

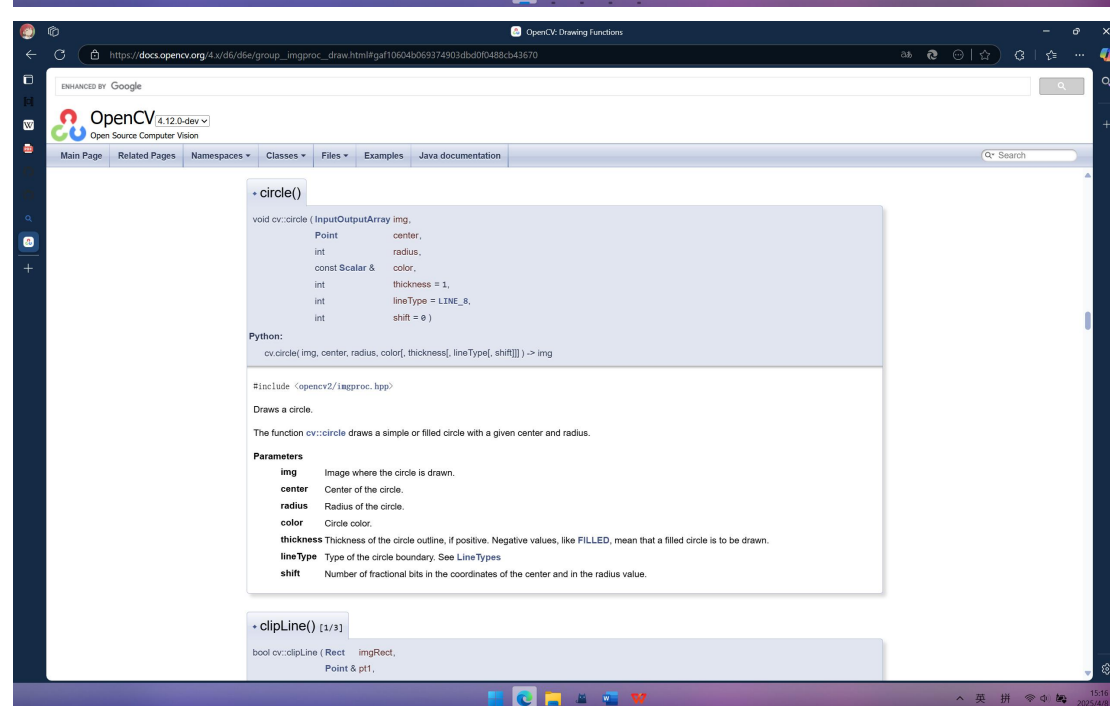
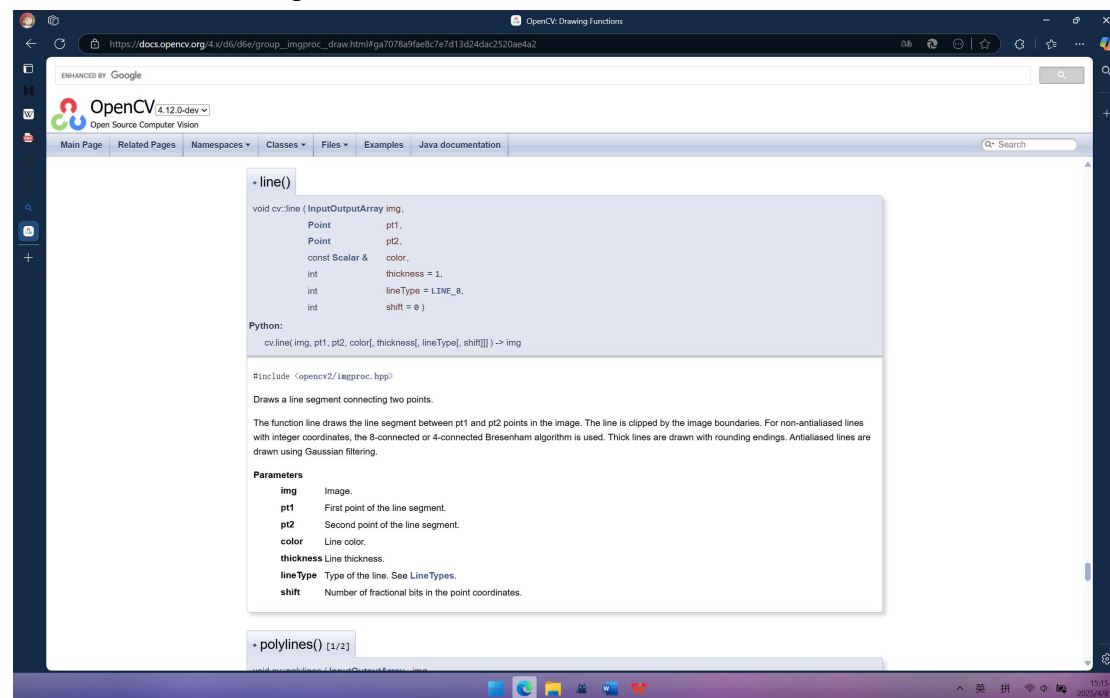
计算机学院实验报告

实验题目： Catmull-Clark 细分		学号： 202300130183
日期： 2025/4/7	班级： 23 级智能班	姓名： 宋浩宇
Email: 2367651943@qq.com 202300130183@mail.sdu.edu.cn zhitian0420@gmail.com		
实验目的: 希望同学们通过本实验锻炼系统能力，实验具体模块如下： 1， 功能模块： 数据录入， 数据结构、 细分算法、 可视呈现； 2， 数据录入： obj 格式， 实现基本的文件读写功能； 3， 数据结构： 就是一个图结构， 点和边分别存储， 需要用到查询一邻域的方法； 4， 细分算法： Catmull 细分方法； 5， 可视呈现： 基于 opencv 绘制线段， 在二维屏幕上呈现细分的迭代过程， 或其他任何可视化手段（libigl, matlab, 等等都可以）；		
实验环境介绍: 软件环境: 主系统： Windows 11 家庭中文版 23H2 22631.4317 虚拟机软件： Oracle Virtual Box 7.1.6 虚拟机系统： Ubuntu 18.04.2 LTS 编辑器： Visual Studio Code 编译器： gcc 7.3.0 计算框架： Eigen 3.3.7 硬件环境: CPU： 13th Gen Intel(R) Core(TM) i9-13980HX 2.20 GHz 内存： 32.0 GB (31.6 GB 可用) 磁盘驱动器： NVMe WD_BLACKSN850X2000GB 显示适配器： NVIDIA GeForce RTX 4080 Laptop GPU		

解决问题的主要思路：

本实验的解决思路如下：

首先我们需要熟悉 opencv 提供的绘制点和直线和函数：



这决定了我们把结果可视化的方式。

然后就是 Catmull-Clark 算法实现的具体方式了。

Catmull-Clark 算法可以概括为以下几个步骤：

1. 计算面点。
2. 计算边点。
3. 更新原有点。
4. 用新点构成新的边和面。

5. 更新全局点集、边集、面集。

我们依次来讲这些部分都是怎么计算的。

1. 计算面点

对于每一个面 F ，假设构成这个面的点集合为 $\{x|x \in F\}$ ，那我们的面点 P_F 就是：

$$P_{F_i} = \frac{1}{n} \sum_{i=1}^n x_i$$

2. 计算边点

对于每一个边 E ，假设构成这个边的点集合为 $\{x|x \in E\}$ ，和这个边相邻的面为 $\{F|E \in F\}$ ，易得面最多有两个。我们用 P_{Em} 表示这个边的中点，那我们可以得到边点：

