a) 
$$H_{L0} = \vec{\lambda} \cdot \vec{B}_{eff}$$

$$= \frac{1}{2m_e^2c^2} \frac{1}{r} \frac{dV_c}{dr} (\vec{l} \cdot \vec{S})$$

$$H_{B} = \frac{-eB}{2m_{e}c} \left( L_{Z} + 2S_{Z} \right)$$

b) 
$$H_{LS} = \frac{1}{2me^{2}c^{2}} \frac{1}{r} \frac{dV_{c}}{dr} (\vec{1} \cdot \vec{S})$$

$$\sim \frac{1}{me^{2}c^{2}} \sim \frac{e^{2}}{a_{0}} \sim \frac{1}{a_{0}} \sim \frac{e^{2}}{a_{0}} \sim \frac{1}{a_{0}} \sim \frac{1}{a_{0}}$$

with 
$$\alpha = \frac{e^2}{hc} \sim \frac{1}{137}$$
 and  $\alpha_0 = \frac{h^2}{mez}$ 

$$H_{LS} \sim \frac{\text{th}^2}{\text{Me}^2\text{c}^2} \left( \frac{\text{Mee}^2}{\text{th}^2} \right)^2 \frac{\text{e}^2}{\text{a}_0} \sim \frac{\text{e}^2}{\text{th}^2\text{c}^2} \frac{\text{e}^2}{\text{a}_0} \sim \left[ \frac{2}{2} \frac{\text{e}^2}{\text{a}_0} \right]$$

$$\frac{he}{\left(\frac{h^2}{e^2a_0}\right)\frac{e^2}{a^2h}}B \sim 2ea_0B \sim H_B$$

By setting strong magnetic limit when  $H_B \gg H_{LS}$ .

All a  $A \not\in A \cap B$   $\Rightarrow A \not\in A \cap B$ Strong magnetic limit when  $A \not\in A \cap B$ Strong magnetic limit when  $A \not\in A \cap B$ Strong magnetic limit when  $A \not\in A \cap B$ Strong magnetic limit when  $A \not\in A \cap B$ Strong magnetic limit when  $A \not\in A \cap B$ 

Bent 
$$\sim 2 \frac{e}{as^2} \sim \frac{1}{137} (4.868 \times 10^{-10} \text{ stateau}) (5.3 \times 10^{-9} \text{ cm})^2$$

$$\sim 1.25 \times 10^6 \text{ Gauss}$$

$$10^4 \text{ Gauss} = 17$$

$$\text{Berit } \sim 12.5 \text{ Tesla}$$

If B >> Borit = 12.5 T than strong magnetic field If B << Borit = 12.5 T then weak magnetic field.

c) Consider  $B \gg B c n + (S + 1) + (S + 2) +$ 

=) After diagonalizing Ho+HB, we should use  $|n,1,5,m_1,m_s\rangle$  we see HB  $\sim$  (Lz + 2Sz), so we should use quantum #, me, me which diagonalizes Lz and Sz.

We cannot use i for J' because now there is a preferred direction in 2 which breaks spherical symmetry, leaving only rotational symmetry around 2.

By using 
$$|n, 1, S = \frac{1}{2}$$
,  $m_1, m_s > \frac{-eB}{2m_e C}$  ( $L_z + 2S_z$ )  $|n, 1, \frac{1}{2}$ ,  $m_1, m_s > \frac{-eB}{2m_e C}$  ( $L_z + 2S_z$ )  $|n, 1, \frac{1}{2}$ ,  $m_1, m_s > \frac{1}{2}$  using  $|L_z| |m_1, m_2 > \frac{1}{2}$  and  $|L_z| |m_2, m_2 > \frac{1}{2}$  and  $|L_z| |m_1, m_2 > \frac{1}{2}$  and  $|L_z| |m_2, m_2 > \frac{1}{2}$  and  $|L_z| |m$ 

d) Now do perturbation theory on His, since His  $\ll$  have unperturbed states  $|n, 1, S = \frac{1}{2}, m_c, m_s\rangle$ If there is just Ho, then we have degeneracy = (28+1)(21+1)for  $S = \frac{1}{2}$ , # of degeneracy = 2(21+1)

