

Molecular Simulation HOMEWORK 3

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Contents

1	Reaction energy of CO oxidation	1
1.1	Compute the reaction energy for $\text{CO} + 1/2 \text{O}_2 \rightarrow \text{CO}_2$	1
1.2	Convergence test	3
2	Zero-point energy corrections	5
2.1	Compute vibrational modes for CO, CO ₂ and O ₂	5
2.2	Compute the CO oxidation reaction energy with zero-point energy corrections.	7
2.3	Compare your computed energy to a value from the literature.	8
3	Plot the electron density of the CO₂ molecule.	8

1 Reaction energy of CO oxidation

1.1 Compute the reaction energy for $\text{CO} + 1/2 \text{O}_2 \rightarrow \text{CO}_2$

Use a cutoff energy of 250 eV. The molecules should all be relaxed to their lowest energy geometry (perform a geometry optimization). Demonstrate that all the forces on the molecule are less than 0.05 eV/Å.

```
1 from ase import Atoms, Atom
2 from jasp import *
3 import numpy as np
4 np.set_printoptions(precision=3, suppress=True)
5
6 CO = Atoms([Atom('C', (0, 0, 0)),
7             Atom('O', (1.2, 0, 0))],
8            cell=(10, 10, 10))
9 O2 = Atoms([Atom('O', (0, 0, 0)),
10            Atom('O', (1.23, 0, 0))],
11           cell=(9.8, 9.9, 10))
12 CO2 = Atoms([Atom('O', (0, 0, 0)),
13             Atom('C', (1.16, 0, 0)),
14             Atom('O', (2.32, 0, 0))],
15            cell=(10, 10, 10))
16 with jasp('probia/CO',
17          xc='PBE', lreal=False,
18          encut=250, prec='Accurate',
19          kpts=(1, 1, 1), ismear=1, sigma=0.05,
```

```

20         ibrion=1, nsw=50, ediffg=-0.05, isif=2,
21         atoms=C0) as C0calc:
22     try:
23         eC0 = C0.get_potential_energy()
24         fC0 = C0.get_forces()
25     except:
26         pass
27     with jasp('probia/O2',
28             xc='PBE', lreal=False,
29             encut=250, prec='Accurate',
30             kpts=(1, 1, 1), ismear=1, sigma=0.05,
31             ibrion=1, nsw=50, ediffg=-0.05, isif=2,
32             atoms=O2) as O2calc:
33     try:
34         eO2 = O2.get_potential_energy()
35         fO2 = O2.get_forces()
36     except:
37         pass
38     with jasp('probia/CO2',
39             xc='PBE', lreal=False,
40             encut=250, prec='Accurate',
41             kpts=(1, 1, 1), ismear=1, sigma=0.05,
42             ibrion=1, nsw=50, ediffg=-0.05, isif=2,
43             atoms=C02) as C02calc:
44     try:
45         eC02 = C02.get_potential_energy()
46         fC02 = C02.get_forces()
47     except:
48         pass
49
50     re = eC02 - eC0 - 0.5*eO2
51     print 'The total energy of C0 is {0:1.3f} eV/atom'.format(eC0)
52     print 'The forces (eV/angstrom) on the atoms in C0 are'
53     print 'C: {0}'.format(fC0[0])
54     print 'O: {0}\n'.format(fC0[1])
55     print 'The total energy of O2 is {0:1.3f} eV/atom'.format(eO2)
56     print 'The forces (eV/angstrom) on the atoms in O2 are'
57     print 'O: {0}'.format(fO2[0])
58     print 'O: {0}\n'.format(fO2[1])
59     print 'The total energy of C02 is {0:1.3f} eV/atom'.format(eC02)
60     print 'The forces (eV/angstrom) on the atoms in C02 are'
61     print 'O: {0}'.format(fC02[0])
62     print 'C: {0}'.format(fC02[1])
63     print 'O: {0}\n'.format(fC02[2])
64     print 'The reaction energy is {0:1.3f} eV/C02'.format(re)

```

The total energy of C0 is -15.168 eV/atom
 The forces (eV/angstrom) on the atoms in C0 are
 C: [-0.033 0. 0.]
 O: [0.033 0. 0.]

