Electrodynamics:

Take
$$\phi$$
 and A : $\overrightarrow{E} = -\overrightarrow{\phi} - \cancel{\lambda} + \overrightarrow{A}$

$$\overrightarrow{B} = \overrightarrow{\phi} \times \overrightarrow{A}$$

Gauge Invariant:
$$\phi \rightarrow \phi' = \phi - \partial_t \chi(\vec{r}, t)$$

 $\vec{A} \rightarrow \vec{A}' = \vec{A} + \vec{\nabla} \chi(\vec{r}, t)$

Energy, momentum density and stress-tensor:

$$\varepsilon = \frac{1}{2} \left[\varepsilon_0 \left| E \right|^2 + \frac{1}{400} \left| B \right|^2 \right] \leftarrow \text{energy density}$$

$$\vec{S} = c^2 \vec{P} = \frac{1}{u_0} \vec{E} \times \vec{B}$$
 \leftarrow energy Flux.

$$\vec{j} = P \vec{E} + \vec{j} \times \vec{B}$$
 \leftarrow force density.

energy conservation: matter and field sectors. $\frac{d}{dt} \int_{V} d^{3}r \, \mathcal{E}_{\text{Pield}} = \frac{d}{dt} \int_{V} d^{3}r \, \left(\mathcal{E}_{\text{lel}} |\mathbf{E}|^{2} + \frac{1}{100} |\mathbf{B}|^{2} \right)$ = - [+ + +] d3 - [= (= x =) - = (= x =)] - 今·(产×号) # Jobrefield = - Jobr E. J - Jobs. B > every flux し、最小水をfield+「は下き・方=一」と言、方

Dynamics in ϕ and \hat{A}

Ue Gauge Invariance to simplify:

$$\frac{1}{c^2} \frac{1}{c^2} \frac{1}$$

$$2 \downarrow \sqrt{2} \overrightarrow{A} - \frac{1}{c^2} 2 \overrightarrow{A} \overrightarrow{A} = -\frac{1}{46} \overrightarrow{J} *$$

Green functions for temporal problems:

$$\overrightarrow{1} = -f$$

$$\overrightarrow{1} = -3(t-t') \delta(\overrightarrow{r}-\overrightarrow{r}')$$

Then $(\overrightarrow{1}(\overrightarrow{r},t) = \int d^3r' \int dt' G(t,\overrightarrow{r},t',\overrightarrow{r}') f(\overrightarrow{r}',t)$

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Then $(\overrightarrow{1}(\overrightarrow{r},t) = \int d^3r' \int dt' G(t,\overrightarrow{r},t',\overrightarrow{r}')$

Then $(\overrightarrow{r},t') = \int d^3r' \int dt' G(t,\overrightarrow{r},t',\overrightarrow{r}')$

Then $(\overrightarrow{r},t') = \int d^3r' \int dt' G(t,\overrightarrow{r},t',\tau',\tau')$

Then $(\overrightarrow{r},t') = \int d^3r' \int dt' G(t,\tau',\tau',\tau',\tau')$

Then $(\overrightarrow{r},t') = \int d^3r' \int dt' G(t,\tau',\tau',\tau',\tau')$

Then $(\overrightarrow{r},t') = \int d^3r' \int dt' G(t,\tau',\tau',\tau',\tau')$

Then (\overrightarrow{r},t')

Getud
$$\rightarrow$$
 $\begin{vmatrix} \dot{1} & \dot{1}_2 \\ \dot{\alpha}_1 & \dot{\alpha}_2 \end{vmatrix} = \begin{pmatrix} f \\ \dot{\alpha}_1 \\ \dot{\alpha}_2 \end{pmatrix} = \begin{pmatrix} f \\ \dot{\alpha}_2 \end{pmatrix}$