$$P_{E_i} = \frac{\frac{P_{F_1} + P_{F_2}}{2} + P_{Em_i}}{2}$$

3. 更新原有点

对于每一个点，我们可以得到它相邻的面和边，分别为 $\{F|P \in F\}$ 、 $\{E|P \in E\}$

为了方便公式的书写，我们使用 F 表示和它相邻的面的面点的均值，用 R 表示和它相邻的边的中点的均值，用公式表示为：

$$F = \frac{\sum_{i=1}^n P_{F_i}}{n}$$
$$R = \frac{\sum_{i=1}^n P_{Em_i}}{n}$$

4. 构成新的面

用更新后的点、面点、边点构成新的面。

实验步骤与实验结果：

首先是实现 OBJ 文件数据的输入。

我们将程序写为了可以通过启动参数来设置导入的文件。

然后为了绘制出来的点能够看起来更清楚，我们给这些点都设置上 `scale` 和 `offset`，以便于将点绘制在画布靠中间的位置并且能让他们不至于距离太近。

然后就是实现 Catmull-Clark 细分算法。

然后为了让程序更灵活一些，我们加入可调整读入文件的部分，以及可以控制细分次数的部分。

以下为代码：

```
#include <algorithm>
#include <cstdlib>
#include <cstring>
#include <ctime>
```

```
#include <fstream>
#include <iostream>
#include <opencv2/highgui.hpp>
#include <opencv2/opencv.hpp>
#include <ostream>
#include <sstream>
#include <stddef.h>
#include <string>
#include <vector>
using namespace cv;

class my_point
{
public:
    double x, y;
    size_t v_id;
};

class my_edge
{
public:
    size_t edge_id;
    size_t v1_id, v2_id;
};

class my_face
{
public:
    size_t face_id;
    std::vector<size_t> points;
    std::vector<size_t> edges;
};

std::vector<my_point> all_points;
std::vector<my_edge> all_edges;
std::vector<my_face> all_faces;
#define SCALE 200.0
#define OFFSET 100.0
// // 设置窗口
// // 注意 opencv 的坐标系原点在左上角
// Mat img = Mat::zeros(Size(800, 800), CV_8UC3);
// img.setTo(255); // 设置屏幕为白色
//
// Point p1(100, 100); // 点 p1
// Point p2(758, 50); // 点 p2
//
// // 画直线函数
```

```

// line(img, p1, p2, Scalar(0, 0, 255), 1); // 红色
// line(img, Point(300, 300), Point(758, 400), Scalar(0, 255,
255), 1); //
// 黄色
//
// // 画点 p1
// circle(img, p1, 3, Scalar(0, 255, 0), -1);
// // 画点 p2
// circle(img, p2, 3, Scalar(120, 120, sum 120), -1);
//
// imshow("画板", img);
// waitKey(0);
void read_file(const char* filename)
{
    std::ifstream file(filename);
    if (!file.is_open())
    {
        std::cout << "Error: cannot open file " << filename <<
std::endl;
        return;
    }
    size_t point_index = 0;
    size_t edge_index = 0;
    size_t face_index = 0;

```

```

char type;
while (file >> type)
{
    if (type == 'v')
    {
        my_point p;
        point_index++;
        file >> p.x >> p.y;
        p.v_id = point_index;
        p.x *= SCALE;
        p.y *= SCALE;
        p.x += OFFSET;
        p.y += OFFSET;
        all_points.push_back(p);
    }
    if (type == 'e')
    {
        my_edge e;
        edge_index++;
    }
}

```

```

    file >> e.v1_id >> e.v2_id;
    e.edge_id = edge_index;
    all_edges.push_back(e);
}
if (type == 'f')
{
    my_face f;
    face_index++;
    std::string str;
    std::getline(file, str);
    std::stringstream ss(str);
    // size_t v1, v2, v3, v4;
    // file >> v1 >> v2 >> v3 >> v4;
    // f.face_id = face_index;
    // f.points.push_back(v1);
    // f.points.push_back(v2);
    // f.points.push_back(v3);
    // f.points.push_back(v4);
    // for (auto& i : all_edges)
    // {
    //     if (i.v1_id == v1 && i.v2_id == v2)
    //     {
    //         f.edges.push_back(i.edge_id);
    //     }
    //     if (i.v1_id == v2 && i.v2_id == v3)
    //     {
    //         f.edges.push_back(i.edge_id);
    //     }
    //     if (i.v1_id == v3 && i.v2_id == v4)
    //     {
    //         f.edges.push_back(i.edge_id);
    //     }
    //     if (i.v1_id == v4 && i.v2_id == v1)
    //     {
    //         f.edges.push_back(i.edge_id);
    //     }
    // }
    f.face_id = face_index;
    size_t buf;
    while (ss >> buf)
    {
        // std::cout << buf << std::endl;
        f.points.push_back(buf);
    }
}

```

```

        for (size_t i = 0; i < f.points.size(); i++)
        {
            auto edge = std::find_if(
                all_edges.begin(), all_edges.end(),
                [f, i](const my_edge& e)
                {
                    return (e.v1_id == f.points[i] &&
                        e.v2_id == f.points[(i + 1) %
f.points.size()]) ||
                        (e.v1_id == f.points[(i + 1) %
f.points.size()] &&
                        e.v2_id == f.points[i]);
                });
            f.edges.push_back(edge->edge_id);
        }
        all_faces.push_back(f);
    }
}

void draw_all(Mat& img)
{
    // 画点
    for (auto& i : all_points)
    {
        circle(img, Point(i.x, i.y), 3, Scalar(0, 255, 0), -1);
    }
    // 画边
    for (auto& i : all_edges)
    {
        auto point_1 =
            std::find_if(all_points.begin(), all_points.end(),
                [i](const my_point& p) { return p.v_id ==
i.v1_id; });
        auto point_2 =
            std::find_if(all_points.begin(), all_points.end(),
                [i](const my_point& p) { return p.v_id ==
i.v2_id; });
        line(img, Point(point_1->x, point_1->y),
Point(point_2->x, point_2->y),
            Scalar(0, 0, 255), 1);
    }
    // 画面
}

void display_all()

```

```

{
    for (auto& i : all_points)
    {
        std::cout << "点" << i.v_id << "(" << i.x << "," << i.y <<
        ")" << std::endl;
    }
    for (auto& i : all_edges)
    {
        std::cout << "边" << i.edge_id << "(" << i.v1_id << "," <<
        i.v2_id << ")"
        << std::endl;
    }
    for (auto& i : all_faces)
    {
        std::cout << "面" << i.face_id << std::endl;
        for (auto& j : i.points)
        {
            std::cout << "点" << j << " " << std::endl;
        }
        for (auto& j : i.edges)
        {
            std::cout << "边" << j << " " << std::endl;
        }
    }
}

void display_faces(std::vector<my_face>& faces)
{
    std::cout << "共有" << faces.size() << "个面" << std::endl;
    for (auto& i : faces)
    {
        std::cout << "面" << i.face_id << std::endl;
        std::cout << "点" << i.points.size() << std::endl;
        for (auto& j : i.points)
        {
            auto point = std::find_if(all_points.begin(),
all_points.end(),
[j](const my_point& p) { return
p.v_id == j; });
            std::cout << "(" << point->x << "," << point->y << ")"
<< std::endl;
        }
        std::cout << "边" << i.edges.size() << std::endl;
        for (auto& j : i.edges)
        {

```



```

        auto edge =
            std::find_if(all_edges.begin(), all_edges.end(),
                [j](const my_edge& e) { return e.edge_id
== j; });
        std::cout << "(" << edge->v1_id << "," << edge->v2_id <<
        ")" << std::endl;
    }
}

void display_points(Mat& img, std::vector<my_point>& points)
{
    std::srand(std::time(0));
    double r = std::rand() % 256;
    double g = std::rand() % 256;
    double b = std::rand() % 256;
    for (auto& i : points)
    {
        circle(img, Point(i.x, i.y), 3, Scalar(b, g, r), -1);
    }
}

void bind_edges()
{
    for (auto& f : all_faces)
    {
        for (size_t i = 0; i < f.points.size(); i++)
        {
            auto edge = std::find_if(
                all_edges.begin(), all_edges.end(),
                [f, i](const my_edge& e)
                {
                    return (e.v1_id == f.points[i] &&
                        e.v2_id == f.points[(i + 1) %
f.points.size()]) ||
                        (e.v1_id == f.points[(i + 1) %
f.points.size()] &&
                        e.v2_id == f.points[i]);
                });
            f.edges.push_back(edge->edge_id);
        }
    }
}

void catmull_clark()
{
    // 面点

