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Using linear model for learning curve effect on highrise floor construction

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The evolution of repetitive scheduling methods led to the introduction of the learning concept in construction planning. It is common knowledge that performing the same activity repeatedly, and in the same conditions, takes less and less time as the activity is repeated (Gates and Scarpa, 1972). This phenomenon is clear in many construction activities and is known as learning experience or learning effect. The increase in productivity is mainly due to the increasing knowledge acquired by work repetition. Graphic representation is through a learning curve that admits duration decreases as the activity is repeated, according to a predictable and constant learning rate. The Linear Model of logarithmic coordinates ($\log_{10}Y = \log_{10}A - n\log_{10}X$) was applied to two repetitive construction processes, frequently used in Portuguese construction. The intent was to examine its applicability and efficiency in predicting future performances, and the interest in incorporating the model in new planning methodologies for repetitive construction. In both cases, learning processes were created.

Keywords: Learning effect, learning curve, linear model, planning construction, models, repetitive construction

Incorporating the learning effect in repetitive construction

Specific scheduling methods may be used advantageously for construction projects with repetitive characteristics, but incorporating the learning effect into the estimation of activity duration may lead to even better results (Pilcher, 1992).

Acknowledging the restrictions imposed by traditional programming methods in treating this type of project, specific methods for repetitive construction have been suggested for the last 30 years (Couto, 1998; Teixeira and Couto, 2002a). They were first based on the Line of Balance concept with a constant production rate, but subsequent developments have considered variable production rates that are best suited to the consideration of the learning effect (Couto and Teixeira, 2002; Teixeira and Couto, 2002b). The time required to perform identical activities successively and in the same conditions is expected to decrease to a certain value; hence, considering the learning effect in performing an activity is the same as admitting an increase in production rates from a certain number of

repetitions, and at least during some subsequent repetitions. Therefore, it is possible to introduce this effect in repetitive construction scheduling methods, thus bringing about an expected efficiency increase after an initial learning period.

Mathematical models for the learning curve

General aspects

The learning curve is graphically represented by the amount of time, cost or number of man-hours needed for carrying out the successive activities required (Everett and Farghal, 1994). The learning curve concept emphasizes that time, cost and man-hours for accomplishing repetitive and subsequent tasks decreases in each repetition, according to a predictable learning rate.

The first known study on the learning curve, conducted by Wright in 1936, concluded that the number of man-hours necessary to install airplane components (Wright, 1936) decreased 20% each time the units produced doubled. In other words, productivity improved 20% due to the learning effect (Carlson, 1973), meaning that the learning rate is 80%. Therefore, the

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smaller the learning, and consequent increase in productivity, the greater the learning rate and vice-versa. Hence, a learning rate of 100% indicates a zero increase in productivity (Lutz *et al.*, 1994).

Theoretically, a learning curve in logarithmic coordinates can be divided into three parts, as illustrated in Figure 1 (Thomas *et al.*, 1986). In the first part, previous experience allows for modest improvement in productivity. As workers become familiar with constructive processes, material and project environment, productivity improves and the learning curve drops sharply. The third part is represented by a horizontal line, evidencing that no additional improvement may be achieved in productivity. Once this stage is reached, improvement in productivity can only be reached with more efficient construction processes (Lutz *et al.*, 1994; Cunningham, 1980). In Figure 1, Y is the cost, man-hours or time required to perform a repeated generic unit X.

The importance of the learning effect in planning has become an attractive research topic first directed to industry and more recently to construction. Accordingly, various mathematical learning curve models have been proposed (Couto and Teixeira, 2004). The difficulty in using the outcomes of this research lies in selecting the most adequate model for each construction activity and how they can possibly inter-relate among the vast amount of activities of an ordinary construction.

