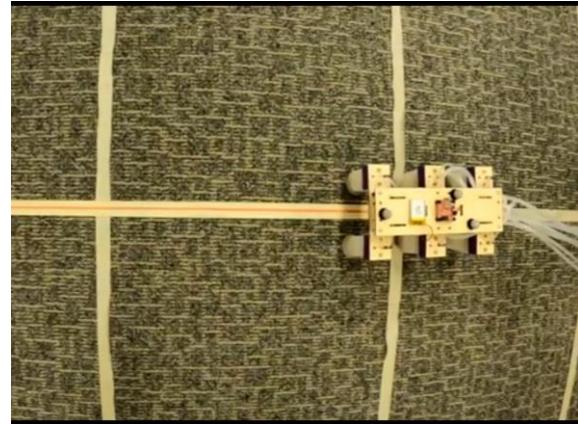
- ❖ Applied same desired pressure inputs to two side of one tripod
- ❖ Desired height different: $h = \pm(L_5 - L_1) = \pm12\text{mm}$
- ❖ Desired roll angle: $\phi = \pm \arctan(\frac{2(L_5 - L_1)}{W_B}) = \pm0.17 \text{ rad}$
- ❖ 3 consecutive trials

Experiment

2D Trajectories - Lines



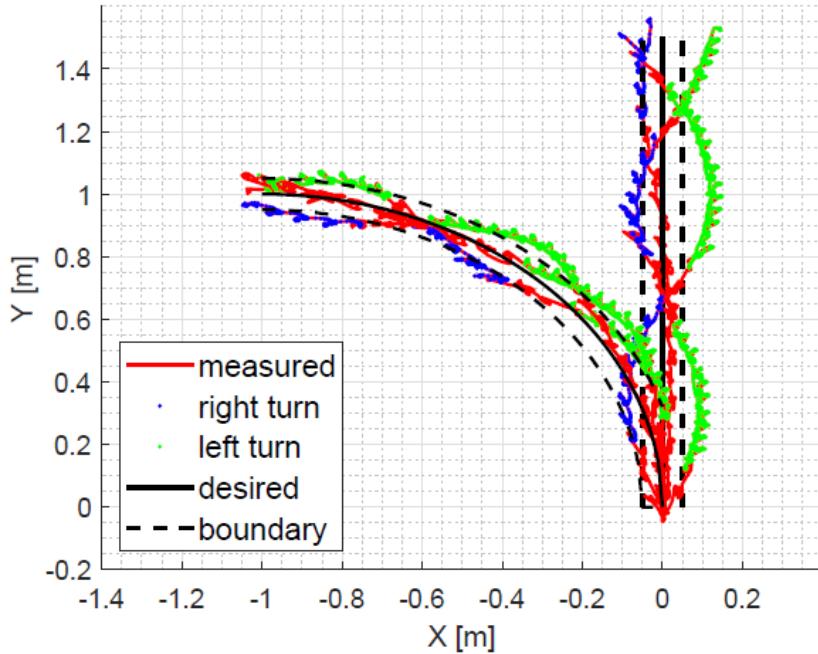
Playback Speed: 8x, starting angle 0



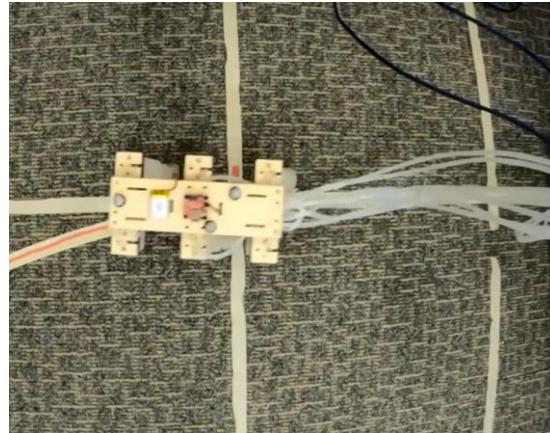
- ❖ Start: $(0,0)$ Goal: $(0,1.5)$ m
- ❖ Desired trajectory: Line $x = 0$
- ❖ Robot stops after passing the line $y = 1.5$ m
- ❖ 2D corridor set as $x = \pm 0.05$ m
- ❖ 3 trials with different starting angles $0, \pm 15^\circ$