Now with  $\langle H_B \rangle = \frac{-eBh}{2mec} (m_1 + 2m_s)$ , we get degeneracy, i.e. Same energy when  $m_1' + 2m_s' = m_1 + 2m_s$ 

where  $m_e = \pm \frac{1}{2}$  so  $2m_e = \pm 1$ 

$$| > m_1' \pm 1 = m_1 \pm |$$
  
 $| > m_2' = m_1 \pm | \mp |$   
 $| > m_2' = m_1 \pm | \mp |$ 

d) Now do perturbation theory on His, since His « His we have unperturbed Hates  $|n, L, S = \frac{1}{2}, m_E, m_S\rangle$ First order perturbation:  $E_{1s}^{(1)} = \langle n, \ell, s = \frac{1}{2}, m_{\ell}, m_{s} | \frac{1}{2m_{e}^{2}c^{2}} \frac{1}{\Gamma} \frac{dV_{c}}{d\Gamma} (\hat{L} \cdot \hat{S}) | n, \ell, s = \frac{1}{2}, m_{\ell}, m_{s} \rangle$ = 3m<sup>2</sup>C<sup>2</sup> < \( \frac{1}{4}\cdot \cdot < \lorente{1.5} \) Non L.S= LzSz + LxSx + LySy use  $S_{t} = \frac{S_{t} + S_{-}}{S_{+} + S_{-}}$   $S_{1} = \frac{S_{1}}{S_{+} - S_{-}}$  $L_{X} = \frac{L_{+} + L_{-}}{2i}$   $L_{Y} = \frac{L_{+} - L_{-}}{2i}$ then [.s= L=S= + + (S+[++L+S-+L-S++8-[--S+[++L+S++L-S+-8-[-)  $= L_{z} S_{z} + \frac{1}{2} (L_{+} S_{-} + L_{-} S_{+})$   $< \tilde{L} \cdot \tilde{S} > = \langle m_{\ell}, m_{S} | L_{z} S_{z} | m_{\ell}, m_{S} \rangle + \frac{1}{2} \langle m_{\ell}, m_{S} | L_{z} S_{-} | m_{\ell}, m_{S} \rangle$ + = <m, ms = S+ | m, ms>
= to m, ms

The Hamiltonian of spin- = system subject to external field is:

using 
$$S_z = \frac{1}{2} \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$$
,  $S_x = \frac{1}{2} \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$ ,  $S_y = \frac{1}{2} \begin{pmatrix} 0 & -i \\ i & 0 \end{pmatrix}$ 

Separate H into Ho (time-independent) and V(t) (time-dependent)

$$H = -\frac{ehB_1}{2m_eC} \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix} - \frac{ehB_0}{2m_eC} \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix} coswt + \begin{pmatrix} 0 & -i \\ i & 0 \end{pmatrix} sin wst$$

$$V(t)$$

So 
$$H_0 = \frac{-ekB_1}{2meC} (|+><+|-|-><-|)$$

and 
$$V(t) = \frac{-ehB_0}{2meC} \left\{ \left( |-><+| + |+><-| \right) \cos \omega t + \left( -i|+><-| + i|-><+| \right) \sin \omega t \right\}$$

The above equation has the same exact form as the equation of the 2-state system that we did in class with

$$\frac{-ehB_0}{2MeC} = 8$$

$$|C_{2}(t)|^{2} = \frac{y^{2}/h^{2}}{y^{2}/h^{2} + (w_{2}-w_{2})^{2}} \sin^{2}\left\{\sqrt{\frac{y^{2}}{h^{2}} + \frac{(w_{2}-w_{2})^{2}}{4}} t\right\}$$

with 
$$\Omega = \sqrt{\frac{\delta^2}{\hbar^2} + \frac{(\omega_0 - \omega_{k1})^2}{4}}$$
, then  $|G(t)|^2 = \frac{\delta^2 h^2}{\Omega^2} \sin(\Omega t)$ 

$$|C_1(t)|^2 = 1 - |C_2(t)|^2$$

Now find P(t), absorption power:

then 
$$P(t) = \frac{d}{dt} \left( |C_2(t)|^2 \Delta E_{21} \right)$$
 where  $\Delta E_{21} = E_2 - E_1$  between 2 states.

$$= \frac{d}{dt} \left( |C_2|^2 + 2 \Delta E_{21} \right)$$

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$$= \frac{d}{dt} \left( |C_2(t)$$

$$P(t) = \hbar \omega_{21} \frac{2 \delta^2 + 2}{\sqrt{\hbar^2 + (\omega_5 \omega_2)^2}} \sin \Omega t \cos \Omega t$$

then 
$$\frac{\delta}{h} = -\frac{eB_0}{2meC} = \frac{|e|B_0}{2meC}$$

$$W_{21} = \frac{-eB_1}{meC} = \frac{|e|B_1}{meC}$$

$$s_0$$
  $\frac{\lambda}{4} \ll \omega_{2|}$ .