Correlation studies of mathematical models for the learning curve

Nowadays, the most frequently used learning curves generally follow the Stanford 'B' Model or the Linear Model of logarithmic coordinates (Tanner, 1985). Graphically, both curves are approximately represented by a straight line in logarithmic coordinates (Lutz *et al.*, 1994). However, various other mathematical models

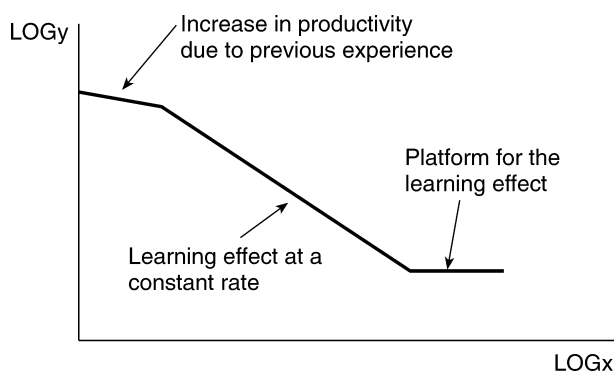


Figure 1 Theoretical learning curve with logarithmic coordinates

may be found in literature, for example the Cubic Model, the Piecewise, the Exponential and the Boeing curves (Thomas *et al.*, 1986; Couto and Teixeira, 2004). The question of which model is the most precise for each construction activity has been the object of several studies, in which researchers have compared the performance of various mathematical models against case studies. Among these studies those made by Thomas *et al.* (1986) and primarily by Everett and Farghal (1994) can be highlighted.

According to Everett and Farghal, for 60 frequent types of construction work the Linear Model (LOGx, LOGy) (or Straight Line Model) offers better predictions while the Cubic Models offer better correlation with past information (Everett and Farghal, 1994).

Principle bases of the Linear Model

In the Wright Model (Wright, 1936), the duration of a number of repetitive activities decreases with a constant rate. It is named the 'Straight Line Model' because the learning curve is a straight line in logarithmic coordinates (Thomas *et al.*, 1986), as illustrated in Figure 1. The mathematical equation is as follows:

$$Y = AX^{-n}; \quad (1)$$

with Y the cost, man-hours or time required to perform a repeated generic unit X, A is the cost, man-hours or time necessary to perform the first unit and n the slope of the logarithmic line. Equation 1 can be logarithmically represented as follows:

$$\log_{10} Y = \log_{10} A - n \log_{10} X. \quad (2)$$

The learning rate L is expressed in percentage and may be obtained from the slope of the logarithmic learning line, or vice-versa, as follows:

$$L = 2^{-n} \text{ or } n = -\frac{\log_{10} L}{\log_{10} 2}. \quad (3)$$

The higher the learning (resulting in an increase in production), the greater the slope of the learning curve and the smaller the learning rate.

In order to define the equation of the learning curve, the value of A must be known and the value of the learning rate must be assumed. Alternatively, the values of A and Y for the kth repetition (for example for k=1), defines the line.

Survey

A survey was made of a set of seven identical housing developments built in the Porto area during the year

2002. Each project consists of several buildings with similar characteristics. The data collected refer to the concrete frame of those buildings, which basically comprises cast *in situ* concrete elements such as columns, beams, walls and slabs. This corresponds to a typical building structure in Portugal and is therefore interesting for analysis. Data from the construction tasks required for the erection of each building floor level have been aggregated into a single construction activity, and the corresponding duration has been computed in terms of man-hours.

The results of this work are summarized in the tables below. Each table relates to a specific project and includes data from the buildings comprised in it. Total man-hours required for erecting each floor level on each building are depicted on the corresponding shaded row.

A first glance at these data clearly show the importance of the learning effect in repetitive construction. Assuming that planned man-hours for the first floor are identical to man-hours recorded for that floor, productivity gains have reached as much as 33% in the best projects, but they were revealed to be negligible, at worst. Moreover, data collected provide evidence of similar productivity evolution in each table, that is to say that buildings pertaining to the same development followed identical learning patterns. This may be possibly explained by the effect of similar site conditions and site management.

