## **Tensor Calculus**

## An Introduction to Tensor Calculus

- 1. Why Tensor Calculus?
- 2. Geometric vectors as the starting point for Tensor Calculus. Vector-valued functions and more!
- 3. The Two Conflicting Definitions of the Gradient
- 4. Two Geometric Gradient Examples (Torricelli's and Heron's Problems)
- 5. The Covariant Basis
- 6. Change of Coordinates
- 7. The Tensor Notation
- 8. Position Vector, Covariant Basis, Covariant Metric Tensor, Contravariant Basis
- 9. A Few Tensor Notation Exercises
- 10. Quadratic Form Minimization
- 11. Decomposition by Dot Product in Tensor Notation
- 12. The Relationship Between the Covariant and the Contravariant Bases
- 13. Index Juggling
- 14. The Tensor Property
- 15. Invariants Are Tensors
- 16. The Christoffel Symbol
- 17. The Covariant Derivative
- 18. The Covariant Derivative 2
- 19. Velocity, Acceleration, Jolt and the New  $\frac{\delta}{\delta t}$ -derivative
- 20. Determinants and Cofactors
- 21. Relative Tensors
- 22. The Levi-Civita Tensors
- 23. The Voss-Weyl Formula

- 24. Embedded Surfaces and the Curvature Tensor
- 25. The Surface Derivative of the Normal
- 26. The Curvature Tensor On The Sphere Of Radius R
- 27. The Christoffel Symbol on the Sphere of Radius R
- 28. The Riemann Christoffel Tensor & Gauss's Remarkable Theorem
- 29. The Equations of Surface and the Shift Tensor
- 30. The Components of the Normal Vector
- 31. The Covariant Surface Derivative in Its Full Generality
- 32. The Normal Derivative
- 33. The Second Order Normal Derivative
- 34. Gauss' Theorema Egregium Part 1
- 35. Gauss' Theorema Egregium Part 2
- 36. Linear Transformations in Tensor Notation
- 37. Inner Products in Tensor Notation
- 38. The Self-Adjoint Property in Tensor Notation
- 39. Integration The Arithmetic Integral
- 40. Integration The Divergence Theorem
- 41. Non-hypersurfaces
- 42. Examples of Curves in 3D
- 43. Non-hypersurfaces Relationship Among The Shift Tensors
- 44. Non-hypersurfaces Relationship Among Curvature Tensors 1
- 45. Non-hypersurfaces Relationship Among Curvature Tensors 2
- 46. Principal Curvatures
- 47. Geodesic Curvature Preview
- 48. Materials

## **Essentials of Tensor Calculus**

- 1. **A**
- 2. **B**
- 3. **C**
- 4. **D**
- 5. **E**

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