```

```

std::vector<my_point> face_points;
for (auto& i : all_faces)
{
    double sum_x = 0.0;
    double sum_y = 0.0;
    size_t cnt = i.points.size();
    for (auto& j : i.points)
    {
        auto point = std::find_if(all_points.begin(),
all_points.end(),
                                [j](const my_point& p) { return
p.v_id == j; });
        sum_x += point->x;
        sum_y += point->y;
    }
    my_point p;
    p.x = sum_x / cnt;
    p.y = sum_y / cnt;
    p.v_id = i.face_id;
    face_points.push_back(p);
}
// std::cout << face_points.size() << std::endl;
// for (auto& i : face_points)
// {
//     std::cout << "点" << i.v_id << "(" << i.x << "," << i.y
<< ")" <<
//     std::endl;
// }
// 边中点
std::vector<my_point> edge_avg_points;
for (auto& i : all_edges)
{
    auto point_1 =
        std::find_if(all_points.begin(), all_points.end(),
                    [i](const my_point& p) { return p.v_id ==
i.v1_id; });
    auto point_2 =
        std::find_if(all_points.begin(), all_points.end(),
                    [i](const my_point& p) { return p.v_id ==
i.v2_id; });
    my_point p;
    p.x = (point_1->x + point_2->x) / 2.0;
    p.y = (point_1->y + point_2->y) / 2.0;
    p.v_id = i.edge_id;
}

```

```

    edge_avg_points.push_back(p);
}
// 边点
std::vector<my_point> edge_points;
for (auto& i : all_edges)
{
    auto start = all_faces.begin();
    my_point sum;
    size_t cnt = 0;
    auto face_1 = std::find_if(
        start, all_faces.end(),
        [i](const my_face& f)
        {
            return find_if(f.edges.begin(), f.edges.end(),
[i](const size_t& e)
                        { return e == i.edge_id; }) !=
f.edges.end();
        });
    start = face_1 + 1;
    auto face_2 = std::find_if(
        start, all_faces.end(),
        [i](const my_face& f)
        {
            return find_if(f.edges.begin(), f.edges.end(),
[i](const size_t& e)
                        { return e == i.edge_id; }) !=
f.edges.end();
        });
    if (face_1 != all_faces.end())
    {
        auto point = std::find_if(face_points.begin(),
face_points.end(),
                                [face_1](const my_point& p)
                                { return p.v_id ==
face_1->face_id; });
        // std::cout << "面的中点" << face_1->face_id << "(" <<
point->x << ","
        // << point->y << ")" << std::endl;
        sum.x = point->x;
        sum.y = point->y;
        cnt++;
    }
    if (face_2 != all_faces.end())
    {

```

```

        auto point = std::find_if(face_points.begin(),
face_points.end(),
                                [face_2](const my_point& p)
                                { return p.v_id ==
face_2->face_id; });
        // std::cout << "面的中点" << face_2->face_id << "(" <<
point->x << ","
        //          << point->y << ")" << std::endl;
        sum.x += point->x;
        sum.y += point->y;
        cnt++;
    }
    sum.x /= cnt;
    sum.y /= cnt;
    sum.x *= 0.5;
    sum.y *= 0.5;
    sum.x +=
        std::find_if(edge_avg_points.begin(),
edge_avg_points.end(),
                    [i](const my_point& e) { return i.edge_id
== e.v_id; })
        ->x *
        0.5;
    sum.y +=
        std::find_if(edge_avg_points.begin(),
edge_avg_points.end(),
                    [i](const my_point& e) { return i.edge_id
== e.v_id; })
        ->y *
        0.5;
    sum.v_id = i.edge_id;
    edge_points.push_back(sum);
}
// 更新点坐标
std::vector<my_point> new_points;
for (auto& i : all_points)
{
    // 接触的面的个数
    long long n = 0;
    std::vector<my_face> faces;
    for (auto& j : all_faces)
    {
        if (std::find_if(j.points.begin(), j.points.end(),
[i](const size_t& p)

```

```

        { return p == i.v_id; }) !=
j.points.end())
    {
        n++;
        faces.push_back(j);
    }
}
// std::cout << "点" << i.v_id << "接触面的个数" << n <<
std::endl;
// 面点均值
my_point face_sum;
face_sum.x = 0.0;
face_sum.y = 0.0;
for (auto& j : faces)
{
    auto point =
        *std::find_if(face_points.begin(),
face_points.end(),
[j](const my_point& p) { return p.v_id
== j.face_id; });
    face_sum.x += point.x;
    face_sum.y += point.y;
    // std::cout << "面的点" << j.face_id << "(" << point.x
<< "," << point.y
    // << ")" << std::endl;
}
face_sum.x /= n * 1.0;
face_sum.y /= n * 1.0;
// std::cout << "面的中点" << face_sum.v_id << "(" <<
face_sum.x << ","
// << face_sum.y << ")" << std::endl;
// 边中点均值
my_point edge_sum;
edge_sum.x = 0.0;
edge_sum.y = 0.0;
long long cnt = 0;
std::vector<my_edge> edges;
for (auto& j : all_edges)
{
    if (j.v1_id == i.v_id || j.v2_id == i.v_id)
    {
        edges.push_back(j);
        cnt++;
    }
}

```

```

    }
    for (auto& j : edges)
    {
        auto point =
            *std::find_if(edge_avg_points.begin(),
edge_avg_points.end(),
                        [j](const my_point& p) { return p.v_id
== j.edge_id; });
        edge_sum.x += point.x;
        edge_sum.y += point.y;
    }
    edge_sum.x /= cnt * 1.0;
    edge_sum.y /= cnt * 1.0;
    // std::cout << "边的中点" << edge_sum.v_id << "(" <<
edge_sum.x << "," <<
    //          << edge_sum.y << ")" << std::endl;
    // 新的点坐标
    my_point new_point;
    // std::cout << "旧的点" << i.v_id << "(" << i.x << "," <<
i.y << ")" <<
    //          << std::endl;
    new_point.x = (n - 3) * i.x + 2.0 * edge_sum.x + face_sum.x;
    new_point.y = (n - 3) * i.y + 2.0 * edge_sum.y + face_sum.y;
    new_point.x /= n * 1.0;
    new_point.y /= n * 1.0;
    new_point.v_id = i.v_id;
    // std::cout << "新的点" << new_point.v_id << "(" <<
new_point.x << "," <<
    //          << new_point.y << ")" << std::endl;
    if (cnt != n)
    {
        new_point.x = i.x;
        new_point.y = i.y;
    }
    new_points.push_back(new_point);
}
// for (auto& i : new_points)
// {
//     std::cout << "新的点" << i.v_id << "(" << i.x << "," <<
i.y << ")" <<
//         << std::endl;
// }
// for (auto& i : all_points)
// {

```

```

    //  std::cout << "旧的点" << i.v_id << "(" << i.x << "," <<
i.y << ")"
    //          << std::endl;
    // }
    // for (auto& i : all_faces)
    // {
    //     std::cout << "面的点的索引" << i.face_id << std::endl;
    //     for (auto& j : i.points)
    //     {
    //         std::cout << j << " ";
    //     }
    //     std::cout << std::endl;
    // }
    // for (auto& i : face_points)
    // {
    //     std::cout << "面点" << i.v_id << "(" << i.x << "," << i.y
    << ")"
    //         << std::endl;
    // }
    // Mat img = Mat::zeros(Size(800, 800), CV_8UC3);
    // img.setTo(255); // 设置屏幕为白色
    // display_points(img, new_points);
    // display_points(img, face_points);
    // display_points(img, edge_points);
    // imshow("花瓣", img);
    // waitKey(0);
    // 更新点边和面, 按面更新
    std::vector<my_point> new_points_tmp;
    std::vector<my_edge> new_edges;
    std::vector<my_face> new_faces;
    new_points_tmp.push_back(all_points[0]);
    new_faces.push_back(all_faces[0]);
    new_edges.push_back(all_edges[0]);