Eq. $\begin{pmatrix} \dot{1} & \dot{1}_2 \\ \dot{\alpha}_2 \end{pmatrix} = \begin{pmatrix} f \\ \dot{\alpha}_2 \end{pmatrix}$

$$\begin{vmatrix} \dot{a}_1 \\ \dot{a}_2 \end{vmatrix} = \frac{1}{1/2 - 1/2} \begin{pmatrix} 1/2 & -1/2 \\ -1/1 & 1/1 \end{pmatrix} \begin{pmatrix} f \\ 0 \end{pmatrix}$$

then
$$a_1 = -\int_{0}^{t} d\tau \frac{1_2(\tau)f(\tau)}{W}$$

some on start

 $-V(\tau)f(\tau)$

$$a_2 = -\int_{\alpha_2}^{t} d\tau \frac{-\gamma_1(\tau)f(\tau)}{W}$$

Some constant.

$$Y(t) = Y_1(t) \left(\int_{x_1}^{t} d\tau \frac{Y_2(\tau)f(\tau)}{W(\tau)} + Y_2(t) \left(\int_{x_2}^{t} d\tau \frac{-Y_1(\tau)f(\tau)}{W(\tau)} \right) \right)$$

$$a_1 \qquad a_2$$

tuning to how much of homogeneous sol goes in , set by initial condition.

then we see by comparing, this is just the Greek's function.

Magnetostatic:



large
$$\rightarrow H = J p \hat{\phi}$$

Collinder

$$\frac{1}{2} \left(-\sin\theta \hat{\chi} + \cos\theta \hat{\gamma} \right)$$

By superposition:
$$\hat{H}_{t+} = H_{large} - H_{small}$$

$$= \frac{1}{2}D\hat{\gamma}, \quad J = \frac{1}{T(c^2-B^2)}$$

$$\frac{1}{2} \frac{1}{2} \frac{1}$$

Solve for the Green's Function: C(t,r; t', r')= 9(t-t', r-r') L fundamental Green Function. (only depend on space and time difference) [t, g(+,r)= S(+) S(r)(-1) then Solve by space Hemporal Fourier transform 9(+,r)= | do | dw (q(w,q) e 19.7 = iwt 1 +, g(t,r) = Jag Jaw [-92 + 2]g(w,9)eg. -iwt then St) & = - (39 Jtw e 19. r-int by Comparing we see $\left[-191^2 + \frac{\omega^2}{c^2}\right] \widehat{g}(\omega, 9) = -1$ but if $\hat{g}(w,q) \neq \frac{1}{w^2 - |q|^2}$ if $w \neq \pm c|q|$ Note w= t c/q/ correspond to homogeneous solution which should be added later. if \(\hat{g}(\omega_9) = \frac{-1}{1921 - \omega^2}, \text{ then} \) Homogoneous Solution. $g(t,\vec{r}) = -\int d^3q \int d\omega \frac{c^2}{\omega^2 - c^2|q|^2} e^{\frac{i\vec{q}\cdot\vec{r} - i\omega t}{2}} + \int d^3q \int d^3q e^{-ic|q|t}$ This integral stops at poles, i.e. $\omega = \pm c|q|$ $+\omega_-(q)e^{-i\vec{q}\cdot\vec{r} + ic|q|t}$

