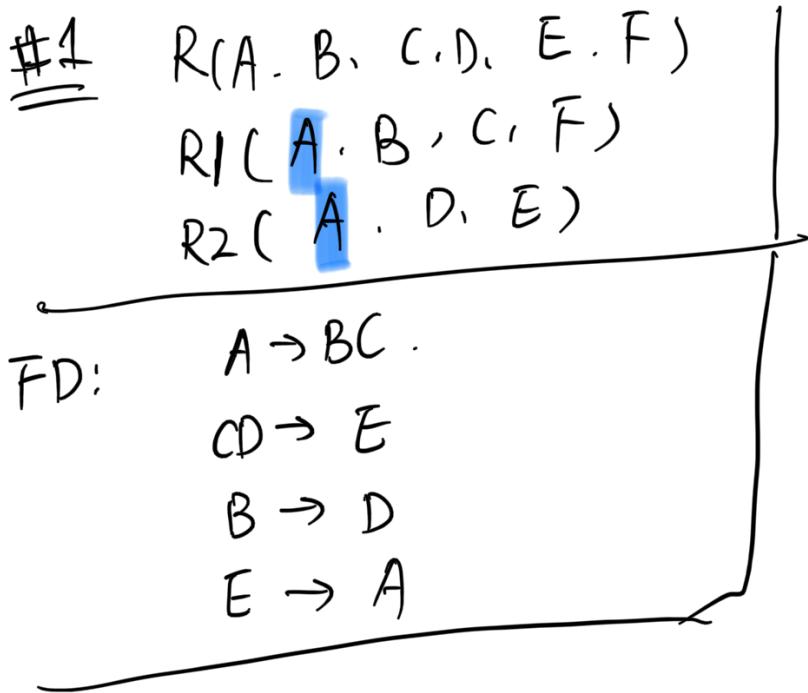


Hw4 q1



Lossless-Join Decomposition:

$R(X, Y, Z) \rightarrow R_1(X, Y) \quad R_2(Y, Z)$ is lossless-join if $Y \rightarrow X, Y \rightarrow Z$

Y is the shared attri.

That's to say, shared attributes need to be the key of R_1 or R_2 .

Answer: shared attribute is 'A'.

Does $A \rightarrow BCF$?

OR Does $A \rightarrow DE$?

check $A \rightarrow BCF$?

$$\{A\}^+ = \{A \underline{B} C\}$$

$$\{A\}^+ = \{A \underline{B} \underline{C} D\}$$

$$\{A\}^+ = \{A \underline{B} \underline{C} \underline{D} E\}$$

Thus. $A \rightarrow DE$ is correct,

Therefore, the decomposition of R is lossless

#2

A	B	C	FD:
a_1	b_1	c_2	$A \rightarrow B$
a_1	b_1	c_2	$C \rightarrow B$
a_2	b_1	c_1	
a_2	b_1	c_3	$AC \rightarrow B$

$$A \rightarrow B ?$$

答：能，因为 A 只能指向同样的 B.

$$A \rightarrow B ? \quad \checkmark$$

$$\begin{array}{l} a_1 \rightarrow b_1 \\ a_2 \rightarrow b_1 \end{array}$$

$$A \rightarrow C ?$$

$$\begin{array}{l} a_2 \rightarrow c_1 \\ a_2 \rightarrow c_3 \end{array} \quad \times$$

$$B \rightarrow A ?$$

$$\begin{array}{l} b_1 \rightarrow a_1 \\ b_1 \rightarrow a_2 \end{array} \quad \times$$

$$B \rightarrow C ?$$

$$\begin{array}{l} b_1 \rightarrow c_1 \\ b_1 \rightarrow c_2 \\ b_1 \rightarrow c_3 \end{array} \quad \times$$

$$C \rightarrow A ?$$

$$\begin{array}{l} c_1 \rightarrow a_2 \\ c_2 \rightarrow a_1 \\ c_3 \rightarrow a_2 \end{array} \quad \checkmark$$

$$C \rightarrow B ?$$

$$\begin{array}{l} c_1 \rightarrow b_1 \\ c_2 \rightarrow b_1 \\ c_3 \rightarrow b_1 \end{array} \quad \checkmark$$

$$A B \rightarrow C ?$$

$$\begin{array}{l} a_1 b_1 \rightarrow c_2 \\ a_2 b_1 \rightarrow c_1 \\ \quad \quad \quad \boxed{c_3} \end{array} \quad \times$$

$$A C \rightarrow B ?$$

$$\begin{array}{l} a_1 c_2 \rightarrow b_1 \\ a_2 c_1 \rightarrow b_1 \\ a_2 c_3 \rightarrow b_1 \end{array} \quad \checkmark$$

$$B C \rightarrow A ?$$

$$\begin{array}{l} b_1 c_2 \rightarrow a_1 \\ b_1 c_1 \rightarrow a_2 \\ b_1 c_3 \rightarrow a_2 \end{array} \quad \checkmark$$

$$A \rightarrow B C ?$$

$$\begin{array}{l} a_1 \rightarrow b_1 c_2 \\ a_2 \rightarrow c_1 c_3 \end{array} \quad \times$$

$$B \rightarrow A C ?$$

$$\begin{array}{l} b_1 \rightarrow c_2 \\ b_1 \rightarrow c_2 \\ \quad \quad \quad \boxed{c_3} \end{array} \quad \times$$

$$C \rightarrow A B ?$$

$$\begin{array}{l} c_1 \rightarrow a_2 b_1 \\ c_2 \rightarrow a_1 b_1 \\ c_3 \rightarrow a_2 b_1 \end{array} \quad \checkmark$$