```

```

for (auto& i : all_faces)
{
    if (i.points.size() == 4)
    {
        auto point_1 = *std::find_if(new_points.begin(),
new_points.end(),
                                [i](const my_point& p)
                                { return p.v_id ==
i.points[0]; });
        auto point_2 = *std::find_if(new_points.begin(),

```

```

new_points.end(),
                                [i](const my_point& p)
                                { return p.v_id ==
i.points[1]; });
    auto point_3 = *std::find_if(new_points.begin(),
new_points.end(),
                                [i](const my_point& p)
                                { return p.v_id ==
i.points[2]; });
    auto point_4 = *std::find_if(new_points.begin(),
new_points.end(),
                                [i](const my_point& p)
                                { return p.v_id ==
i.points[3]; });
    // std::cout << "四边形面" << i.face_id << std::endl;
    // std::cout << "point_1:" << "(" << point_1.x << "," <<
point_1.y << ")"
    // << std::endl;
    // std::cout << "point_2:" << "(" << point_2.x << "," <<
point_2.y << ")"
    // << std::endl;
    // std::cout << "point_3:" << "(" << point_3.x << "," <<
point_3.y << ")"
    // << std::endl;
    // std::cout << "point_4:" << "(" << point_4.x << "," <<
point_4.y << ")"
    // << std::endl;
    auto edge_1_2_index = *std::find_if(
        all_edges.begin(), all_edges.end(),
        [point_1, point_2](const my_edge& e)
        {
            return (e.v1_id == point_1.v_id && e.v2_id ==
point_2.v_id) ||
                (e.v1_id == point_2.v_id && e.v2_id ==
point_1.v_id);
        });
    auto edge_point_1_2 =
        *std::find_if(edge_points.begin(),
edge_points.end(),
                        [edge_1_2_index](const my_point& p)
                        { return p.v_id ==
edge_1_2_index.edge_id; });
    auto edge_2_3_index = *std::find_if(
        all_edges.begin(), all_edges.end(),

```



```

        [point_2, point_3](const my_edge& e)
        {
            return (e.v1_id == point_2.v_id && e.v2_id ==
point_3.v_id) ||
                (e.v1_id == point_3.v_id && e.v2_id ==
point_2.v_id);
        });
        auto edge_point_2_3 =
            *std::find_if(edge_points.begin(),
edge_points.end(),
                [edge_2_3_index](const my_point& p)
                { return p.v_id ==
edge_2_3_index.edge_id; });
        auto edge_3_4_index = *std::find_if(
            all_edges.begin(), all_edges.end(),
            [point_3, point_4](const my_edge& e)
            {
                return (e.v1_id == point_3.v_id && e.v2_id ==
point_4.v_id) ||
                    (e.v1_id == point_4.v_id && e.v2_id ==
point_3.v_id);
            });
        auto edge_point_3_4 =
            *std::find_if(edge_points.begin(),
edge_points.end(),
                [edge_3_4_index](const my_point& p)
                { return p.v_id ==
edge_3_4_index.edge_id; });
        auto edge_4_1_index = *std::find_if(
            all_edges.begin(), all_edges.end(),
            [point_4, point_1](const my_edge& e)
            {
                return (e.v1_id == point_4.v_id && e.v2_id ==
point_1.v_id) ||
                    (e.v1_id == point_1.v_id && e.v2_id ==
point_4.v_id);
            });
        auto edge_point_4_1 =
            *std::find_if(edge_points.begin(),
edge_points.end(),
                [edge_4_1_index](const my_point& p)
                { return p.v_id ==
edge_4_1_index.edge_id; });
        auto face_point =

```

```

        *std::find_if(face_points.begin(),
face_points.end(),
                    [i](const my_point& p) { return p.v_id
== i.face_id; });
    point_1.v_id = new_points_tmp.size();
    new_points_tmp.push_back(point_1);
    point_2.v_id = new_points_tmp.size();
    new_points_tmp.push_back(point_2);
    point_3.v_id = new_points_tmp.size();
    new_points_tmp.push_back(point_3);
    point_4.v_id = new_points_tmp.size();
    new_points_tmp.push_back(point_4);
    edge_point_1_2.v_id = new_points_tmp.size();
    new_points_tmp.push_back(edge_point_1_2);
    edge_point_2_3.v_id = new_points_tmp.size();
    new_points_tmp.push_back(edge_point_2_3);
    edge_point_3_4.v_id = new_points_tmp.size();
    new_points_tmp.push_back(edge_point_3_4);
    edge_point_4_1.v_id = new_points_tmp.size();
    new_points_tmp.push_back(edge_point_4_1);
    face_point.v_id = new_points_tmp.size();
    new_points_tmp.push_back(face_point);
    my_face new_face_1;
    my_face new_face_2;
    my_face new_face_3;
    my_face new_face_4;
    my_edge new_edge_1_1;
    my_edge new_edge_1_2;
    my_edge new_edge_1_3;
    my_edge new_edge_1_4;
    my_edge new_edge_2_1;
    my_edge new_edge_2_2;
    my_edge new_edge_2_3;
    my_edge new_edge_2_4;
    my_edge new_edge_3_1;
    my_edge new_edge_3_2;
    my_edge new_edge_3_3;
    my_edge new_edge_3_4;
    my_edge new_edge_4_1;
    my_edge new_edge_4_2;
    my_edge new_edge_4_3;
    my_edge new_edge_4_4;
    // 面1(a,edge_point_ab,face_point,edge_point_da)
    // 边1(a,edge_point_ab)

