

高级搜索

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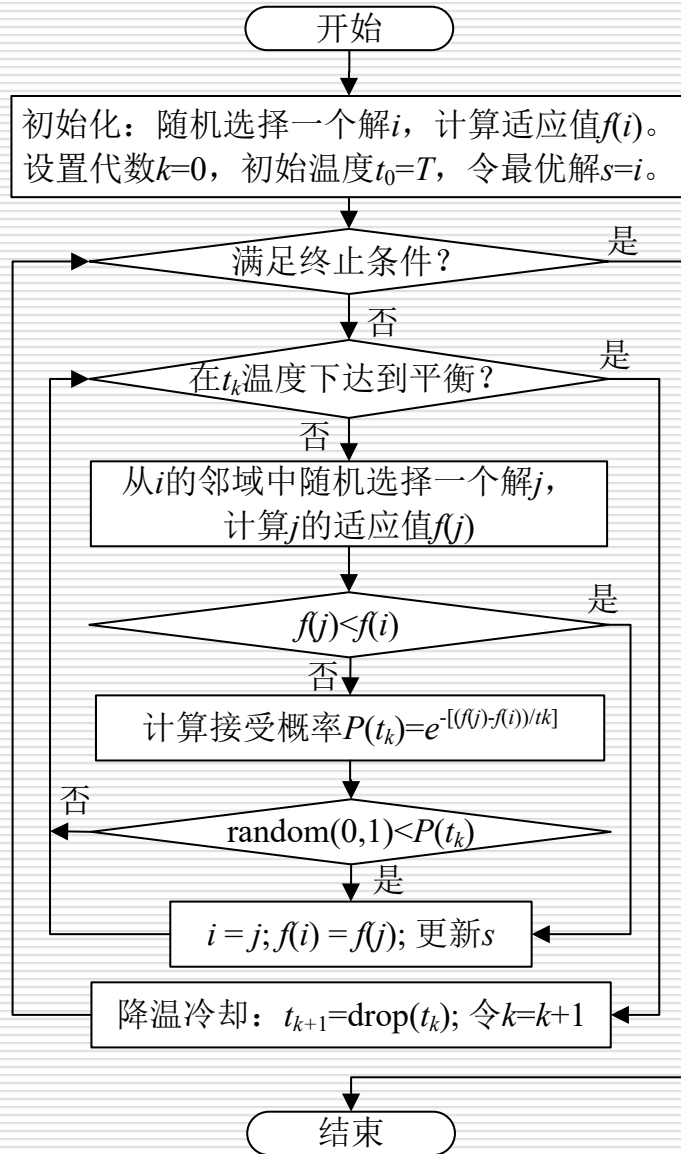
1.2 遗传算法

1.3 遗传算法在旅行商问题(TSP)中的应用

2. 实验任务(选做)

(Coding) 用模拟退火算法和遗传算法编程求解 TSP 问题

1.1 模拟退火算法



//功能: 模拟退火算法伪代码

//说明: 本例以求问题最小值为目标

//参数: T 为初始温度; L 为内层循环次数

procedure SA

//Initialization

Randomly generate a solution X_0 , and calculate its
fitness value $f(X_0)$;

$X_{best} = X_0; k=0; t_k=T;$

while not stop

//The search loop under the temperature t_k

for $i=1$ to L //The loop times

Generate a new solution X_{new} based on the current
solution X_k , and calculate its fitness value $f(X_{new})$.

if $f(X_{new}) < f(X_k)$

$X_k = X_{new};$

if $f(X_k) < f(X_{best})$ $X_{best} = X_k;$

continues;