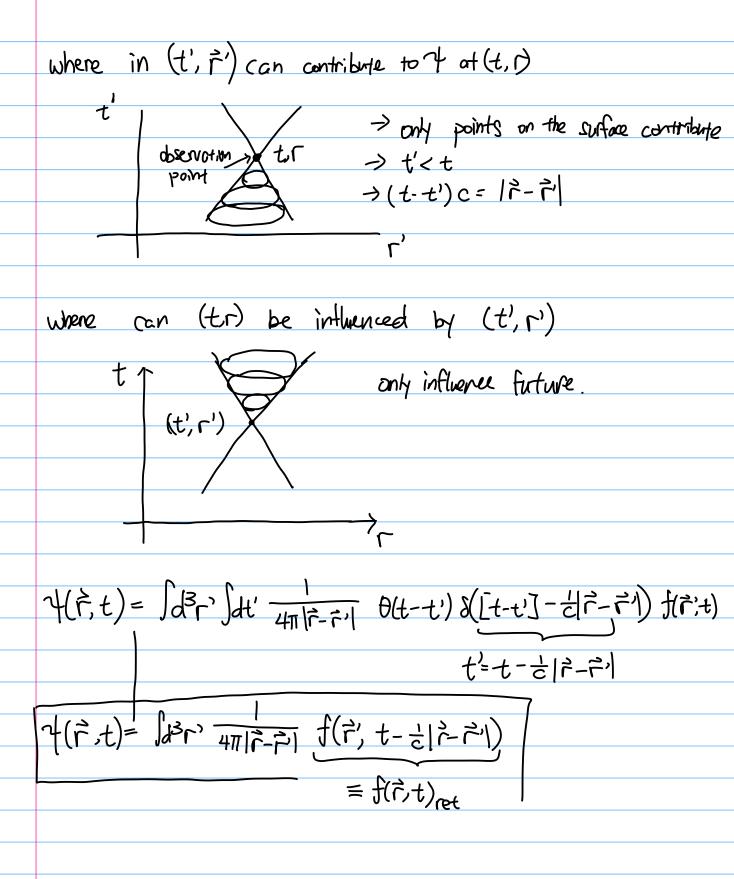
 $\omega = -c|q|$ $\omega = c|q|$ ω

Side note.
$$\int_{0}^{\infty} dz = \int_{0}^{\infty} \frac{id\theta + e^{i\theta}}{i\theta^{2}} = 2\pi i$$
Now integrate
$$\int_{0}^{\infty} dw = \frac{e^{i\phi} \dot{r} - iwt}{w^{2} - e^{2i\eta^{2}}} c^{2} \text{ in complex plane.}$$

$$= \frac{i}{2} t < 0, \text{ we want } w > 0$$

$$= \frac{i}{2} \frac{(iw)t + iw)t}{(iw)t} = \frac{e^{i\phi} t}{e^{i\phi} + e^{iw}t}$$

$$= \frac{i}{2} \frac{e^{i\phi} t}{(iw)t} + \frac{e^{i\phi} t}{(iw)t} = \frac{e^{i\phi} t}{(iw)t} + \frac{e^{i\phi} t}{(iw)t} + \frac{e^{i\phi} t}{(iw)t} = \frac{e^{i\phi} t}{(iw)t} + \frac{e^{i\phi} t}{(iw)t} + \frac{e^{i\phi} t}{(iw)t} = \frac{e^{i\phi} t}{(iw)t} + \frac{e^{i\phi} t}{(iw)t} + \frac{e^{i\phi} t}{(iw)t} = \frac{e^{i\phi} t}{(iw)t} + \frac{e^{i\phi} t}{(iw)t} + \frac{e^{i\phi} t}{(iw)t} = \frac{e^{i\phi} t}{(iw)t} + \frac{e^{i\phi} t}{(iw)$$



Multipole Expansion for ϕ and A: non-relativelic source. - Calculate \$, À → È, B - Keep leading order term. (*F) PJ 740 $P \sim T$ timescale of change in PNon-relativistic: with L, Length scale. \(\text{ \ C} \) : non nelation \(\text{candition} \) (everything makes up fis Slow compared to c) 는 < C : relativistic.

$$\hat{A}(\vec{r},t) = \int_{\vec{r}}^{\vec{r}} \frac{A}{4\pi} \frac{1}{|\vec{r}-\vec{r}|} J(\vec{r},t-\frac{1}{c}|\vec{r}-\vec{r}'|)$$

$$\phi(\vec{r},t) = \int_{\vec{r}}^{\vec{r}} r' \frac{A}{4\pi} \frac{1}{|\vec{r}-\vec{r}'|} f(\vec{r}',t-\frac{1}{c}|\vec{r}-\vec{r}'|)$$

$$= \frac{1}{2} (\vec{r},t)_{\text{ret}}^{-1} + r_{\text{ret}} (\vec{r},t)$$
With multipole expansion: $r' < r$ for away.
$$\phi(\vec{r},t) = \frac{1}{4\pi r} \int_{\vec{r}}^{\vec{r}} r' \rho(\vec{r}',t-\frac{1}{c}|\vec{r}-\vec{r}'|)$$

$$= \frac{1}{r'} \cdot \hat{r} \cdot \hat{r}' \cdot \hat{r}' + O(\frac{r'^2}{r})$$