FD:

$$\begin{array}{l} A \rightarrow B \\ C \rightarrow A \\ C \rightarrow B \\ AC \rightarrow B \\ BC \rightarrow A \\ C \rightarrow AB \end{array}$$

Completely Non-trivial.

$$\begin{array}{l} AB \rightarrow B \\ A \ B \rightarrow A \\ A \rightarrow A \end{array}$$

trivial FD

Hw4 q3 tp be done

#3. Student .
Class .

Take(sid , dept. cnum)

(a). One - to - One . relationship exists between .

Student . and class . $\boxed{\begin{matrix} \text{sid} \rightarrow \text{dept}, \text{cnum} \\ \text{dept}, \text{cnum} \rightarrow \text{sid} \end{matrix}}$

(b) many - to - one relationship exists between .

Student . and class . $\boxed{\text{sid} \rightarrow \text{dept}, \text{cnum}}$

~~#4~~

FD: $A \rightarrow BC$. $CD \rightarrow E$ $B \rightarrow D$ $E \rightarrow A$

a): Is A a key for R ? $A \rightarrow R$?
Logical implication.

I use Canonical database to solve it:

Yes. $A \rightarrow R(A B C D E)$

<u>R</u>	<u>A</u>	<u>B</u>	<u>C</u>	<u>D</u>	<u>E</u>
<u>u₁</u>	a ₁	b ₁	c ₁	d ₁	e ₁
<u>u₂</u>	a ₁	<u>b₁</u>	<u>c₁</u>	<u>d₁</u>	<u>e₁</u>
	<u>b₁</u>	<u>c₁</u>	<u>d₁</u>	<u>e₁</u>	?

b) Is BC a key for R?
 $BC \rightarrow R$?

<u>R</u>	<u>A</u>	<u>B</u>	<u>C</u>	<u>D</u>	<u>E</u>
<u>u₁</u>	a ₁	b ₁	c ₁	d ₁	e ₁
<u>u₂</u>	<u>a₁</u>	b ₁	c ₁	d ₁	e ₁
	<u>a₁</u>			<u>d₁</u>	<u>e₁</u>

FD: $A \rightarrow BC$. $CD \rightarrow E$ $B \rightarrow D$ $E \rightarrow A$

Hw4 q5

Assume FD hold for $R(A, B, C, D, E, F)$

$$\begin{aligned} FD: \quad A &\rightarrow BC \\ &C \rightarrow E \\ &B \rightarrow D. \end{aligned}$$

Is R is BCNF?

R is in BCNF iff. X contains a key, for
every $(X \rightarrow Y) \in FD$.

Answer: FDs are:

$$A \rightarrow BC \quad A \text{ contain a key?}$$

$$C \rightarrow E \quad C \text{ contain a key?}$$

$$B \rightarrow D. \quad B \text{ contain a key?}$$

$$\left. \begin{array}{l} \{A\}^+ = \{ABC\} \\ \{A\}^+ = \{ABCDEF\} \end{array} \right\} A \text{ doesn't contain a key.}$$

$$\left. \begin{array}{l} \{B\}^+ = \{BD\}. \end{array} \right\} B \text{ doesn't contain a key.}$$

$\{C\}^f = \{CE\}$ } C doesn't contain a key.

BCNF Decomposition Algorithm

Decompose R into $R_1(X^+)$ and $R_2(X, Z)$

X is the common attribute

Z is all attr except X^+

Step 1: $A \rightarrow BC$.

$$\{A\}^f = \{ABC DE\}$$

$R_1(ABCDE) \quad R_2(AF)$

Step 2: $C \rightarrow E$

$$\{C\}^f = \{CE\}$$

$R_3(CE)$ $R_4(C, AB \& D \notin F)$

$R_4(A, B, C, D, F)$

Step 3: $B \rightarrow D$

$$\{B\}^f = \{BD\}$$

$R_5(B, D)$

$R_6(A, B, C, E, F)$

Hw4 q6 to be done

(a) CHECK . (weight > 0 kg AND weight \leq 5 kg)

(b) CREATE TRIGGER

BEFORE INSERT on Laptop.

UPDATE Laptop SET weight = NULL.

WHEN weight \geq 5 OR weight < 0

Hw4 q8

#8:

A	B
1	0
1	9
(1) 0	0