```

```
new_edge_1_1.v1_id = point_1.v_id;
new_edge_1_1.v2_id = edge_point_1_2.v_id;
// 边2(edge_point_ab,face_point)
new_edge_1_2.v1_id = edge_point_1_2.v_id;
new_edge_1_2.v2_id = face_point.v_id;
// 边3(face_point,edge_point_da)
new_edge_1_3.v1_id = face_point.v_id;
new_edge_1_3.v2_id = edge_point_4_1.v_id;
// 边4(edge_point_da,a)
new_edge_1_4.v1_id = edge_point_4_1.v_id;
new_edge_1_4.v2_id = point_1.v_id;
// 新增边
new_edge_1_1.edge_id = new_edges.size();
new_edges.push_back(new_edge_1_1);
new_edge_1_2.edge_id = new_edges.size();
new_edges.push_back(new_edge_1_2);
new_edge_1_3.edge_id = new_edges.size();
new_edges.push_back(new_edge_1_3);
new_edge_1_4.edge_id = new_edges.size();
new_edges.push_back(new_edge_1_4);
```

```
// 新增面
new_face_1.points = {point_1.v_id, edge_point_1_2.v_id,
                    edge_point_4_1.v_id};
// new_face_1.edges = {new_edge_1_1.edge_id,
new_face_1.edges = {new_face_1_2.edge_id,
                    new_face_1_3.edge_id, new_face_1_4.edge_id};
new_face_1.face_id = new_faces.size();
new_faces.push_back(new_face_1);
```

```
// 面2(b,edge_point_bc,face_point,edge_point_ab)
// 边1(b,edge_point_bc)
new_edge_2_1.v1_id = point_2.v_id;
new_edge_2_1.v2_id = edge_point_2_3.v_id;
// 边2(edge_point_bc,face_point)
new_edge_2_2.v1_id = edge_point_2_3.v_id;
new_edge_2_2.v2_id = face_point.v_id;
// 边3(face_point,edge_point_ab)
new_edge_2_3.v1_id = face_point.v_id;
new_edge_2_3.v2_id = edge_point_1_2.v_id;
// 边4(edge_point_ab,b)
new_edge_2_4.v1_id = edge_point_1_2.v_id;
new_edge_2_4.v2_id = point_2.v_id;
```

```
// 新增边
```

```
new_edge_2_1.edge_id = new_edges.size();  
new_edges.push_back(new_edge_2_1);  
new_edge_2_2.edge_id = new_edges.size();  
new_edges.push_back(new_edge_2_2);  
new_edge_2_3.edge_id = new_edges.size();  
new_edges.push_back(new_edge_2_3);  
new_edge_2_4.edge_id = new_edges.size();  
new_edges.push_back(new_edge_2_4);
```

```
// 新增面
```

```
new_face_2.points = {point_2.v_id, edge_point_2_3.v_id,  
face_point.v_id,
```

```
edge_point_1_2.v_id};
```

```
// new_face_2.edges = {new_edge_2_1.edge_id,  
new_edge_2_2.edge_id,
```

```
// new_face_2.edges = {new_edge_2_1.edge_id,  
new_edge_2_2.edge_id,  
new_edge_2_3.edge_id,  
new_edge_2_4.edge_id};
```

```
new_face_2.face_id = new_faces.size();
```

```
new_faces.push_back(new_face_2);
```

```
// 面 3(c,edge_point_cd,face_point,edge_point_bc)
```

```
// 边 1(c,edge_point_cd)
```

```
new_edge_3_1.v1_id = point_3.v_id;
```

```
new_edge_3_1.v2_id = edge_point_3_4.v_id;
```

```
// 边 2(edge_point_cd,face_point)
```

```
new_edge_3_2.v1_id = edge_point_3_4.v_id;
```

```
new_edge_3_2.v2_id = face_point.v_id;
```

```
// 边 3(face_point,edge_point_bc)
```

```
new_edge_3_3.v1_id = face_point.v_id;
```

```
new_edge_3_3.v2_id = edge_point_2_3.v_id;
```

```
// 边 4(edge_point_bc,c)
```

```
new_edge_3_4.v1_id = edge_point_2_3.v_id;
```

```
new_edge_3_4.v2_id = point_3.v_id;
```

```
// 新增边
```

```
new_edge_3_1.edge_id = new_edges.size();
```

```
new_edges.push_back(new_edge_3_1);
```

```
new_edge_3_2.edge_id = new_edges.size();
```

```
new_edges.push_back(new_edge_3_2);
```

```
new_edge_3_3.edge_id = new_edges.size();
```

```
new_edges.push_back(new_edge_3_3);
```

```
new_edge_3_4.edge_id = new_edges.size();
```

```
new_edges.push_back(new_edge_3_4);
```

```
// 新增面
```

```
new_face_3.points = {point_3.v_id, edge_point_3_4.v_id,
```

```

face_point.v_id,
                                edge_point_2_3.v_id};
    // new_face_3.edges = {new_edge_3_1.edge_id,
new_edge_3_2.edge_id,
    // new_edge_3_3.edge_id, new_edge_3_4.edge_id};
    new_face_3.face_id = new_faces.size();
    new_faces.push_back(new_face_3);
    // 面4(d,edge_point_da,face_point,edge_point_cd)
    // 边1(d,edge_point_da)
    new_edge_4_1.v1_id = point_4.v_id;
    new_edge_4_1.v2_id = edge_point_4_1.v_id;
    // 边2(edge_point_da,face_point)
    new_edge_4_2.v1_id = edge_point_4_1.v_id;
    new_edge_4_2.v2_id = face_point.v_id;
    // 边3(face_point,edge_point_cd)
    new_edge_4_3.v1_id = face_point.v_id;
    new_edge_4_3.v2_id = edge_point_3_4.v_id;
    // 边4(edge_point_cd,d)
    new_edge_4_4.v1_id = edge_point_3_4.v_id;
    new_edge_4_4.v2_id = point_4.v_id;
    // 新增边
    new_edge_4_1.edge_id = new_edges.size();
    new_edges.push_back(new_edge_4_1);
    new_edge_4_2.edge_id = new_edges.size();
    new_edges.push_back(new_edge_4_2);
    new_edge_4_3.edge_id = new_edges.size();
    new_edges.push_back(new_edge_4_3);
    new_edge_4_4.edge_id = new_edges.size();
    new_edges.push_back(new_edge_4_4);
    // 新增面
    new_face_4.points = {point_4.v_id, edge_point_4_1.v_id,
face_point.v_id,
                                edge_point_3_4.v_id};
    // new_face_4.edges = {new_edge_4_1.edge_id,
new_edge_4_2.edge_id,
    // new_edge_4_3.edge_id, new_edge_4_4.edge_id};
    new_face_4.face_id = new_faces.size();
    new_faces.push_back(new_face_4);
    // std::cout << "新增边 new_edge_1_1:\n"
    //          << "\tfrom\t" << new_edge_1_1.v1_id <<
"\tto\t"
    //          << new_edge_1_1.v2_id << std::endl;
    // std::cout << "新增边 new_edge_1_2:\n"
    //          << "\tfrom\t" << new_edge_1_2.v1_id <<

```

```

"\tto\t"
//          << new_edge_1_2.v2_id << std::endl;
// std::cout << "新增边 new_edge_1_3:\n"
//          << "\tfrom\t" << new_edge_1_3.v1_id <<
"\tto\t"
//          << new_edge_1_3.v2_id << std::endl;
// std::cout << "新增边 new_edge_1_4:\n"
//          << "\tfrom\t" << new_edge_1_4.v1_id <<
"\tto\t"
//          << new_edge_1_4.v2_id << std::endl;
// std::cout << "新增边 new_edge_2_1:\n"
//          << "\tfrom\t" << new_edge_2_1.v1_id <<
"\tto\t"
//          << new_edge_2_1.v2_id << std::endl;
// std::cout << "新增边 new_edge_2_2:\n"
//          << "\tfrom\t" << new_edge_2_2.v1_id <<
"\tto\t"
//          << new_edge_2_2.v2_id << std::endl;
// std::cout << "新增边 new_edge_2_3:\n"
//          << "\tfrom\t" << new_edge_2_3.v1_id <<
"\tto\t"
//          << new_edge_2_3.v2_id << std::endl;
// std::cout << "新增边 new_edge_2_4:\n"
//          << "\tfrom\t" << new_edge_2_4.v1_id <<
"\tto\t"
//          << new_edge_2_4.v2_id << std::endl;
// std::cout << "新增边 new_edge_3_1:\n"
//          << "\tfrom\t" << new_edge_3_1.v1_id <<
"\tto\t"
//          << new_edge_3_1.v2_id << std::endl;
// std::cout << "新增边 new_edge_3_2:\n"
//          << "\tfrom\t" << new_edge_3_2.v1_id <<
"\tto\t"
//          << new_edge_3_2.v2_id << std::endl;
// std::cout << "新增边 new_edge_3_3:\n"
//          << "\tfrom\t" << new_edge_3_3.v1_id <<
"\tto\t"
//          << new_edge_3_3.v2_id << std::endl;
// std::cout << "新增边 new_edge_3_4:\n"
//          << "\tfrom\t" << new_edge_3_4.v1_id <<
"\tto\t"
//          << new_edge_3_4.v2_id << std::endl;
// std::cout << "新增边 new_edge_4_1:\n"
//          << "\tfrom\t" << new_edge_4_1.v1_id <<

```

```

"\tto\t"
    //          << new_edge_4_1.v2_id << std::endl;
    // std::cout << "新增边 new_edge_4_2:\n"
    //          << "\tfrom\t" << new_edge_4_2.v1_id <<
"\tto\t"
    //          << new_edge_4_2.v2_id << std::endl;
    // std::cout << "新增边 new_edge_4_3:\n"
    //          << "\tfrom\t" << new_edge_4_3.v1_id <<
"\tto\t"
    //          << new_edge_4_3.v2_id << std::endl;
    // std::cout << "新增边 new_edge_4_4:\n"
    //          << "\tfrom\t" << new_edge_4_4.v1_id <<
"\tto\t"
    //          << new_edge_4_4.v2_id << std::endl;
}
else if (i.points.size() == 3)
{
    auto point_1 = *std::find_if(new_points.begin(),
new_points.end(),
                                [i](const my_point& p)
                                { return p.v_id ==
i.points[0]; });
    auto point_2 = *std::find_if(new_points.begin(),
new_points.end(),
                                [i](const my_point& p)
                                { return p.v_id ==
i.points[1]; });
    auto point_3 = *std::find_if(new_points.begin(),
new_points.end(),
                                [i](const my_point& p)
                                { return p.v_id ==
i.points[2]; });
    // std::cout << "三角形面" << i.face_id << std::endl;
    // std::cout << "point_1:" << "(" << point_1.x << "," <<
point_1.y << ")"
    //          << std::endl;
    // std::cout << "point_2:" << "(" << point_2.x << "," <<
point_2.y << ")"
    //          << std::endl;
    // std::cout << "point_3:" << "(" << point_3.x << "," <<
point_3.y << ")"
    //          << std::endl;
    auto edge_1_2_index = *std::find_if(
all_edges.begin(), all_edges.end(),