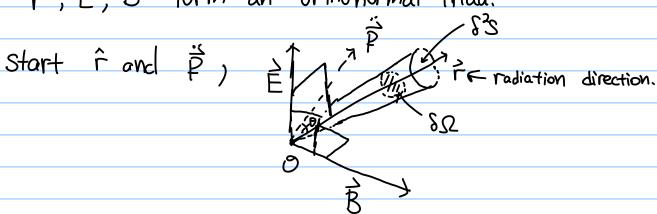
$$= \frac{1}{r'} \cdot \hat{r} \cdot \hat{r}' \cdot \hat{r}'$$

Similarly:

Now calculate È, B:

Qualitative Features:

- leading order of E,B is T, radiation field
- 2) $\left[\stackrel{\sim}{p}(t) \right]_{ret} \rightarrow radiation.$
- 3) F, È, B form an orthonormal triad.



energy flux density
$$\frac{\vec{S}}{16\pi^{2}c} = \frac{1}{\Gamma^{2}} \left[\frac{\vec{E} \times \vec{B}}{\vec{F}} \right]^{2} = \frac{1}{16\pi^{2}c} \left[\frac{\vec{F}}{\vec{F}} \right]^{2} \left[\frac{\vec{F}}{\vec{F}} \right]^{2} = \frac{1}{16\pi^{2}c} \left[\frac{\vec{F}}{\vec{F}} \right]^{2} = \frac{1}{16$$

 $SP = \lim_{S \to \infty} S^{2}S^{2}S = \frac{10}{16\pi^{2}c} \left[\frac{1}{P}(t)\right]_{ret}^{2} S^{2}S^{2}S = \frac{1}{16\pi^{2}c} \left[\frac{1}{P}(t)\right]_{ret}^{2} S^{2}S^{2}S = \frac{1}{16\pi^{2}c} \left[\frac{1}{P}(t)\right]_{ret}^{2}$ $P = \int_{S} d\Omega \frac{SP}{S\Omega} = \int_{S} d\phi \int_{S} \sin\theta d\theta \frac{SP}{S\Omega} = \frac{1}{16\pi^{2}c} \left[\frac{1}{P}(t)\right]_{ret}^{2}$

Formula

Comp exam guestioni

A charge Q in uniform rectlinear motion. What are E and B?

$$\nabla^2 \phi - \frac{1}{2} \partial_t^2 \phi = -\frac{1}{2} P(r,t) = -\frac{1}{2} Q S(\vec{r} - \vec{R}(t))$$

$$\nabla^{2}\hat{A} - \frac{1}{c^{2}} \hat{J}_{t}^{2}\hat{A} = - u_{0}\hat{J}(r_{0}t) = -u_{0}Q_{1}\hat{z}_{s}(\vec{r}-\vec{R}(t))$$

Calculate Fourier transformi

$$\phi(\vec{r},t) = \int_{a}^{b} k \hat{\phi}(\vec{k},t) e^{i\vec{k}\cdot\vec{r}}$$

$$\hat{\beta}(\vec{r},t) = \int_{a}^{b} k \hat{\beta}(\vec{k},t) e^{i\vec{k}\cdot\vec{r}}$$

$$4 \left(|\mathbf{k}|^2 + \frac{1}{c^2} \lambda^2 \right) \hat{\phi}(\vec{k}, t) = \frac{Q}{\epsilon_0} e^{-i\vec{k} \cdot \vec{k}(t)}$$

assume
$$\hat{\phi} \sim \beta e^{-1} \hat{k}$$
. It &

then we find
$$\beta = \frac{0}{6} \frac{1}{|\vec{k}|^2 - \frac{1}{6^2} v^2 k_2^2}$$

then we find
$$\beta = \frac{0}{\varepsilon} \frac{1}{|\vec{k}|^2 - \frac{1}{c^2} \sqrt{2} k_z^2}$$

$$\Rightarrow \hat{\phi}(\vec{k}, t) = \frac{1}{\varepsilon} \frac{0}{k_x^2 + k_y^2 + y^2 k_z^2} \quad \text{where} \quad y^2 = 1 - \frac{1}{c^2}$$

$$\hat{A}(\vec{k},t) = u_0 \frac{\partial v \hat{z} e^{-i\vec{k} \cdot vt \hat{z}}}{k_x^2 + k_y^2 + v^2 k_z^2}$$