end if

Calculate $P(t_k) = e^{-(f(X_{new})-f(X_k))/t_k};$

if random(0,1) < P

$X_k = X_{new};$

end if

end for

//Drop down the temperature

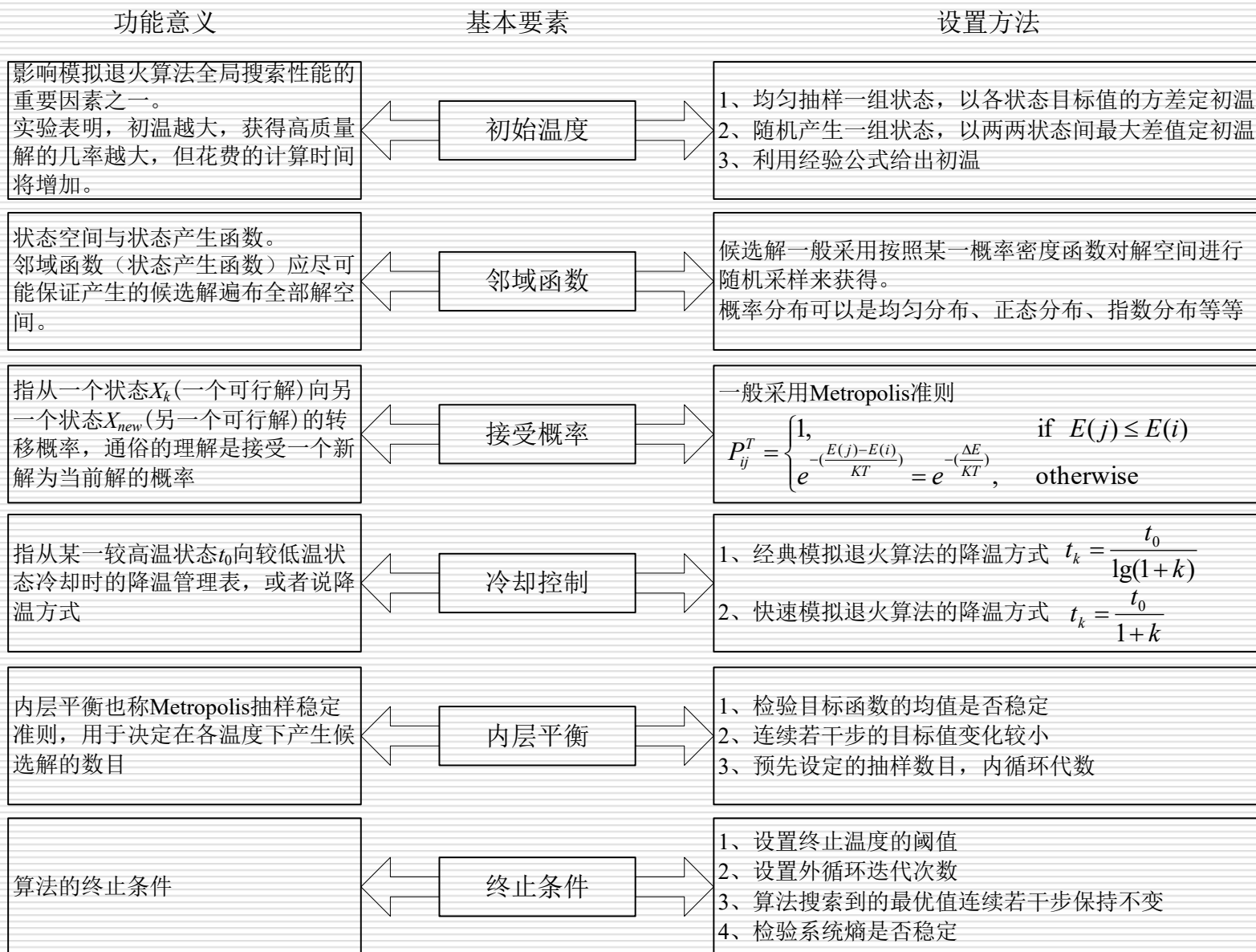
$t_{k+1} = \text{drop}(t_k); k=k+1;$

end while

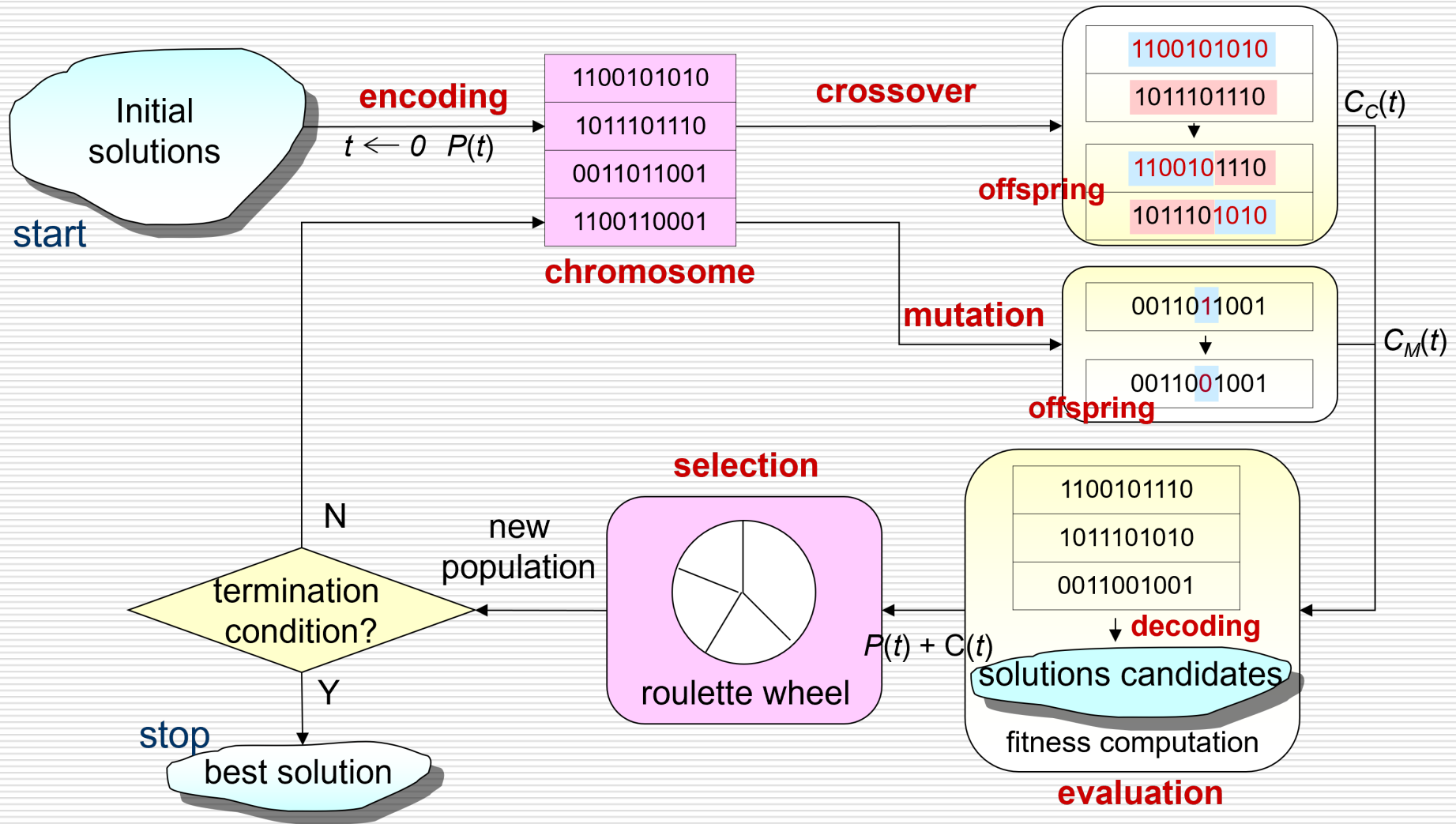
print X_{best}

end procedure

1.1 模拟退火算法



1.2 遗传算法



1.2 遗传算法

procedure: Simple GA

input: GA parameters

output: best solution

begin

$t \leftarrow 0;$

// t : generation number

initialize $P(t)$ by **encoding routine**;

// $P(t)$: population of chromosomes

fitness $eval(P)$ by **decoding routine**;

while (not termination condition) do

crossover $P(t)$ to yield $C(t)$;

// $C(t)$: offspring

mutation $P(t)$ to yield $C(t)$;

 fitness $eval(C)$ by **decoding routine**;

select $P(t+1)$ from $P(t)$ and $C(t)$;

$t \leftarrow t+1$;

end

output best solution;

end

1.3 旅行商问题(TSP)

- The **Traveling Salesman Problem (TSP)** is one of the most widely studied combinatorial optimization problems.
- Its statement is deceptively simple: A salesperson seeks the **shortest tour** through n cities.