```

```

        [point_1, point_2](const my_edge& e)
        {
            return (e.v1_id == point_1.v_id && e.v2_id ==
point_2.v_id) ||
                (e.v1_id == point_2.v_id && e.v2_id ==
point_1.v_id);
        });
        auto edge_point_1_2 =
            *std::find_if(edge_points.begin(),
edge_points.end(),
                [edge_1_2_index](const my_point& p)
                { return p.v_id ==
edge_1_2_index.edge_id; });
        auto edge_2_3_index = *std::find_if(
            all_edges.begin(), all_edges.end(),
            [point_2, point_3](const my_edge& e)
            {
                return (e.v1_id == point_2.v_id && e.v2_id ==
point_3.v_id) ||
                    (e.v1_id == point_3.v_id && e.v2_id ==
point_2.v_id);
            });
        auto edge_point_2_3 =
            *std::find_if(edge_points.begin(),
edge_points.end(),
                [edge_2_3_index](const my_point& p)
                { return p.v_id ==
edge_2_3_index.edge_id; });
        auto edge_3_1_index = *std::find_if(
            all_edges.begin(), all_edges.end(),
            [point_3, point_1](const my_edge& e)
            {
                return (e.v1_id == point_3.v_id && e.v2_id ==
point_1.v_id) ||
                    (e.v1_id == point_1.v_id && e.v2_id ==
point_3.v_id);
            });
        auto edge_point_3_1 =
            *std::find_if(edge_points.begin(),
edge_points.end(),
                [edge_3_1_index](const my_point& p)
                { return p.v_id ==
edge_3_1_index.edge_id; });
        auto face_point =

```



```

        *std::find_if(face_points.begin(),
face_points.end(),
                    [i](const my_point& p) { return p.v_id
== i.face_id; });
        // 新增点

```

```

point_1.v_id = new_points_tmp.size();
new_points_tmp.push_back(point_1);
point_2.v_id = new_points_tmp.size();
new_points_tmp.push_back(point_2);
point_3.v_id = new_points_tmp.size();
new_points_tmp.push_back(point_3);
edge_point_1_2.v_id = new_points_tmp.size();
new_points_tmp.push_back(edge_point_1_2);
edge_point_2_3.v_id = new_points_tmp.size();
new_points_tmp.push_back(edge_point_2_3);
edge_point_3_1.v_id = new_points_tmp.size();
new_points_tmp.push_back(edge_point_3_1);
face_point.v_id = new_points_tmp.size();
new_points_tmp.push_back(face_point);
my_face new_face_1;
my_face new_face_2;
my_face new_face_3;
my_edge new_edge_1_1;
my_edge new_edge_1_2;
my_edge new_edge_1_3;
my_edge new_edge_1_4;
my_edge new_edge_2_1;
my_edge new_edge_2_2;
my_edge new_edge_2_3;
my_edge new_edge_2_4;
my_edge new_edge_3_1;
my_edge new_edge_3_2;
my_edge new_edge_3_3;
my_edge new_edge_3_4;
// 面1(a, edge_point_ab, face_point, edge_point_ca)
// 边1(a, edge_point_ab)
new_edge_1_1.v1_id = point_1.v_id;
new_edge_1_1.v2_id = edge_point_1_2.v_id;
// 边2(edge_point_ab, face_point)
new_edge_1_2.v1_id = edge_point_1_2.v_id;
new_edge_1_2.v2_id = face_point.v_id;
// 边3(face_point, edge_point_ca)
new_edge_1_3.v1_id = face_point.v_id;

```

```

new_edge_1_3.v2_id = edge_point_3_1.v_id;
// 边4(edge_point_ca, a)
new_edge_1_4.v1_id = edge_point_3_1.v_id;
new_edge_1_4.v2_id = point_1.v_id;
// 新增边
new_edge_1_1.edge_id = new_edges.size();
new_edges.push_back(new_edge_1_1);
new_edge_1_2.edge_id = new_edges.size();
new_edges.push_back(new_edge_1_2);
new_edge_1_3.edge_id = new_edges.size();
new_edges.push_back(new_edge_1_3);
new_edge_1_4.edge_id = new_edges.size();
new_edges.push_back(new_edge_1_4);
// 新增面
new_face_1.points = {point_1.v_id, edge_point_1_2.v_id,
face_point.v_id,
                        edge_point_3_1.v_id};
// new_face_1.edges = {new_edge_1_1.edge_id,
new_edge_1_2.edge_id,
// new_edge_1_3.edge_id};
new_face_1.face_id = new_faces.size();
new_faces.push_back(new_face_1);
// 面2(b, edge_point_bc, face_point, edge_point_ab)
// 边1(b, edge_point_bc)
new_edge_2_1.v1_id = point_2.v_id;
new_edge_2_1.v2_id = edge_point_2_3.v_id;
// 边2(edge_point_bc, face_point)
new_edge_2_2.v1_id = edge_point_2_3.v_id;
new_edge_2_2.v2_id = face_point.v_id;
// 边3(face_point, edge_point_ab)
new_edge_2_3.v1_id = face_point.v_id;
new_edge_2_3.v2_id = edge_point_1_2.v_id;
// 边4(edge_point_ab, b)
new_edge_2_4.v1_id = edge_point_1_2.v_id;
new_edge_2_4.v2_id = point_2.v_id;
// 新增边
new_edge_2_1.edge_id = new_edges.size();
new_edges.push_back(new_edge_2_1);
new_edge_2_2.edge_id = new_edges.size();
new_edges.push_back(new_edge_2_2);
new_edge_2_3.edge_id = new_edges.size();
new_edges.push_back(new_edge_2_3);
new_edge_2_4.edge_id = new_edges.size();
new_edges.push_back(new_edge_2_4);

```

```

        // 新增面
        new_face_2.points = {point_2.v_id, edge_point_2_3.v_id,
face_point.v_id,
                                edge_point_1_2.v_id};
        // new_face_2.edges = {new_edge_2_1.edge_id,
new_edge_2_2.edge_id,
        // new_edge_2_3.edge_id};
        new_face_2.face_id = new_faces.size();
        // 面3(c, edge_point_ca, face_point, edge_point_bc)
        // 边1(c, edge_point_ca)
        new_faces.push_back(new_face_2);
        new_edge_3_1.v1_id = point_3.v_id;
        new_edge_3_1.v2_id = edge_point_3_1.v_id;
        // 边2(edge_point_ca, face_point)
        new_edge_3_2.v1_id = edge_point_3_1.v_id;
        new_edge_3_2.v2_id = face_point.v_id;
        // 边3(face_point, edge_point_bc)
        new_edge_3_3.v1_id = face_point.v_id;
        new_edge_3_3.v2_id = edge_point_2_3.v_id;
        // 边4(edge_point_bc, c)
        new_edge_3_4.v1_id = edge_point_2_3.v_id;
        new_edge_3_4.v2_id = point_3.v_id;
        // 新增边
        new_edge_3_1.edge_id = new_edges.size();
        new_edges.push_back(new_edge_3_1);
        new_edge_3_2.edge_id = new_edges.size();
        new_edges.push_back(new_edge_3_2);
        new_edge_3_3.edge_id = new_edges.size();
        new_edges.push_back(new_edge_3_3);
        new_edge_3_4.edge_id = new_edges.size();
        new_edges.push_back(new_edge_3_4);
        // 新增面
        new_face_3.points = {point_3.v_id, edge_point_3_1.v_id,
face_point.v_id,
                                edge_point_2_3.v_id};
        // new_face_3.edges = {new_edge_3_1.edge_id,
new_edge_3_2.edge_id,
        //
                                new_edge_3_3.edge_id};
        new_face_3.face_id = new_faces.size();
        new_faces.push_back(new_face_3);
        // std::cout << "新增边 new_edge_1_1:\n"
        //
        << "\tfrom\t" << new_edge_1_1.v1_id <<
"\tto\t"
        //
        << new_edge_1_1.v2_id << std::endl;