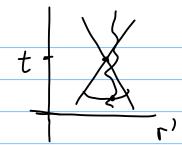
and let
$$k_z = 8 k_z$$

then
$$\phi(\vec{r},t) = \frac{Q}{E_0} \frac{1}{4\pi} \sqrt{\frac{1}{|x^2+y^2|} + \frac{|z-yt||^2}{|x^2+y^2|}}$$

$$\vec{A}(\vec{r},t) = 16QV \hat{z} \frac{1}{|y^2(x^2+y^2) + (z-yt)|^2}$$

$$\vec{E}(\vec{r},t) = \frac{Q}{4\pi\epsilon_0} \frac{1}{|x^2(x^2+y^2) + (z-yt)|^2} (\vec{r} - \vec{R}(t))$$

Lienard-Wiechart potential:



potential caused by single charge particle

We Know:

$$\phi(t,\vec{r}) = \frac{1}{4\pi\epsilon_0} \int d^3r' \frac{f(t,\vec{r}')_{re+}}{|\vec{r}-\vec{r}'|}$$

Instead of day dt'

$$\phi(t, \dot{r}) = \frac{1}{4\pi\epsilon} \int dt' \, d^3r' \frac{\theta(t-t')}{|\dot{r}-\dot{r}'|} S([t-t']-\dot{c}|\dot{r}-\dot{r}']) 98(\dot{r}-\dot{r}_{k})$$

$$\vec{A}(t,\vec{r}) = \frac{u}{4\pi} \int dt' d\vec{r}' \frac{\partial (t-t')}{|\vec{r}-\vec{r}'|} \, 8([t-t']-[-t']-[-r']) \, 9\vec{R} \, S(\vec{r}-\vec{R})$$

$$\hat{A}(t,\hat{r}) = \frac{910}{471} \int_{at}^{at} \frac{\hat{R}(t')}{\hat{r}-\hat{R}(t')} S([t-t'] - \frac{1}{c} |\hat{r}-\hat{R}(t')|)$$

then
$$f(t') = (t-t') - \frac{1}{c} |\hat{r} - \hat{R}(t')|$$
 note that $= t' - \frac{1}{c} |\hat{r} - \hat{R}(t')|$

$$f(t') \approx f(t_{ret}) + (t'-t_{ret}) \frac{d}{dt'} f(t) \Big|_{t'=t_{ret}}$$

$$= (t'-t_{ret}) \frac{d}{dt'} \Big\{ t-t' - \frac{1}{c'} \Big[r^2 - 2\hat{r} \cdot \hat{R}(t') + R^2(t') \Big]^{1/2} \Big|_{t'=t_{ret}}$$

$$= (t'-t_{ret}) \Big[-1 - \frac{1}{c'} \frac{1}{r'-\hat{R}(t_{ret})} + R^2(t') \Big] \frac{1}{t'=t_{ret}}$$

$$= (t'-t_{ret}) \Big[-1 + \frac{1}{c'} \frac{\hat{r}-\hat{R}(t_{ret})}{|\hat{r}-\hat{R}(t_{ret})|} \cdot \hat{R}(t_{ret}) \Big]$$

then
$$S([t-t']-\dot{\epsilon}|\hat{r}-\hat{R}(t)|) = S([t'-t_{ret}]\{-1+\dot{\epsilon}\hat{R}\cdot\hat{n}\})$$

$$\phi(t, \hat{r}) = \frac{1}{4\pi\epsilon} q \frac{1}{|\hat{r} - \hat{R}(t_{ret})|} \frac{1}{1 - \frac{1}{c}\hat{R}(t_{ret}) \cdot \hat{h}}$$

$$\vec{A}(t,\vec{r}) = \frac{u_0}{4\pi} \sqrt[q]{|\vec{r} - \vec{R}(t_{ret})|} \frac{\vec{R}(t_{ret})}{|-\frac{1}{c}|\vec{R}(t_{ret})|}$$