The total energy of O2 is -8.719 eV/atom
 The forces (eV/angstrom) on the atoms in O2 are
 O: [0.019 0. 0.]
 O: [-0.019 0. 0.]

The total energy of C02 is -23.508 eV/atom
 The forces (eV/angstrom) on the atoms in C02 are
 O: [-0.015 0. 0.]
 C: [0. 0. 0.]

```
O: [ 0.015  0.      0.    ]
```

The reaction energy is -3.980 eV/C02

1.2 Convergence test

Repeat the previous problem at 350, 450, and 500 eV. Reoptimize the geometry at each ENCUT value. Compare (in a graph) the convergence of the total energy of each species with the convergence of the reaction energy. Which converges faster?

```
1 from ase import Atoms, Atom
2 from jasp import *
3 import numpy as np
4 np.set_printoptions(precision=3, suppress=True)
5
6 C0 = Atoms([Atom('C', (0, 0, 0)),
7             Atom('O', (1.2, 0, 0))],
8            cell=(10, 10, 10))
9 O2 = Atoms([Atom('O', (0, 0, 0)),
10            Atom('O', (1.23, 0, 0))],
11           cell=(9.8, 9.9, 10))
12 C02 = Atoms([Atom('O', (0, 0, 0)),
13             Atom('C', (1.16, 0, 0)),
14             Atom('O', (2.32, 0, 0))],
15            cell=(10, 10, 10))
16 dirs = ('/e350', '/e450', '/e500')
17 cuts = (350, 450, 500)
18 eC0s = []
19 eO2s = []
20 eC02s = []
21
22 for d, cut in zip(dirs, cuts):
23     with jasp('pro1b' + d + '/C0',
24              xc='PBE', lreal=False,
25              encut=cut, prec='Accurate',
26              kpts=(1, 1, 1), ismear=1, sigma=0.05,
27              ibrion=1, nsw=50, ediffg=-0.05, isif=2,
28              atoms=C0) as C0calc:
29         try:
30             eC0 = C0.get_potential_energy()
31             eC0s.append(eC0)
32         except:
33             pass
34     with jasp('pro1b' + d + '/O2',
35              xc='PBE', lreal=False,
36              encut=cut, prec='Accurate',
37              kpts=(1, 1, 1), ismear=1, sigma=0.05,
38              ibrion=1, nsw=50, ediffg=-0.05, isif=2,
39              atoms=O2) as O2calc:
40         try:
41             eO2 = O2.get_potential_energy()
42             eO2s.append(eO2)
43         except:
44             pass
45     with jasp('pro1b' + d + '/C02',
46              xc='PBE', lreal=False,
47              encut=cut, prec='Accurate',
48              kpts=(1, 1, 1), ismear=1, sigma=0.05,
49              ibrion=1, nsw=50, ediffg=-0.05, isif=2,
50              atoms=C02) as C02calc:
51         try:
52             eC02 = C02.get_potential_energy()
```

```

53         eC02s.append(eC02)
54     except:
55         pass
56
57     import matplotlib.pyplot as plt
58     from matplotlib.ticker import ScalarFormatter
59     import numpy as np
60
61     eC0s = np.array(eC0s)
62     e02s = np.array(e02s)
63     eC02s = np.array(eC02s)
64
65     fig = plt.figure(1)
66     axC0 = fig.add_subplot(221)
67     axC0.plot(cuts, eC0s, marker='o')
68     axC0.set_title(r'$\mathdefault{CO}$')
69     axC0.set_xlim((300, 550))
70     axC0.set_ylim((-14.81, -14.75))
71     axC0.set_xticklabels(())
72     axC0.yaxis.set_major_formatter(ScalarFormatter(useOffset=False))
73     axC0.set_ylabel('Total Energy (eV/atom)')
74
75     ax02 = fig.add_subplot(222)
76     ax02.plot(cuts, e02s, marker='o')
77     ax02.set_title(r'$\mathdefault{O_2}$')
78     ax02.set_xlim((300, 550))
79     ax02.set_ylim((-8.76, -8.70))
80     ax02.set_xticklabels(())
81     ax02.yaxis.set_major_formatter(ScalarFormatter(useOffset=False))
82
83     axC02 = fig.add_subplot(223)
84     axC02.plot(cuts, eC02s, marker='o')
85     axC02.set_title(r'$\mathdefault{CO_2}$')
86     axC02.set_xlim((300, 550))
87     axC02.set_xlabel('Kinetic Energy Cutoff (eV)')
88     axC02.set_ylabel('Total Energy (eV/atom)')
89     axC02.xaxis.set_major_formatter(ScalarFormatter(useOffset=False))
90     axC02.yaxis.set_major_formatter(ScalarFormatter(useOffset=False))
91
92     axrxn = fig.add_subplot(224)
93     axrxn.plot(cuts, eC02s - eC0s - 0.5*e02s, marker='o')
94     axrxn.set_title(r'$\Delta H\mathdefault{(CO + \frac{1}{2} O_2)} \rightarrow \mathdefault{CO_2}$')
95     axrxn.set_xlim((300, 550))
96     axrxn.set_ylim((-3.84, -3.78))
97     axrxn.set_xlabel('Kinetic Energy Cutoff (eV)')
98     axrxn.xaxis.set_major_formatter(ScalarFormatter(useOffset=False))
99     axrxn.yaxis.set_major_formatter(ScalarFormatter(useOffset=False))
100     fig.tight_layout()
101     plt.savefig('1b.png')
102     plt.show()