So when 
$$\omega_{2} \simeq \omega_{21} \rightarrow \omega_{-} \omega_{21} \sim 0$$
, so  $\Omega \sim \frac{\gamma}{h}$ 

and 
$$\Omega = \sqrt{\left(\frac{1}{K}\right)^2 + \frac{\left(W - W_{21}\right)^2}{4}} \sim \frac{7}{K}$$
, which is very small.

so the oscillation behavior of absorption power will be slow.

Show 
$$W = e^{A+\lambda B} = e^{A} \left[ 1 + \lambda \int_{0}^{1} d\tau, e^{TA} B e^{TA} + \cdots \right]$$

BI

 $\frac{d}{d\tau} U(\tau) = \frac{d}{d\tau} \left[ e^{TA} e^{T(A+\lambda B)} \right]$ 

Note:  $\uparrow$  is just a number, so  $[\tau A, \lambda] = 0$ 
 $\frac{d}{d\tau} e^{TA} = A e^{A} = e^{TA} A$ 
 $= -A e^{TA} e^{T(A+\lambda B)} + e^{TA} (A+\lambda B) e^{T(A+\lambda B)}$ 
 $= e^{TA} (A) e^{T(A+\lambda B)} + e^{TA} (A+\lambda B) e^{T(A+\lambda B)}$ 
 $\Rightarrow \frac{d}{d\tau} U(\tau) = e^{TA} A B e^{T(A+\lambda B)}$ 

Now integrate above expression:

 $U(\tau) - U(\tau = 0) = \int_{0}^{\tau} e^{TA} A B e^{T(A+\lambda B)} d\tau,$ 

Note  $U(\tau) = e^{TA} e^{T(A+\lambda B)}$  and  $U(\tau = 0) = 1$ 
 $\Rightarrow e^{TA} e^{T(A+\lambda B)} - 1 = \lambda \int_{0}^{\tau} e^{TA} A B e^{T(A+\lambda B)} d\tau,$ 
 $\Rightarrow e^{T(A+\lambda B)} = e^{TA} \left[ 1 + \lambda \int_{0}^{\tau} e^{TA} A B e^{T(A+\lambda B)} d\tau, \right]$ 

Use iteration:

 $\Rightarrow e^{T(A+\lambda B)} = e^{TA} \left[ 1 + \lambda \int_{0}^{\tau} e^{TA} A B e^{T(A+\lambda B)} d\tau, \right]$ 

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 $\Rightarrow e^{TA} e^{T(A+\lambda B)} = e^{TA} \left[ 1 + \lambda \int_{0}^{\tau} e^{TA} A B e^{T(A+\lambda B)} d\tau, \right]$ 
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 $\Rightarrow e^{TA} e^{T(A+\lambda B)} = e^{TA} \left[ 1 + \lambda \int_{0}^{\tau} e^{TA} A B e^{T(A+\lambda B)} d\tau, \right]$ 
 $\Rightarrow e^{TA} e^{TA}$ 

$$t < 0$$
:  $H = \frac{p^2}{2m} + \frac{1}{2} m w_0^2 x^2$ 

$$=\frac{p^2}{2m}+\frac{1}{2}m\omega^2\left(\chi^2-\frac{29\ell}{m\omega^2}\chi\right)$$

$$H = \frac{p^2}{2m} + \frac{1}{2}mw_0^2 \left( \chi - \frac{qE}{mw_0^2} \right)^2 - \frac{1}{2} \frac{q^2 E^2}{mw_0^2}$$

with eigeneners. 
$$E_{\alpha} = \hbar w_{o} \left( \alpha + \frac{1}{2} \right) - \frac{1}{2} \frac{g^{2} e^{2}}{m w_{o}^{2}}$$

For 
$$\mathcal{H}_{old}$$
:  $a = \sqrt{\frac{mW_o}{2\hbar}} \left( x + i \frac{p}{mW_o} \right)$ 

