

Automatic Differentiation, Adjoint, and Sensitivities

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Automatic Differentiation Primitive Rules

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