

## Performance indices of an M/M/1 queue

Consider a server that executes jobs arriving according to a Poisson process of rate  $\lambda = 10 \text{ job/s}$ , and serves them with an average service time  $D = 85 \text{ ms}$ .

Determine:

- The utilization of the system
- The probability of having exactly one job in the system
- The probability of having more than 5 jobs in the system
- The average queue length (job not in service)
- The average response time
- The probability that the response time is greater than 0.5 s.
- The 90 percentile of the response time distribution

- The utilization of the system  
 $U = 0.85$
- The probability of having exactly one job in the system  
 $p_1 = 0.1275$
- The probability of having more than 5 jobs in the system  
 $p(N > 5) = 0.3771$
- The average queue length (job not in service)  
 $Q = 4.8167$
- The average response time  
 $R = 0.5667 \text{ s}$
- The probability that the response time is greater than 0.5 s.  
 $p(R > 0.5) = 0.4138$
- The 90 percentile of the response time distribution  
 $\theta_R(90) = 1.3048 \text{ s}.$