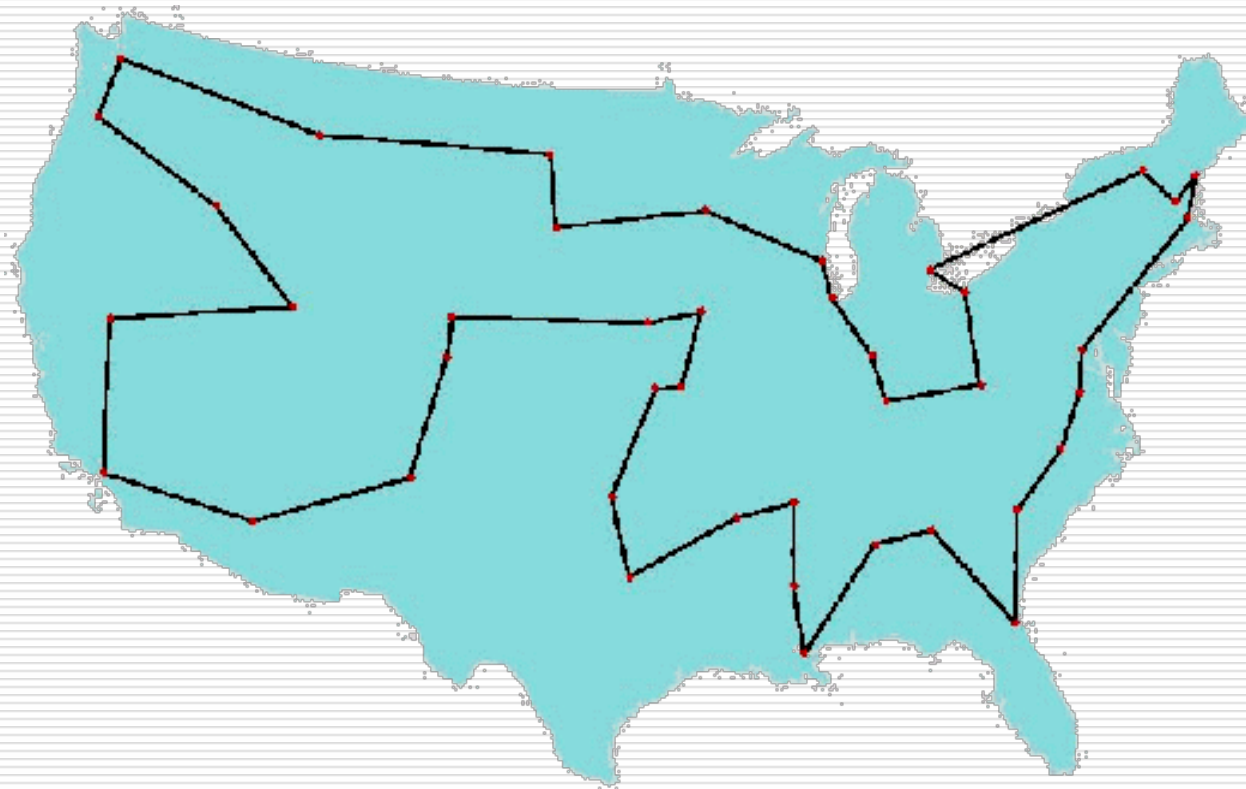


Fig. 3.4 **George Dantzig, Ray Fulkerson, and Selmer Johnson (1954)**
a description of a method for solving the TSP :49 cities

1.3.1 Representation

□ Random Keys Representation

- This indirect representation encodes a solution with random numbers from (0,1).
- These values are used as sort keys to decode the solution.

	1	2	3	4	5	6	7	8	9
chromosome	0.23	0.82	0.45	0.74	0.87	0.11	0.56	0.69	0.78

where position i in the list represents city i .

tour list 6 - 1 - 3 - 7 - 8 - 4 - 9 - 2 - 5

procedure: Random Keys Encoding

Input: city set,

total number of cities N

output: chromosome v

begin

for $i=1$ to N

$v[i] \leftarrow \text{random}[0,1];$

output chromosome v ;

end

procedure: Random Keys Decoding

Input: chromosome v ,

total number of cities N

output: tour list L

begin

$L \leftarrow \emptyset;$

for $i=1$ to N

$L \leftarrow L \cup i;$

 sort L by $v[i];$

output tour list L ;

end

1.3.2 Crossover Operators

- During the past decade, several crossover operators have been proposed for permutation representation, such as **partial-mapped crossover (PMX)**, **order crossover (OX)**, **cycle crossover (CX)**, **position-based crossover**, **order-based crossover** and so on.
- These operators can be classified into two classes:
 - **Canonical approach**
 - The canonical approach can be viewed as an extension of two-point or multipoint crossover of binary strings to permutation representation.
 - **Heuristic approach**
 - The application of heuristics in crossover intends to generate an improved offspring.