```

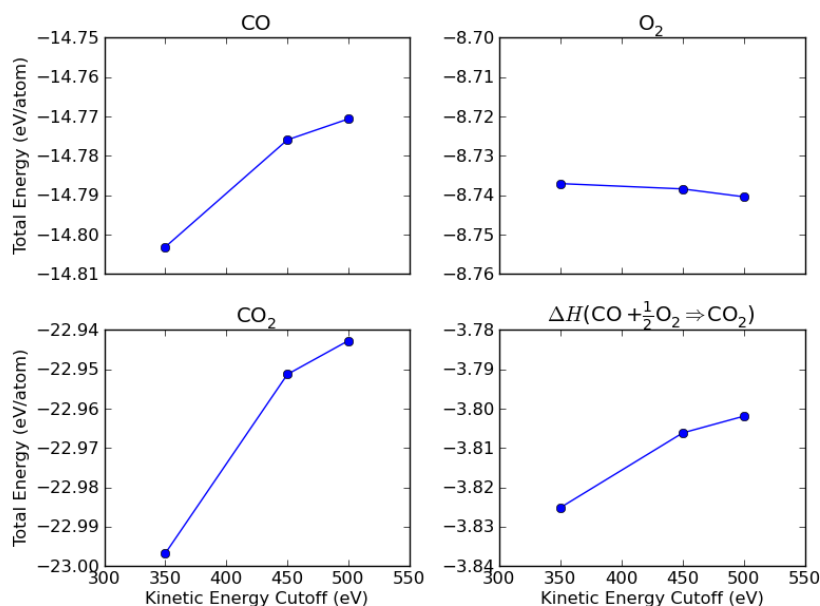


Figure 1: Convergence of CO, O₂, CO₂, and the reaction enthalpy of CO + 1/2O₂ → CO₂ with respect to plane wave cutoff energy

The total energy of the oxygen molecule converges the fastest. Note, all y-axis tick spacings are the same.