Since 
$$H_{\text{new}} = H_{\text{old}} \left( \chi - \frac{q \varepsilon}{\text{mw}_0^2} \right) - \frac{1}{2} \frac{q^2 \varepsilon^2}{\text{mw}_0^2}$$

by analogy define annihilation operator for Hnew as:

$$\alpha_{\text{new}} = \sqrt{\frac{m\omega_{0}}{2\hbar}} \left( \left[ X - \frac{q\varepsilon}{m\omega_{0}^{2}} \right] + i \frac{P}{m\omega_{0}} \right)$$

$$= \sqrt{\frac{m\omega_{0}}{2\hbar}} \left( X + i \frac{P}{m\omega_{0}} \right) - \sqrt{\frac{m\omega_{0}}{2\hbar}} \frac{q\varepsilon}{m\omega_{0}^{2}}$$

$$a_{\text{new}} = a - \sqrt{\frac{mw_{\text{o}}}{2h}} \frac{q_{\text{E}}}{mw_{\text{o}}^2}$$

$$\lambda = \sqrt{\frac{mw_{\text{o}}}{2h}} \frac{q_{\text{E}}}{mw_{\text{o}}^2}$$

$$\lambda = \sqrt{\frac{mw_{\text{o}}}{2h}} \frac{q_{\text{E}}}{mw_{\text{o}}^2}$$

Now define a new State (x=0) to denote the ground state of Hnew.

is annihilation operator of Hnew, Now since anew We should have:

 $\begin{array}{c|c}
\text{Cinew} & |d=0\rangle = 0 \\
\text{but Gnow} = a - \lambda \\
& (a - \lambda) & |d=0\rangle = 0
\end{array}$ 

$$(a-\lambda)$$
  $|a=0\rangle=0$ 

By the above expression, we observe that the eigenstate la=0> for Hnew is also eigenstate for the onnihilation operator for Hod and the eigenvalue is the difference between anew and a.

now lets define ld> as the general eigenstate for thew

so expanding In=0> in Id>

$$|n=0\rangle = \sum_{\alpha=0}^{\infty} |\alpha\rangle \langle \alpha | n=0\rangle$$

So 
$$P_{\alpha} = \left| \langle \alpha \rangle \right|^{2} =$$

Now determine Cu:

$$C_{\lambda} = \langle \lambda \mid | N=0 \rangle$$

$$= \langle \lambda \mid | \frac{1}{|\alpha|} (a_{new}) \mid | N=0 \rangle$$

$$= \langle \lambda \mid | \frac{1}{|\alpha|} (a_{new}) \mid | N=0 \rangle$$

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$$= \langle \lambda \mid | N=0 \rangle$$

$$= \langle$$

C<sub>d=0</sub> Now find C<sub>d=0</sub> via normalization:

$$\langle n=0 | n=0 \rangle = 1$$
 $\downarrow \sum_{d=0}^{\infty} |C_{d}|^{2} = 1$ 

Taylor expansion of exp{ | \lambda|^2}

$$C_{2=0} = \exp\left\{-\frac{|\lambda|^2}{2}\right\}$$

So 
$$C_{\alpha=0} = \exp\left\{-\frac{|\lambda|^2}{2}\right\}$$

$$C_{\alpha} = \frac{1}{|\alpha|}(-\lambda)^{\alpha} e^{-\frac{|\lambda|^2}{2}} \text{ with } \lambda = \sqrt{\frac{mu_0}{2}} \frac{9\epsilon}{mu_0^2}$$

Therefore:  $P_{cl} = |C_{cl}|^2 = \frac{1}{cl} \left[ \frac{m\omega_o}{2t_0} \left( \frac{q\varepsilon}{m\omega_o^2} \right)^2 \right] \exp \left\{ -\frac{m\omega_o}{2t_0} \left( \frac{q\varepsilon}{m\omega_o^2} \right)^2 \right\}$ probability of going to the  $close{cl}$  excited state in the new Hamiltonian from the ground state in dd Hamiltonian

5) 
$$H_{\text{new}} = \frac{p^2}{2m} + \frac{1}{2}mw^2\chi^2 - 9E\chi\exp\{-\frac{t^2\eta^2}{2}\}$$

a) 
$$t_0 = -\infty$$
,  $|m, t_0 = -\infty$ ,  $t = t_0 > = |n|$ 

$$P_{n\rightarrow m} = \left| C_m^{(i)}(t) \right|^2$$

$$|n, t_0 = -\infty, t\rangle_{I} = U_1(t, t_0 = -\infty) |n, t_0 = -\infty; t = t_0)$$