1.3.2 Crossover Operators

e.g. **Partial-Mapped Crossover (PMX)**

procedure : PMX crossover

input : chromosome v_1, v_2 ,
length of chromosome l

output : offspring v'_1, v'_2

begin

$R \leftarrow \emptyset$;

// step 1: select two positions
at random

$s \leftarrow \text{random}[1:l-1]$;

$t \leftarrow \text{random}[s+1:l]$;

// step 2: exchange two substrings

$\leftarrow v_1[1:s-1] // v_2[s:t] // v_1[t+1:l]$;

$v'_1 \leftarrow v_2[1:s-1] // v_1[s:t] // v_2[t+1:l]$;

// step 3: determine the mapping
relationship

$R \leftarrow \text{relation}(v_1[s:t], v_2[s:t])$;

// step 4: legalize offspring

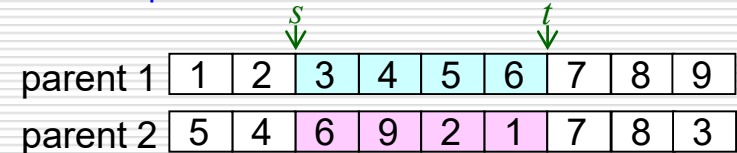
$\text{legalize}(\quad, \quad, R)$;

output offspring \quad, \quad ;

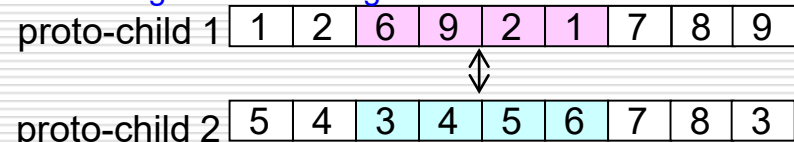
end

$v'_1 \quad v'_2$

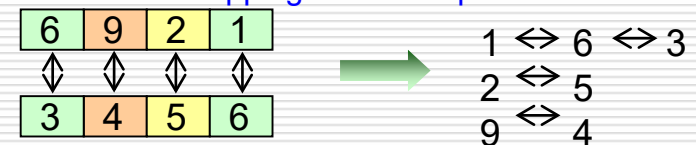
step 1 : select two positions at random



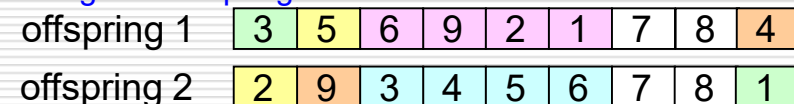
step 2: exchange two substrings



step 3 : determine the mapping relationship



step 4 : legalize offspring



v_1 : parent chromosome 1

v_2 : parent chromosome 2

l : length of chromosome

v'_1 : offspring chromosome 1

v'_2 : offspring chromosome 2

R : relationships

s : start position of substring

t : end position of substring

$\text{relation}(v_1, v_2)$: searching relationship between v_1 and v_2

$\text{legalize}(v_1, v_2, R)$ change genes value of v_1, v_2 based on relationship R

1.3.3 Mutation Operators

e.g. Inversion Mutation

procedure : Inversion Mutation

input : chromosome v_1, v_2 ,
length of chromosome l

output : offspring v'

begin

// step 1: select subtour at random

$s \leftarrow \text{random}[1:l-1]$;

$t \leftarrow \text{random}[s+1:l]$;

// step 2: produce offspring by
copying inverse string of
substring

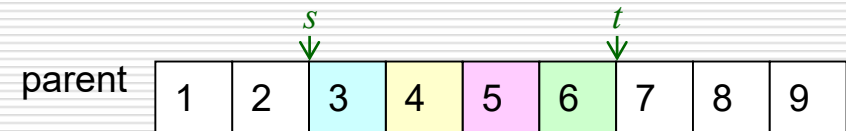
$S \leftarrow \text{invert}(v[s:t])$;

$v' \leftarrow v[1:s-1] // S // v[t+1:l]$;

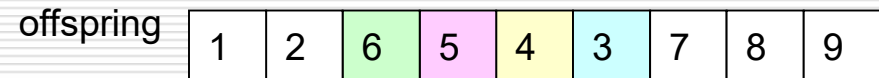
output offspring v'

end

step 1: select subtour at random



step 2: produce offspring by copying inverse string of substring



v : parent chromosome

v' : offspring chromosome

t : end position of substring

$\text{invert}(string)$: inversely changing order of $string$

l : length of chromosome

s : start position of substring

S : inverse string of substring

1.3.4 Overall Algorithm

□ GA procedure for Traveling Salesperson Problem

procedure: GA for Traveling Salesperson Problem (TSP)