2 Zero-point energy corrections

2.1 Compute vibrational modes for CO, CO₂ and O₂

Compute the vibrational modes of each molecule in the CO oxidation reaction. Do this at 350 eV cutoff energy only. Prepare a table of the vibrational modes for molecule.

```

1  import os
2  import sys
3  from ase.calculators.vasp import Vasp
4  import ase.units
5  from jasp import *
6
7  # Since we wanted relaxed molecules for these calculations, we can take
8  # these geometries from the previous problem.
9
10 with jasp('prob1b/e350/CO') as calc:
11     CO = calc.get_atoms()
12 with jasp('prob1b/e350/O2') as calc:
13     O2 = calc.get_atoms()
14 with jasp('prob1b/e350/CO2') as calc:
15     CO2 = calc.get_atoms()
16
17 # Now we're ready to perform the vibrational calculations
18 with jasp('prob2a/CO',
19         xc='PBE', lreal=False,
20         encut=350, prec='Accurate', ediff=1e-8,
21         kpts=(1, 1, 1), ismear=0, sigma=0.05,
```

```

22         ibrion=6, nsw=1, potim=0.015, nfree=2,
23         atoms=C0) as calcC0:
24     try:
25         C0.get_potential_energy()
26         energies, modes = calcC0.get_vibrational_modes()
27         print 'Energies of C0\n=====
28         for i, e in enumerate(energies):
29             print '{0:02d}: {1} eV'.format(i, e)
30     except:
31         pass
32 with jasp('prob2a/O2',
33         xc='PBE', lreal=False,
34         encut=350, prec='Accurate', ediff=1e-8,
35         kpts=(1, 1, 1), ismear=0, sigma=0.05,
36         ibrion=6, nsw=1, potim=0.015, nfree=2,
37         atoms=O2) as calcO2:
38     try:
39         O2.get_potential_energy()
40         energies, modes = calcO2.get_vibrational_modes()
41         print '\nEnergies of O2\n=====
42         for i, e in enumerate(energies):
43             print '{0:02d}: {1} eV'.format(i, e)
44     except:
45         pass
46 with jasp('prob2a/CO2',
47         xc='PBE', lreal=False,
48         encut=350, prec='Accurate', ediff=1e-8,
49         kpts=(1, 1, 1), ismear=0, sigma=0.05,
50         ibrion=6, nsw=1, potim=0.015, nfree=2,
51         atoms=CO2) as calcCO2:
52     try:
53         CO2.get_potential_energy()
54         energies, modes = calcCO2.get_vibrational_modes()
55         print '\nEnergies of CO2\n=====
56         for i, e in enumerate(energies):
57             print '{0:02d}: {1} eV'.format(i, e)
58     except:
59         pass

```

Energies of C0

=====

```

00: 0.261840727 eV
01: 0.003767323 eV
02: 0.003767323 eV
03: (3.0739e-05+0j) eV
04: (0.000943898+0j) eV
05: (0.000943898+0j) eV

```

Energies of O2

=====

```

00: 0.189490603 eV
01: 0.004093929 eV
02: 1e-09 eV
03: 0.0 eV
04: (1e-09+0j) eV
05: (0.006638148+0j) eV

```

Energies of CO2

=====

00: 0.291924562 eV
01: 0.16318552 eV
02: 0.078492458 eV
03: 0.078492458 eV
04: 0.004836504 eV
05: 0.004836504 eV
06: (4.1677e-05+0j) eV
07: (5.9833e-05+0j) eV
08: (5.9833e-05+0j) eV

2.2 Compute the CO oxidation reaction energy with zero-point energy corrections.

Compare the reaction energy with and without the zero-point energy correction.

```
1 from jasp import *
2 import numpy as np
3 c = 3e10 # speed of light cm/s
4 h = 4.135667516e-15 # eV/s
5
6 # Get the vibrational energies from problem 2a. Get the total energies from
7 # problem 1b at 350 eV.
8
9 with jasp('prob2a/CO') as calc:
10     COfreq = calc.get_vibrational_frequencies()
11 with jasp('prob1b/e350/CO') as calc:
12     atoms = calc.get_atoms()
13     COe = atoms.get_potential_energy()
14 for f in COfreq:
15     if not isinstance(f, float):
16         continue
17     nu = f*c
18     COe += 0.5*h*nu
19 with jasp('prob2a/O2') as calc:
20     O2freq = calc.get_vibrational_frequencies()
21 with jasp('prob1b/e350/O2') as calc:
22     atoms = calc.get_atoms()
23     O2e = atoms.get_potential_energy()
24 for f in O2freq:
25     if not isinstance(f, float):
26         continue
27     nu = f*c
28     O2e += 0.5*h*nu
29 with jasp('prob2a/CO2') as calc:
30     CO2freq = calc.get_vibrational_frequencies()
31 with jasp('prob1b/e350/CO2') as calc:
32     atoms = calc.get_atoms()
33     CO2e = atoms.get_potential_energy()
34 for f in CO2freq:
35     if not isinstance(f, float):
36         continue
37     nu = f*c
38     CO2e += 0.5*h*nu
39 s = 'The reaction energy for CO oxidation with zero point contributions is {0:1.3f} eV'
40 print s.format(CO2e - COe - 0.5*O2e)
```

The reaction energy for CO oxidation with zero point contributions is -3.697 eV

2.3 Compare your computed energy to a value from the literature.

Provide a reference for your literature value.