Then
$$\dot{E}(t,\dot{r}) = \frac{q}{4\pi\epsilon_0} \left[\frac{[\hat{n}-\dot{z}\dot{R}][1-\dot{z}\dot{R}^2]}{z^3|\dot{r}-\dot{R}|^2} \right]$$

$$\vec{B}(t,\vec{r}) = - \hat{b} \times \vec{E}(t,\vec{r})$$

$$\hat{N} = \frac{\hat{\Gamma} - \hat{R}}{|\hat{\Gamma} - \hat{R}|}$$

for
$$\alpha = 1 - \frac{1}{c} \hat{n} \cdot \hat{R}$$

 $\hat{n} = \frac{\hat{r} - \hat{R}}{|\hat{r} - \hat{R}|}$ all evaluated at tret

Plane Waves

> Solution to Maxwell's equation for ϕ and \tilde{A} when there are no source terms P.J.

together with Lorenz Gauge: - 2224 + 7. A = 0

and additional gauge freedom such that $\overline{7}X = 0$

Plane wave Solutions:
$$\phi(t, \vec{r}) = 0$$
 due to gauge choice.

Now determine A(t, r):

Suppose:
$$\vec{A}(t,\vec{r}) = \int d^3q \, e^{i\vec{q}\cdot\vec{r}} \, \hat{A}(t,\vec{q})$$

If A(t, ?) is real, this means

$$\Rightarrow \vec{A}(t,\vec{r}) = \vec{A}(t,\vec{r})^*$$

$$\rightarrow \vec{A}(t,-\vec{q}) = \vec{A}(t,\vec{q})^*$$
 With Fourier.

Using Lovenz Garge: 7. A=0

In Fourier 1> 9. A(t, 9) = 0

This means à has no component along à direction. so A is transverse.

with
$$\Box \tilde{A}(t,\tilde{r}) = 0$$
 $\Rightarrow -\frac{1}{C} dt^2 \tilde{A}(t,\tilde{r}) - \tilde{q}^2 \tilde{A}(t,\tilde{r}) = 0$

Harmonic Decillator-like

Solution \Rightarrow Since $\tilde{A}(t,\tilde{q})$ is complex and 3 components \Rightarrow 6 eq

 \Rightarrow but due to the transverse property, $\tilde{q}, \tilde{A}(t,\tilde{r}) = 0$

we can eliminate 2 equations, for real and amplex:

then $6 \Rightarrow 4$ eq.

 \Rightarrow Also know $\tilde{A}(t,\tilde{q})$ is actually real, so $4 \Rightarrow 2$ eq.

80 gaineral solution is?

 $\tilde{A}(t,\tilde{q}) = \tilde{C} = \tilde{C} + \tilde{C} + \tilde{C} = \tilde{C} + \tilde{C} + \tilde{C} + \tilde{C} = \tilde{C} + \tilde{C} + \tilde{C} + \tilde{C} + \tilde{C} = \tilde{C} + \tilde{C}$

Now consider the entire Fourier Transform from to -9: (C,(q)e-icqt + B,(q)e+icqt)eig-+ + (C,(-9)e+B,(-9)eiq+B, use $C_1(-9) = C_2^*(9)$ and $C_2(-9) = C_1^*(9)$ = (c, (q)eic9t+c, (q)eic9t)ei9.7+(c, (q)eic9t+c, (q)*eic9t)ei9.7 = (q) e 19. - 109t + (q(q) e 19. + 109t + CC. = $\hat{C}(\hat{q}) = \hat{q} \cdot \hat{r} - icqt$ Complex plane electromagnetic wave. Polarization is managed by $\hat{C}(\hat{q})$ then $\vec{A}(t,\vec{r}) = \text{Re} \int \vec{J}^3 q \vec{c}(\vec{q}) \exp\{i\hat{q}\cdot\hat{r} - icqt\}$ 4 pieces of information, amplitude and phase for the two directions normal to q.

