

# CS143 Homework#1:

1. Suppose relation  $R(A, B, C)$  has the tuples:

| A | B | C |
|---|---|---|
| 7 | 5 | 3 |
| 2 | 1 | 2 |
| 1 | 4 | 3 |
| 5 | 8 | 7 |
| 6 | 7 | 9 |

and relation  $S(A, B, C)$  has the tuples:

| A | B | C |
|---|---|---|
| 2 | 1 | 2 |
| 1 | 4 | 4 |
| 8 | 3 | 2 |
| 5 | 8 | 7 |

Compute  $(R - S) \cup (S - R)$ , often called the “symmetric difference” of  $R$  and  $S$ . List all the tuples in the result relation.

Answer:

$(R - S)$  has the tuples:

| A | B | C |
|---|---|---|
| 7 | 5 | 3 |
| 1 | 4 | 3 |
| 6 | 7 | 9 |

$(S - R)$  has the tuples:

| A | B | C |
|---|---|---|
| 1 | 4 | 4 |
| 8 | 3 | 2 |

$(R - S) \cup (S - R)$  has the tuples:

| A | B | C |
|---|---|---|
| 7 | 5 | 5 |
| 1 | 4 | 3 |
| 6 | 7 | 9 |
| 1 | 4 | 4 |
| 8 | 3 | 4 |

2. Suppose relation  $R(L, M)$  has the tuples:

| L | M |
|---|---|
| 4 | 3 |
| 6 | 5 |
| 8 | 7 |

and relation  $S(M, N, P)$  has the tuples:

| M | N | P |
|---|---|---|
| 6 | 1 | 8 |
| 1 | 6 | 4 |
| 2 | 5 | 1 |
| 3 | 4 | 7 |

Compute  $\sigma_{R.L > S.M \wedge R.M < S.P}(R \times S)$ . List all the tuples in the result relation.

$(R \times S)$  has the tuples:

| L | R.M | S.M | N | P |
|---|-----|-----|---|---|
| 4 | 3   | 6   | 1 | 8 |
| 4 | 3   | 1   | 6 | 4 |
| 4 | 3   | 2   | 5 | 1 |
| 4 | 3   | 3   | 4 | 7 |
| 6 | 5   | 6   | 1 | 8 |
| 6 | 5   | 1   | 6 | 4 |
| 6 | 5   | 2   | 5 | 1 |
| 6 | 5   | 3   | 4 | 7 |
| 8 | 7   | 6   | 1 | 8 |
| 8 | 7   | 1   | 6 | 4 |
| 8 | 7   | 2   | 5 | 1 |
| 8 | 7   | 3   | 4 | 7 |

$\sigma_{R.L > S.M \wedge R.M < S.P}(R \times S)$  has the tuples:

| L | R.M | S.M | N | P |
|---|-----|-----|---|---|
| 4 | 3   | 1   | 6 | 4 |
| 4 | 3   | 3   | 4 | 7 |
| 6 | 5   | 3   | 4 | 7 |
| 8 | 7   | 6   | 1 | 8 |

Problem3:

$$\Pi_{i.ID, i.name} ((\sigma_{i.salary > w.salary} (Q_i(instructor) \times \sigma_{w.id=12121} (Q_w(instructor)))))$$
$$\sigma_{dept\_name = \text{“Physics”}}(instructor \bowtie_{instructor.ID=teaches.ID} teaches)$$
$$(\sigma_{deptname = \text{“Physics”}}(instructor)) \bowtie_{instructor.ID=teaches.ID} teaches$$
$$\sigma_{deptname = \text{building}}(department)$$
$$Student \bowtie_{Student.Student-name=Enrollment.Student-name} Enrollment$$

a). Find the names of all students who are not enrolled in the ‘Database Management Systems’ course.

$$\Pi_{Student-name} (Student) - \Pi_{Student-name} ( \sigma_{Course-name = \text{“Database Management Systems”}} (Enrollment) )$$

b). Find the names of all students who are enrolled in at least one course not offered by their home department.

*Student\_Enrolled*  $\leftarrow$  *Student*  $\bowtie_{Student.Student-name=Enrollment.Student-name}$  *Enrollment*

// Result schema is :

// *Student\_Enrolled*(*Student.Student-name*, *Department*, *Enrollment.Student-name*, *Course-name* )

*Result2*  $\leftarrow$  *Student\_Enrolled*  $\bowtie_{Result1.Course-name=Course.Course-name}$  *Course*

// Result schema is:

// *Result2* ( *Student.Student-name*, *Student\_Enrolled.Department*, *Enrollment.Student-name*, *Student\_Enrolled.Course-name*, *Course.Course-name*, *Course.Department* )

$\Pi_{Student.Student-name}(\sigma_{Student\_Enrolled.Department \neq Course.Department}(Result2))$

c). Find the names of all courses which have no students enrolled.

$\Pi_{Course-name}(Course) - \Pi_{Course-name}(Enrollment)$

d). Find the department names that students belong to if the students takes at least one class offered by the CS department.

$\Pi_{\text{Student.Student-name, Student\_Enrolled.Department}}(\sigma_{\text{Course.Department} = \text{"CS"}}(\text{Result2}))$

e). Find the department names of all students who are enrolled in at most one course.

$\text{Result\_e1} \leftarrow \text{Enrollment} \times \rho_{\text{Enrollment2}}(\text{Enrollment})$

$\text{Result\_e2} \leftarrow \sigma_{\text{Enrollment.Student-name} = \text{Enrollment2.Student-name} \text{ AND } \text{Enrollment.Course-name} \neq \text{Enrollment2.Course-name}}(\text{Result\_e1})$

// Student who are taking more than 1 course:

$\text{Result\_e3} \leftarrow \rho_{\text{Student\_taking\_more\_than\_one}}(\text{Student-name})(\Pi_{\text{Enrollment.Student-name}} \text{Result\_e2})$

$\text{Result\_e3} \leftarrow \text{Result\_e3} \bowtie_{\text{Result\_e3.Student-name} = \text{Student.Student-name}} \text{Student}$

$\rho_{\text{Student\_taking\_more\_than\_one\_course}}(\text{Student-name, Department})(\Pi_{\text{Student.Student-name, Department}})$

$\text{Final\_relation} \leftarrow \text{Student} - \text{Student\_taking\_more\_than\_one\_course}$

#4.

$\rho_{Company2}(Company)$

$Not\_Cheapest\_Companies \leftarrow \Pi_{Company.company-name}(\sigma_{Company.company-name > Company2.company-name} (Company \times Company2))$

$Cheapest\_Company = \Pi_{company-name}(Company) - Not\_Cheapest\_Companies$