A further analysis of the data has shown that it could be reasonably approached by a two-stage learning curve, instead of the three-stage model of Figure 1 above. Although some initial increase in productivity may possibly exist, the effect of this is likely to be diluted in the performance of the elementary tasks of the first level. Accordingly, the number of man-hours required for each building floor has been computed at a constant learning rate up to a level where no further productivity increase has been recorded. The same number of man-hours has been used for the upper floor levels. These results are depicted on the second and third rows in the tables and correspond to the second and third stages of Figure 1.

The curve corresponding to a constant learning rate (actually, a straight line in logarithmic coordinates as shown in Figure 1) has been fitted to data collected through a minimum square of differences approach. The calculation of man-hours required for erecting each floor is very easy after Equation 3. The platform corresponding to no further learning (or to a learning rate of 100%) tends to be achieved no earlier than the fifth repetition in all projects surveyed. For the whole, the differences between actual project durations and computed durations have been minimized.

A more detailed analysis of each project allows for other interesting conclusions. Project SGL (Table 1)

reveals typical learning curves with identical learning rates of roughly 83% for all buildings. SGL2B and SGL3B evidence interruptions in the learning processes on the fourth level, with further reflections on the upper two levels. This may have resulted from changes in the work crews involved in the project on that occasion.

For project INFOC (Table 2) it was not possible to detect any learning effect because data recorded on site are very erratic. This may be due to poor management, constant variations, many changes in the work crews, etc.

Project IDF (Table 3) shows the effect of disturbing the project sequence (because of holidays). The learning process was interrupted and recovered later. A better approach to this would possibly be through a new learning curve after the disruption (see case study B below). The survey reported above shows that the learning process is dependent on a number of factors, namely:

- Project characteristics some projects allow for larger learning than others. Slight differences between successive floors may force the learning rate to increase.
- Project variations – these may impose changes in earlier provisions and introduce delays.
- Changes in the work crew – new crewmembers need time to adapt thus slowing down the learning evolution and introducing delays.
- Replacement of work crews or subcontractors – the replacement of work crews or subcontractors resets the learning process.
- Poor management – lack of work preparation or insufficient production factors may introduce delays, leading to the frustration and demotivation of workers, which in turn is reflected in lower productivity.

In view of the above it may be concluded that in order to benefit from the learning effect, building design must be appropriate, careful site preparation is needed, few changes in work teams ought to be allowed and efficient management is required. For projects fulfilling these characteristics, a learning rate of not less than 85% in no more than five succeeding floor repetitions appears to adequately fit site productivity. These results have been used in two case studies, as reported in the next section.

Case studies

Case study A

Case study A is about the construction of a concrete structure for a building comprising basement, ground

[illegible]

Table 2 Project INFOC

Building	Durations	Learning rates	Floor levels									Total duration	Diff
			1	2	3	4	5	6	7	8	9		
INFOC 3A	Actual duration		14	11	9	10	10	9	9			58	8
	Computed duration	92%		11.00	10.12	9.64	9.31	9.06	8.87				
	Computed duration	100%							8.87			58.00	0%
INFOC 3B	Actual duration		19	9	10	8	8	10	11			56	-2
	Computed duration	100%		9.00	9.00	9.00	9.00	9.00					
	Computed duration	100%										45.00	-20%
INFOC 3C	Actual duration		17	10	9	11	9	11	9	12		71	-1
	Computed duration	100%		10.00	10.00	10.00	10.00	10.00	10.00				
	Computed duration	100%							10.00	10.00		70.00	-1%
INFOC 4A1	Actual duration		14	11	9	31	8	9				68	-13
	Computed duration	87%		11.00	9.57	8.82	8.33	7.96					
	Computed duration	100%										45.68	-33%
INFOC 4A2	Actual duration		15	9	10	10	9	9				47	-2
	Computed duration	100%		9.00	9.00	9.00	9.00	9.00					
	Computed duration	100%										45.00	-4%
INFOC 4B1	Actual duration		14	11	15	10	11	10				57	-2
	Computed duration	100%		11.00	11.00	11.00	11.00	11.00					
	Computed duration	100%										55.00	-4%
INFOC 4B2	Actual duration		8	7	10	11	9	11				48	-13
	Computed duration	100%		7.00	7.00	7.00	7.00	7.00					
	Computed duration	100%										35.00	-27%