Experiment

2D Trajectories - Curves



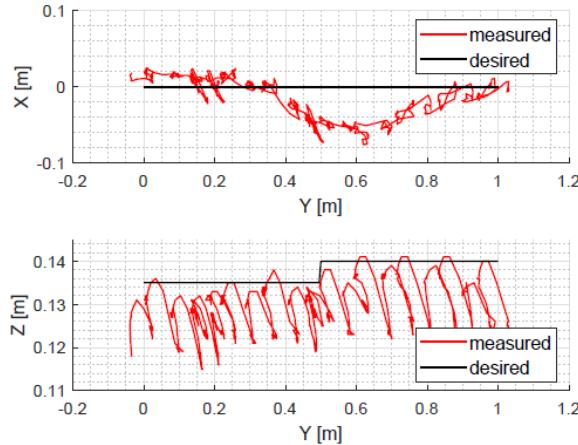
Playback Speed: 8x, starting angle 0



- ❖ Start: (0,0) Goal: (-1,1) m
- ❖ Desired trajectory: Quarter circle of $(x + 1)^2 + y^2 = 1$
- ❖ Robot stops after passing the line $x = -1$ m
- ❖ 2D corridor set as quarter circles of $(x + 1)^2 + y^2 = (1 \pm 0.05)^2$
- ❖ 3 trials with the same starting angle 0

Experiment

Variable-Height & Analysis

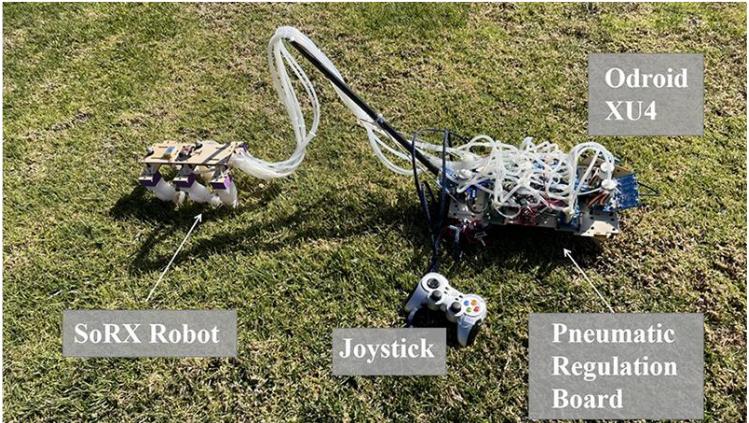


- ❖ Repeat the line tracking test
- ❖ Desired trajectory: Line $x = 0$
- ❖ Desired maximal height switching from 0.135 to 0.140 m after the line $y = 0.5$

Tracking Performance for all tests

Variables	Tracking Errors	Units
Step Response p	-0.737 ± 11.198	kPa
Position Control Height h_1	-0.263 ± 4.910	mm
Position Control Angle ϕ	0.006 ± 0.073	rad
Trajectory Tracking Line d_1	0.029 ± 0.019	m
Trajectory Tracking Curve d_2	0.045 ± 0.020	m
Trajectory Tracking Variable-Height d_3	0.024 ± 0.020	m
Trajectory Tracking Variable-Height h_2	-1.474 ± 2.245	mm

Outdoor Field Tests



- ❖ SoRX can operate in outdoor environments, thanks to the compact and portable pneumatic regulation board.
- ❖ Walking and steering is remote-controlled.
- ❖ Motivate research on autonomous soft legged robots in outdoor environments.



- ❖ Powered by the untethered board, SoRX operates on various types of natural rough terrain, including creeks and gravel.

Discussion

Limitations:

- ❖ Tethered
- ❖ Nonconverging tracker
- ❖ Relying on motion capture for feedback

Future Work:

- ❖ Fully untethered soft legged robot
- ❖ More involved trajectory trackers
- ❖ Autonomous operations in outdoor environment

Acknowledgement

The authors wish to thank Dr. Elia Scudiero for offering access to outdoor experimental fields for testing.





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Thank you!