Input: TSP data set, GA parameters

output: best tour route

begin

$t \leftarrow 0$;

initialize $P(t)$ by permutation encoding or random keys encoding;

fitness $eval(P)$ by permutation decoding or random keys decoding;

while (not termination condition) **do**

 crossover $P(t)$ to yield $C(t)$ by partial-mapped crossover;

 mutation $P(t)$ to yield $C(t)$ by swap mutation;

 fitness $eval(C)$ by permutation decoding or random keys decoding;

 select $P(t+1)$ from $P(t)$ and $C(t)$;

$t \leftarrow t+1$;

end

output best tour route;

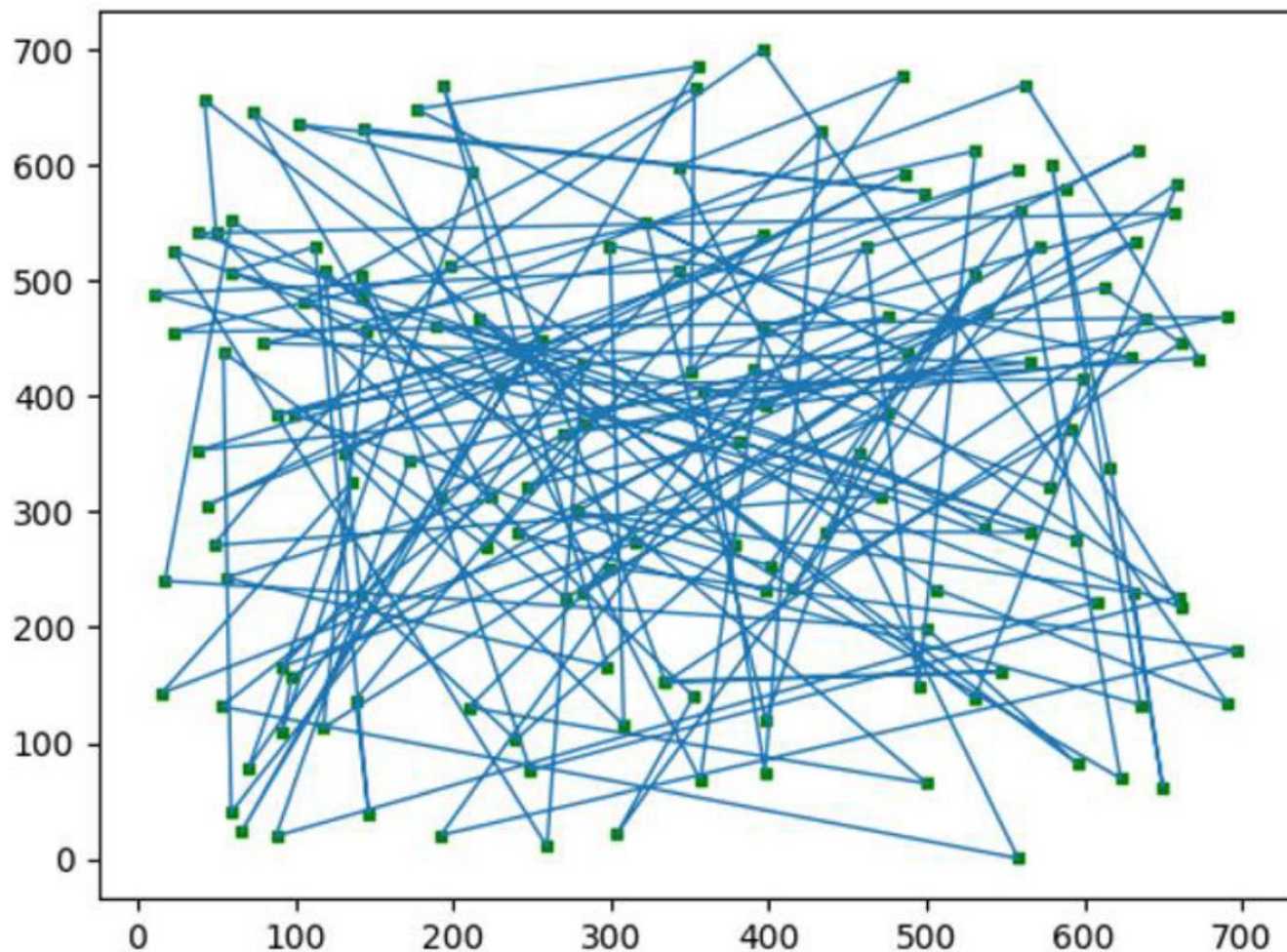
end

实验任务(选做)