From first order perturbation theory:

$$C_{m}^{(1)}(t) = \frac{1}{\pi} \int_{-\infty}^{t} \langle m | V_{I} | n \rangle dt'$$

$$= \frac{1}{\pi} \int_{-\infty}^{t} \langle m | e^{\frac{ikt}{\pi}} | v e^{\frac{-ikt}{\pi}} | n \rangle dt'$$

for Harmanic oscillar Holm> = Enln> for En=two(n+1)

$$=\lim_{t\to\infty}\frac{-i}{\pi}\int_{-\infty}^{t=\infty}\frac{i}{(E_m-E_n)t'}\langle m|\left(-9\epsilon_n\chi\right)e^{\frac{-t'^2}{12}}|n\rangle dt'$$

$$=\frac{1}{4}9\epsilon\int_{\infty}^{\infty}e^{i\omega_{0}(m-n)t'}\langle m|\chi|n\rangle e^{\frac{-t'^{2}}{4t'}}dt'$$

$$=\frac{1}{4}9\epsilon\langle m|\chi|n\rangle\int_{\infty}^{\infty}e^{i\omega_{0}(m-n)t'}e^{\frac{-t'^{2}}{4t'}}dt'$$

$$= \sqrt{11} + \exp\left\{-\frac{1}{4} \left(m-n\right)^{2}\right\}$$

$$=\frac{i\sqrt{\pi}}{4\pi}q_{\infty} \Upsilon \exp\left\{-\frac{r^2w^2(m-n)^2}{4}\right\} \sqrt{\frac{\pi}{2m\omega_{\infty}}} \ll m|\alpha^{\dagger}+\alpha|n\rangle$$

$$=\frac{i\sqrt{\pi}}{4\pi}q_{\infty} \Upsilon \exp\left\{-\frac{r^2w^2(m-n)^2}{4}\right\} \sqrt{\frac{\pi}{2m\omega_{\infty}}} (\sqrt{n+1} S_{m,n+1} + \sqrt{n} S_{m,n-1})$$
then  $P_m^{(1)}(t=\infty) = |C_m^{(1)}(t=\infty)|^2$ 

$$=\frac{\pi}{2m\omega_{\infty}} \exp\left\{-\frac{r^2w^2(m-n)^2}{2}\right\} ((n+1)S_{m,m+1} + n S_{m,n+1})$$
So
$$=(n+1)\frac{\pi q^2e^2\Gamma^2}{2km\omega_{\infty}} \exp\left\{-\frac{r^2\omega_{\infty}^2}{2}\right\} \quad \text{if } m=n+1$$

$$=n\frac{\pi q^2e^2\Gamma^2}{2km\omega_{\infty}} \exp\left\{-\frac{r^2\omega_{\infty}^2}{2}\right\} \quad \text{if } m=n-1$$

$$=0 \qquad \text{otherwise}$$
D) The condition of application when  $|C_n^{(1)}(t-\omega)| \ll 1$ 

$$|C_n^{(1)}(t=\omega)|^2 \approx \frac{(q_{\infty}\tau)^2}{km\omega_{\infty}} \exp\left\{-\frac{r^2\omega_{\infty}^2}{2}\right\} \ll 1$$
So
$$=(n+1)\frac{r^2e^2\Gamma^2}{2km\omega_{\infty}} \exp\left\{-\frac{r^2\omega_{\infty}^2}{2}\right\} \ll 1$$
So
$$=(n+1)\frac{r^2e^2\Gamma^2}{2km\omega_{\infty}} \exp\left\{-\frac{r^2\omega_{\infty}^2}{2}\right\} \ll 1$$

$$=(n+1)\frac{r^2e^2\Gamma^2}{2km\omega_{\infty}} \exp\left\{-\frac{r^2\omega_{\infty}^2}{2}\right\} \ll 1$$
So
$$=(n+1)\frac{r^2e^2\Gamma^2}{2km\omega_{\infty}} \exp\left\{-\frac{r^2\omega_{\infty}^2}{2}\right\} \approx 1$$
So
$$=(n+1)\frac{r^2\omega_{\infty}^2}{2} \exp\left\{-\frac{r^2\omega_{\infty}^2}{2}\right\} \exp\left\{-\frac{r^2\omega_{\infty}^2}{2}\right\} \approx 1$$
So
$$=(n+1)\frac{r^2\omega_{\infty}^2}{2} \exp\left\{-\frac{r$$