All values are taken from the NIST-JANAF Thermochemical Tables at kinetics.nist.gov/janaf.

```
1 # Values of heats of formation at 0 K in kJ/mol
2 Hf_CO = -113.805
3 Hf_CO2 = -393.151
4 Hf_O2 = 0 # Pure component is reference
5
6 Hf_rxn = Hf_CO2 - HF_CO
7 s = 'The experimental heat of reaction is {0:1.3f} eV/atom'
8 print s.format(Hf_rxn * 0.010364) # Convert from kJ/mol to eV/atom (atom as in formula unit)
```

The experimental heat of reaction is -2.895 eV/atom

Our computed heat of reaction is too exothermic. This means that either the products (CO₂) are too stable, or the reactants (O₂ and CO) are unstable.

3 Plot the electron density of the CO₂ molecule.

Include the figure in your homework.

```
1 from jasp import *
2 from enthought.mayavi import mlab
3 from ase.data import vdw_radii
4 from ase.data.colors import cpk_colors
5 from ase import Atom, Atoms
6
7 # Lets first get the relaxed CO2 at 500 eV plane wave cutoff, center it,
8 # and recalculate the electron density in the centered cell
9
10 with jasp('prob1b/e500/CO2') as calc:
11     CO2 = calc.get_atoms()
12     CO2.center()
13 with jasp('prob3a/CO2-centered',
14         xc='PBE', lreal=False,
15         encut=500, prec='Accurate',
16         kpts=(1, 1, 1), ismear=1, sigma=0.05,
17         atoms=CO2) as calc:
18     CO2.get_potential_energy()
19     x, y, z, cd = calc.get_charge_density()
20
21 mlab.figure(bgcolor=(1, 1, 1))
22 # plot the atoms as spheres
23 for atom in CO2:
24     mlab.points3d(atom.x,
25                   atom.y,
26                   atom.z,
27                   scale_factor=vdw_radii[atom.number]/5.,
28                   resolution=20,
29                   # a tuple is required for the color
30                   color=tuple(cpk_colors[atom.number]),
31                   scale_mode='none')
32
33 # draw the unit cell - there are 8 corners, and 12 connections
34 a1, a2, a3 = CO2.get_cell()
35 origin = [0, 0, 0]
36 cell_matrix = [[origin, a1],
```



```

37         [origin, a2],
38         [origin, a3],
39         [a1, a1 + a2],
40         [a1, a1 + a3],
41         [a2, a2 + a1],
42         [a2, a2 + a3],
43         [a3, a1 + a3],
44         [a3, a2 + a3],
45         [a1 + a2, a1 + a2 + a3],
46         [a2 + a3, a1 + a2 + a3],
47         [a1 + a3, a1 + a3 + a2]]
48
49 for p1, p2 in cell_matrix:
50     mlab.plot3d([p1[0], p2[0]], # x-positions
51                [p1[1], p2[1]], # y-positions
52                [p1[2], p2[2]], # z-positions
53                tube_radius=0.02)
54
55 # Now plot the charge density
56 mlab.contour3d(x, y, z, cd, transparent=True)
57
58 # this view was empirically found by iteration
59 mlab.view(azimuth=-90, elevation=90, distance='auto')
60
61 mlab.savefig('co2-density.png')

```

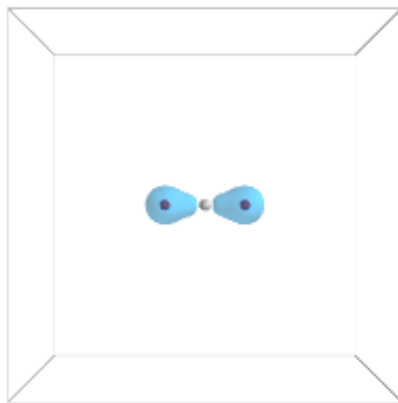


Figure 2: Charge density of CO2