```

```

// std::cout << "新增边 new_edge_1_2:\n"
//          << "\tfrom\t" << new_edge_1_2.v1_id <<
"\tto\t"
//          << new_edge_1_2.v2_id << std::endl;
// std::cout << "新增边 new_edge_1_3:\n"
//          << "\tfrom\t" << new_edge_1_3.v1_id <<
"\tto\t"
//          << new_edge_1_3.v2_id << std::endl;
// std::cout << "新增边 new_edge_1_4:\n"
//          << "\tfrom\t" << new_edge_1_4.v1_id <<
"\tto\t"
//          << new_edge_1_4.v2_id << std::endl;
// std::cout << "新增边 new_edge_2_1:\n"
//          << "\tfrom\t" << new_edge_2_1.v1_id <<
"\tto\t"
//          << new_edge_2_1.v2_id << std::endl;
// std::cout << "新增边 new_edge_2_2:\n"
//          << "\tfrom\t" << new_edge_2_2.v1_id <<
"\tto\t"
//          << new_edge_2_2.v2_id << std::endl;
// std::cout << "新增边 new_edge_2_3:\n"
//          << "\tfrom\t" << new_edge_2_3.v1_id <<
"\tto\t"
//          << new_edge_2_3.v2_id << std::endl;
// std::cout << "新增边 new_edge_2_4:\n"
//          << "\tfrom\t" << new_edge_2_4.v1_id <<
"\tto\t"
//          << new_edge_2_4.v2_id << std::endl;
// std::cout << "新增边 new_edge_3_1:\n"
//          << "\tfrom\t" << new_edge_3_1.v1_id <<
"\tto\t"
//          << new_edge_3_1.v2_id << std::endl;
// std::cout << "新增边 new_edge_3_2:\n"
//          << "\tfrom\t" << new_edge_3_2.v1_id <<
"\tto\t"
//          << new_edge_3_2.v2_id << std::endl;
// std::cout << "新增边 new_edge_3_3:\n"
//          << "\tfrom\t" << new_edge_3_3.v1_id <<
"\tto\t"
//          << new_edge_3_3.v2_id << std::endl;
// std::cout << "新增边 new_edge_3_4:\n"
//          << "\tfrom\t" << new_edge_3_4.v1_id <<
"\tto\t"
//          << new_edge_3_4.v2_id << std::endl;

```

```

    }
}

// 最终结果
new_faces.erase(new_faces.begin());
new_edges.erase(new_edges.begin());
new_points_tmp.erase(new_points_tmp.begin());
all_faces = new_faces;
all_edges = new_edges;
all_points = new_points_tmp;
bind_edges();
// for (auto& i : all_points)
// {
//     std::cout << "点" << i.v_id << "(" << i.x << "," << i.y
<< ")" << std::endl;
// }
// for (auto& i : all_edges)
// {
//     std::cout << "边" << i.edge_id << " from " << i.v1_id
<< " to " << i.v2_id
//         << std::endl;
// }
// for (auto& i : all_faces)
// {
//     std::cout << "面" << i.face_id << std::endl;
//     std::cout << "\t点\t";
//     for (auto& j : i.points)
//     {
//         std::cout << j << " ";
//     }
//     std::cout << std::endl;
//     std::cout << "\t边\t";
//     for (auto& j : i.edges)
//     {
//         std::cout << j << " ";
//     }
//     std::cout << std::endl;
// }
}

void write_all(const char* path)
{
    std::ofstream ofs(path);
    for (auto& i : all_points)
    {
        ofs << "v " << (i.x - OFFSET) / SCALE << " " << (i.y - OFFSET)

```

```

/ SCALE
    << "\n";
}
for (auto& i : all_edges)
{
    ofs << "e " << i.v1_id << " " << i.v2_id << "\n";
}
for (auto& i : all_faces)
{
    ofs << "f ";
    for (auto& j : i.points)
    {
        ofs << j << " ";
    }
    ofs << "\n";
}
}
int main(int argc, char** argv)
{
    std::string filepath = "obj1.txt";
    if (argc > 1)
    {
        filepath = argv[1];
    }
    size_t loop_times = 1;
    if (argc > 2)
    {
        loop_times = std::stoull(argv[2]);
    }
    read_file(filepath.c_str());
    Mat img = Mat::zeros(Size(800, 800), CV_8UC3);
    img.setTo(255); // 设置屏幕为白色
    draw_all(img);
    imshow("画板", img);
    waitKey(0);
    for (size_t i = 0; i < loop_times; i++)
    {
        // if (i > 0)
        // {
        //     read_file(".temp.obj");
        // }
        std::cout << "\n\n\n";
        std::cout << "第" << i + 1 << "次细分" << std::endl;
        std::cout << "\n\n\n";
    }
}

```

```
img.setTo(255);
catmull_clark();
draw_all(img);
imshow("画板", img);
waitKey(0);
// write_all(".temp.obj");
}
// system("rm .temp.obj");
if (loop_times == 0)
{
    img.setTo(255);
    draw_all(img);
    imshow("画板", img);
    waitKey(0);
}
// 输出 png
imwrite("output.png", img);
if (argc > 3)
{
    if (strcmp(argv[3], "-o") == 0)
    {
        std::string output_filepath = argv[4];
        write_all(output_filepath.c_str());
    }
}
return 0;
}
```