Then
$$\vec{E} = -\vec{P}\vec{\Phi} - \lambda_t \vec{A}$$

$$= Re \int_{\vec{q}} \vec{r} \cdot \vec{q} \cdot \vec{r} - icqt$$

$$= Re \int_{\vec{q}} \vec{r} \cdot \vec{q} \cdot \vec{r} \cdot icqt$$
these are arthogonal to each other and orthogonal to \vec{q} .
$$= Re \int_{\vec{q}} \vec{r} \cdot \vec{q} \cdot \vec{r} \cdot icqt$$

$$= Re \int_{\vec{q}} \vec{r} \cdot \vec{q} \cdot \vec{r} \cdot icqt$$

Notice:
$$\frac{\left[i\hat{q}\times\hat{c}(q)\right]\cdot\left[-i\hat{q}\times\mathcal{C}(q)^{*}\right]}{\left[C(q)iCq\right]\cdot\left[\hat{c}(q)^{*}(q)\right]} = \frac{1}{c^{2}}$$

$$\frac{\left[C(q)iCq\right]\cdot\left[\hat{c}(q)^{*}(q)\right]}{\Rightarrow \text{speed of light.}}$$

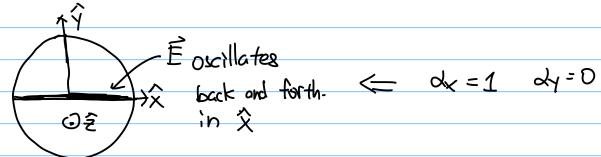
then
$$\dot{E} = Re \left[\dot{c}(\dot{q}) i c q \right] exp \left\{ i \dot{q} \cdot \dot{r} - i c q t \right\}$$

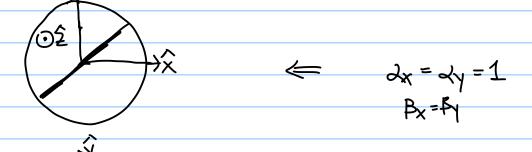
$$= Re \left[\dot{d}_{x} e^{i \dot{p}_{x}} \dot{\chi} + d_{y} e^{i \dot{p}_{y}} \dot{\gamma} \right] e^{i \dot{q} \cdot \dot{r} - i c q t}$$

$$= d_{x} \cos \left(q(z - ct) + \beta_{x} \right) \dot{\gamma}$$

$$+ d_{y} \cos \left(\gamma(z - ct) + \beta_{y} \right) \dot{\gamma}$$

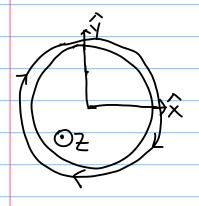
Polarization: lihear





$$\Rightarrow \lambda_{x} = \lambda_{y} = 1$$

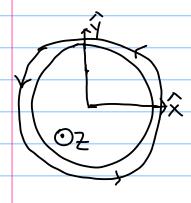
Polarization: Circular / Elliptical.

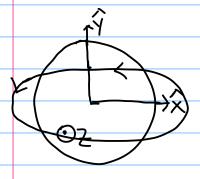


$$Circular$$

$$\iff \lambda_x = \lambda_y = 1$$

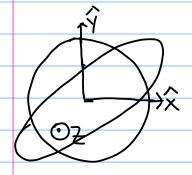
$$\Rightarrow \beta_x = \beta_1 + \frac{\pi}{2}$$





$$\begin{aligned}
& = \frac{\text{Elliptical}}{\text{dx} = 1} \\
& = \frac{\text{dy} = \frac{1}{2}}{\text{dx}}
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	Coming back to complex plane EM wave:
	$\vec{C}(\vec{q})e^{i\vec{q}\cdot\vec{r}-iCqt}$ with $\vec{C}(\vec{q})\cdot\vec{q}=0$
	~ \$.\$=0 andition.
	At fixed t, for plane to be constant, it must be on the
	surface:
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	9·r-ct=f, const r] ← Plake wave
Compt	nent of it along or
9 69	icle for all part
on th	all for all positions. 2 constant surface.