- 在TSPLIB (<http://comopt.ifl.uni-heidelberg.de/software/TSPLIB95/>), 多个地址有备份; 其他网站还可以找到有趣的art TSP和national TSP) 中选一个大于100个城市数的TSP问题, 使用模拟退火和遗传算法求解。
- 模拟退火:
 - 采用多种邻域操作的局部搜索策略求解;
 - 在局部搜索策略的基础上, 加入模拟退火策略, 并比较两者的效果;
 - 提供可视化, 观察路径的变化和交叉程度(参考附录往届学生演示)。
- 遗传算法:
 - 设计较好的交叉操作, 并且引入多种局部搜索(变异)操作;
 - 和之前的模拟退火算法(采用相同的局部搜索操作)进行比较;
 - 得出设计高效遗传算法的一些经验, 并比较单点搜索和多点搜索的优缺点。

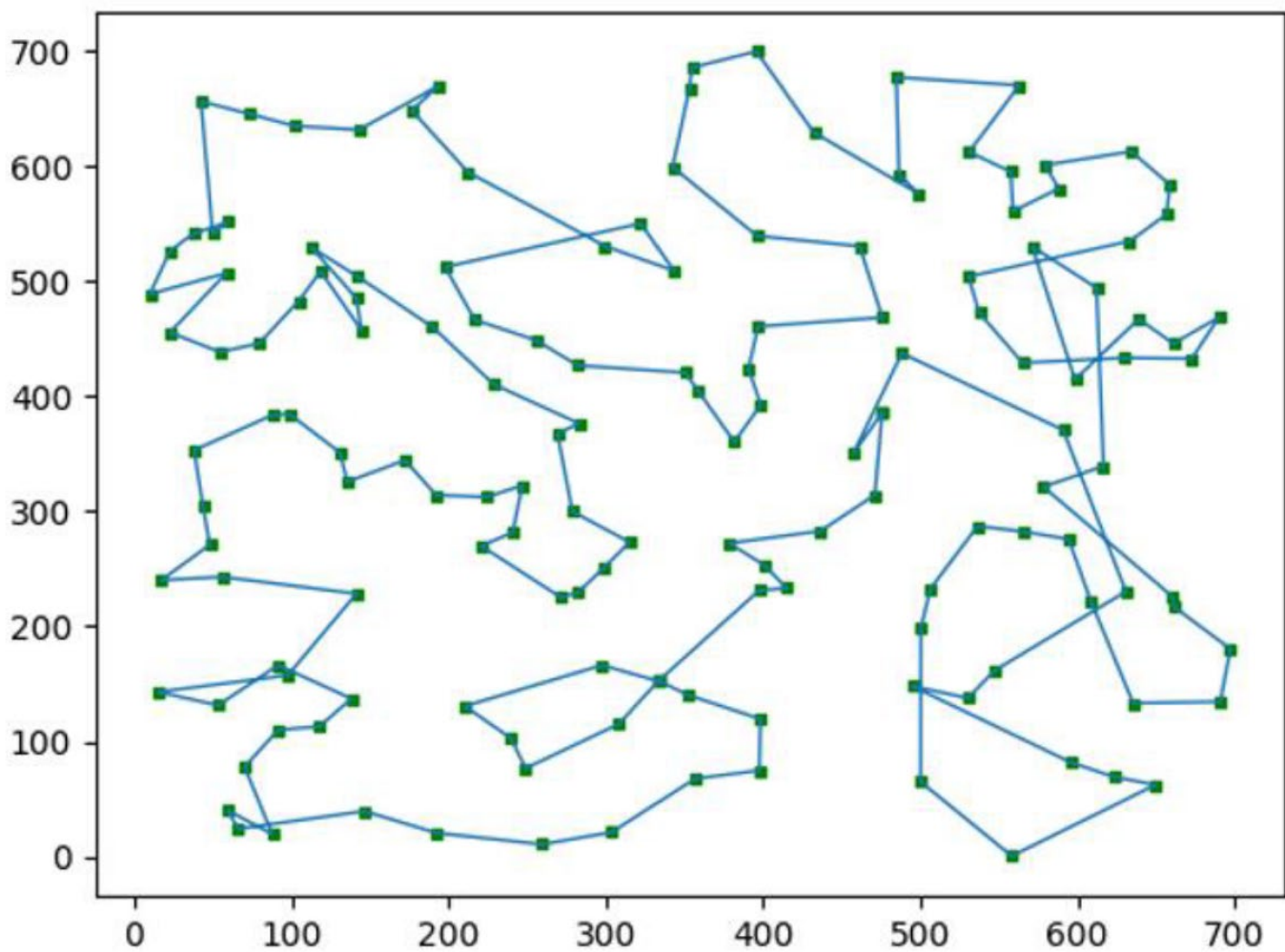
往届学生作品演示

□ 路径可视化



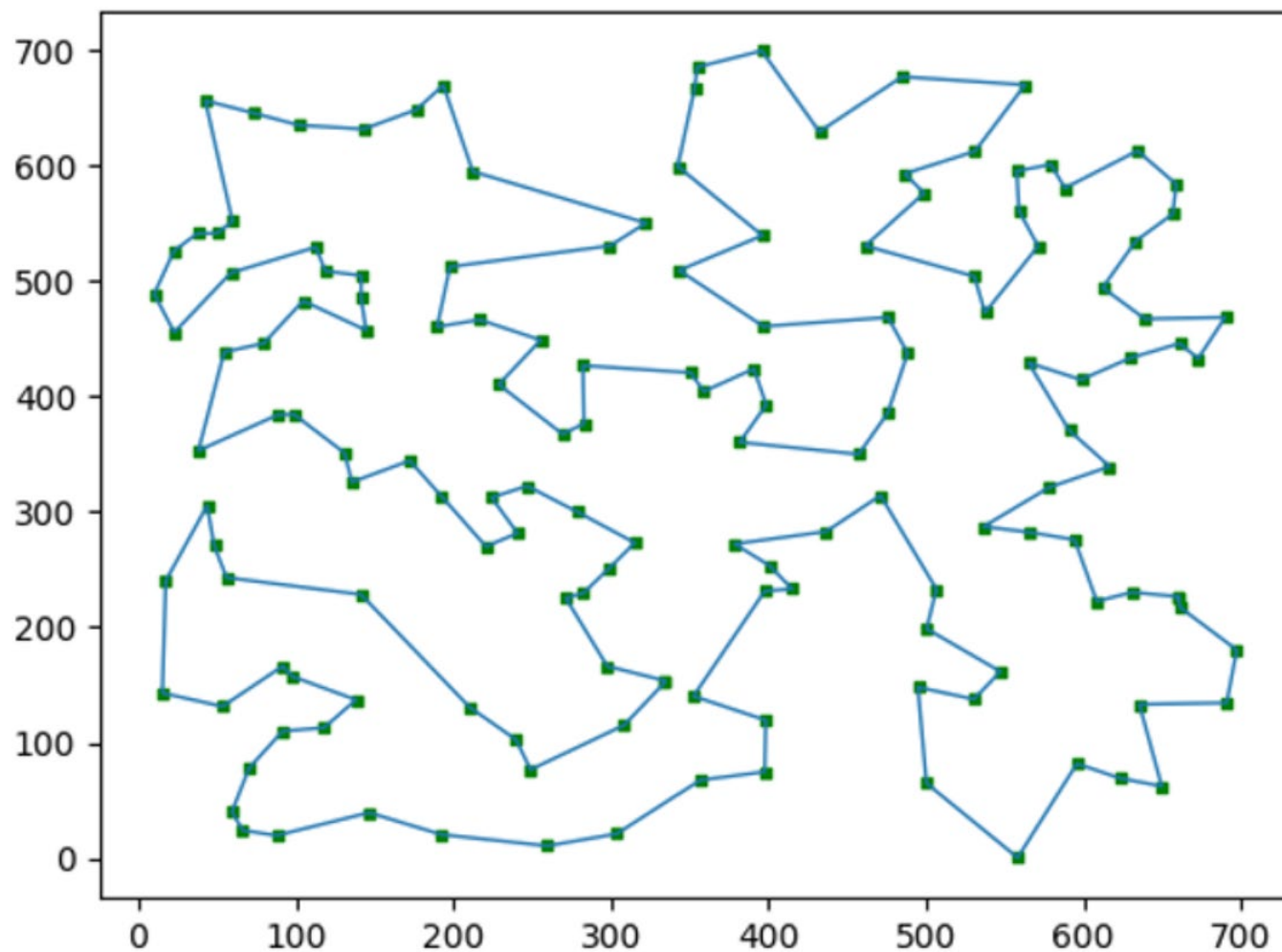
往届学生作品演示

□ 路径可视化



往届学生作品演示

□ 路径可视化



往届学生作品演示

□ 模拟退火收敛曲线