实验结果的截图如下：

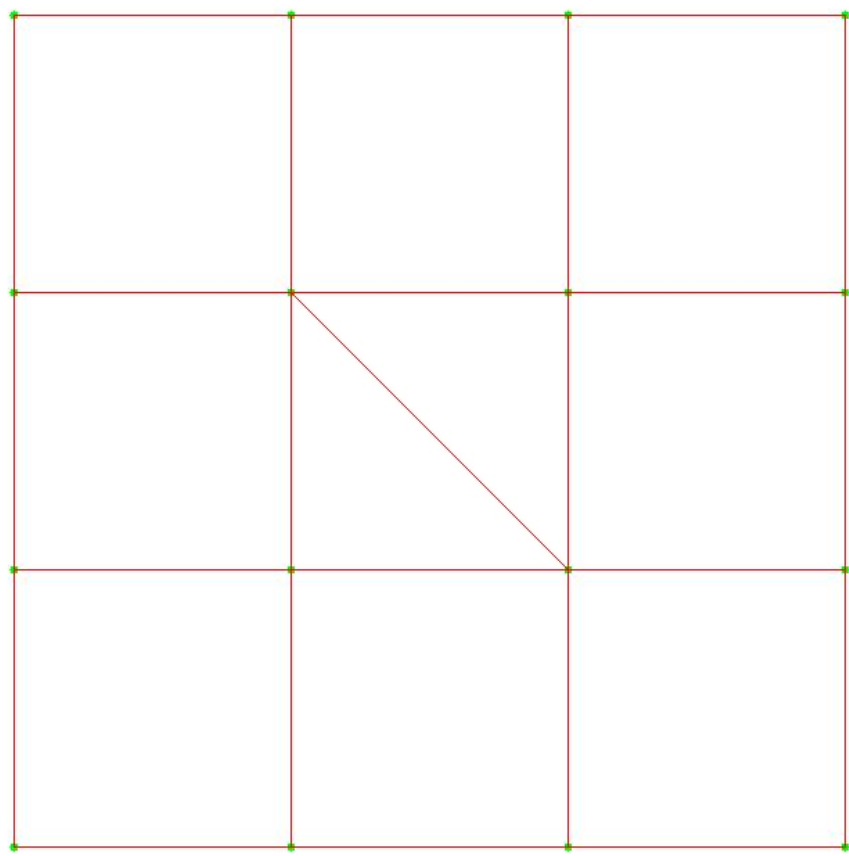


图 1 带三角的网格不细分

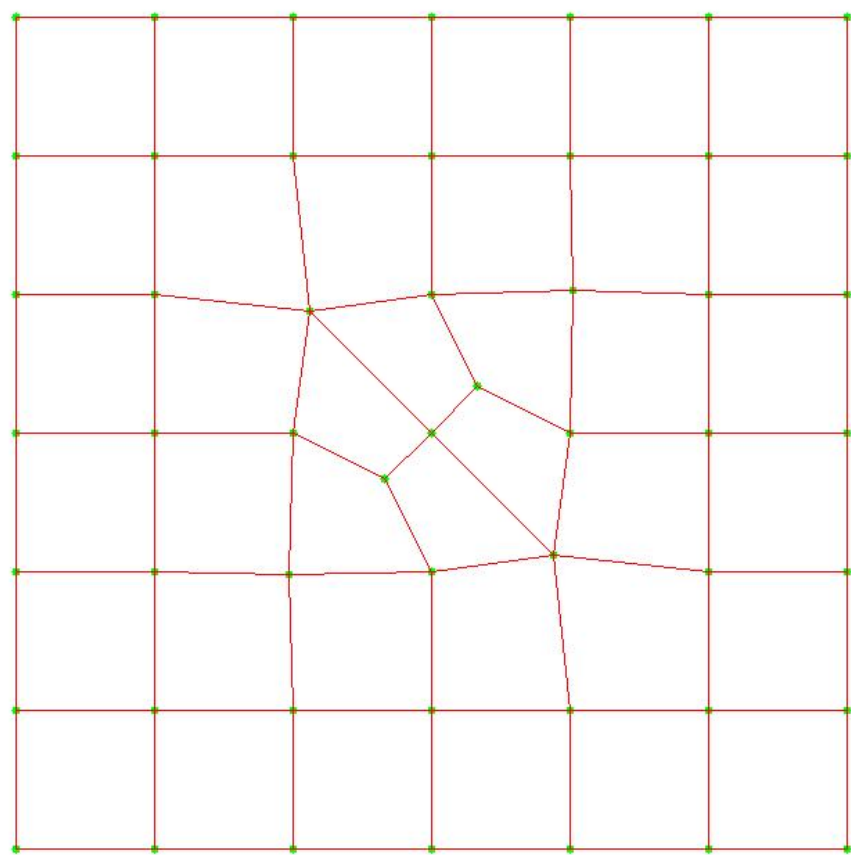


图 2 带三角的网格细分一次

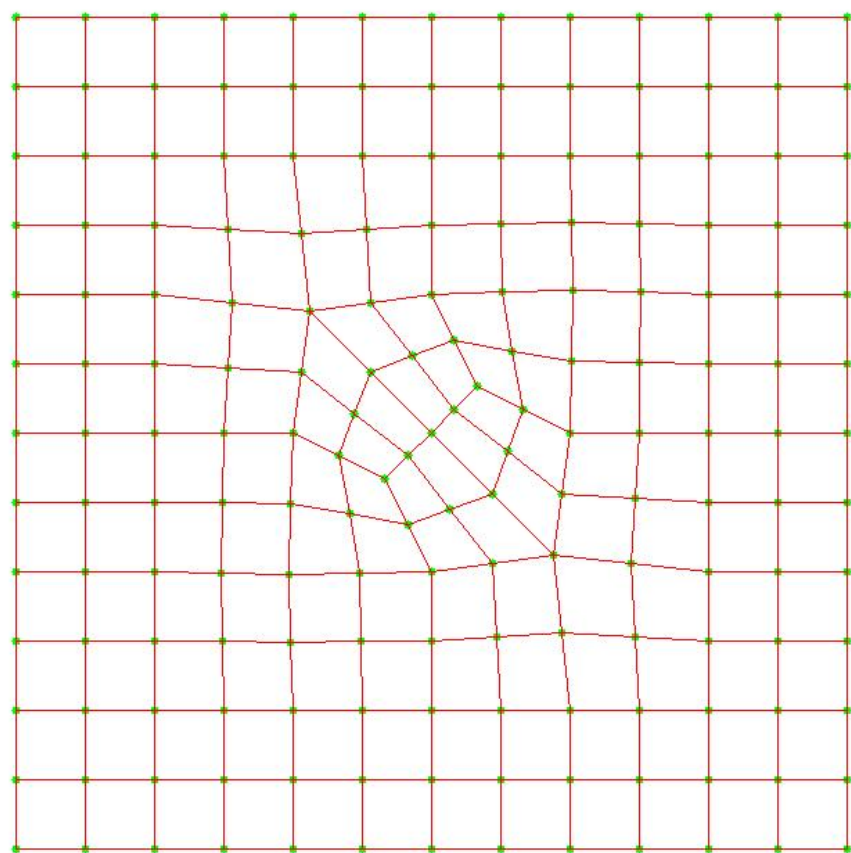


图 3 带三角的网格细分两次

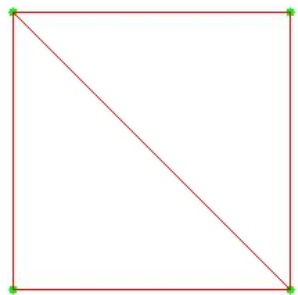


图 4 最简单的三角网格不细分

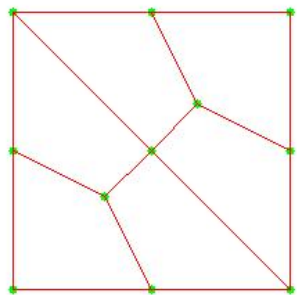


图 5 最简单的三角网格细分一次

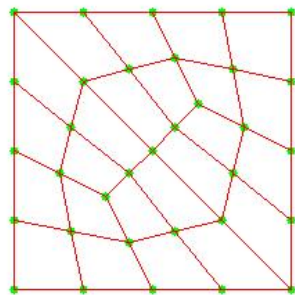


图 6 最简单的三角网格细分两次

实验中存在的问题及解决：

问题 1: Catmull-Clark 算法最初设计是三维闭合图形的细分，但是本次实验要求的是对二维非闭合平面图形进行细分，应该怎么办？

回答 1: 只需要对边界情况进行特殊处理即可，在确认一个点是边界点（即图形边缘的点，数学的描述就是相邻面和边的个数不一致）之后，只需要在更新原始点坐标的时候不更新这个点的坐标即可。

问题 2: 实验指导书给出的点坐标更新算法是分别处理了奇异点和非奇异点，有没有通用的办法？

回答 2: 有的兄弟有的，Catmull-Clark 算法的提出者给出了通用计算公式，即无论该点有多少个相邻面都可以按这个方式计算：

$$\frac{F + 2R + (n - 3)P}{n}$$

问题 3: 实验指导书给的边存储面以及面存储边和点的方式是储存索引, 而实验指导书使用 `vector` 这种线性结构来存储所有点和边和面, 这样是不是会麻烦很多, 降低效率? 有没有更好的选择?

回答 3: 我全程按照实验指导书给的类(结构体)定义以及用 `vector` 来作为全局容器来完成这个实验, 全程体验下来我可以很清楚地说明: 用 `vector` 存储没有任何好处, 甚至全是坏处。首先这会让存索引, 准确的说是存编号这种方式变得意义不明, 为了迎合这种存储方式, 在很多地方需要使用一些难以维护的 `find` 函数, 也难以使用 C++ 的运算符重载等特性, 并且因为 `vector` 这种线性容器 $O(n)$ 的查询时间复杂度, 当点的个数变多之后(实测下来当点的个数达到 6 万个左右的时候延迟就会达到秒级别)。只能说使用 `vector` 是完完全全不如使用 `unordered_map` 的, 而且使用唯一编号做索引这种方式, 因为这个编号是 `size_t(unsigned long long)` 类型, 他是非常适合使用哈希表这种数据结构的, 效率又高, 维护起来又容易。不过为了按照实验指导书的做法完成实验, 我并没有使用。