Table 3 Project IDF

Building	Durations	Learning rates	Floor levels												Total duration	Diff
			1	2	3	4	5	6	7	8	9	10	11	12		
IDF 16	Actual duration		16	13	8	10	8	8	9	11	9	7	8		78	-6
	Computed duration	100%			8.00	8.00	8.00	8.00	8.00	8.00						
	Computed duration	100%								8.00	8.00	8.00	8.00		72.00	-8%
IDF 17	Actual duration		19	10	10	9	8	8	10	9	9	7	7		77	13
	Computed duration	92%			10.00	9.20	8.76	8.46	8.24	8.06						
	Computed duration	100%								8.06	8.06	8.06	8.06		76.91	0%

Table 4 Case study A

Building	Durations	Learning rates	Floor levels											Total durations	Diff
			1	2	3	4	5	6	7	8	9	10	11		
CSA	Actual duration		14	11	12	9	9	8	9	10	8	8		73	23
	Computed duration	85%			12.00	10.20	9.27	8.67	8.23	7.88					
	Computed duration	100%								7.88	7.88	7.88		72.02	-1%

Table 5 Calculation of duration periods per floor according to the linear model, case A

Storeys		X-index	Actual duration/floor	Accumulated actual duration	Planned duration/floor	Accumulated planned duration
1 st Phase	Basement	–	(14)	–	–	–
	Ground floor	–	(11)	–	–	–
	1st floor	1	12	12	12	12
	2nd floor	2	9	21	10.2	22.2
	3rd floor	3	9	30	9.27	31.47
	4th floor	4	8	38	8.67	40.14
	5th floor	5	9	47	8.23	48.37
	6th floor	6	10	57	7.88	56.26
2 nd Phase	7th floor	2	8	65	7.88	64.14
	8th floor	3	8	73	7.88	72.02

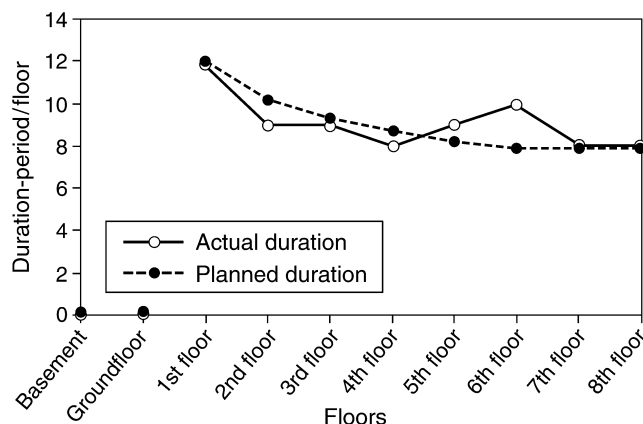


Figure 2 Variation of the duration period/floor - case A

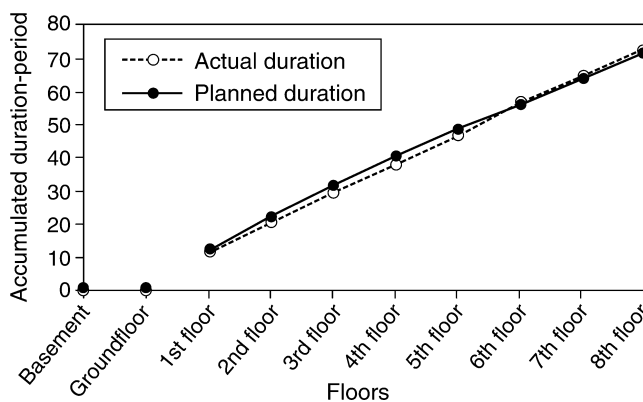


Figure 3 Production graphic - case A

floor and eight identical upper floors. An increase in productivity of 15% corresponding to a learning rate of 85% has been recorded from the first to the sixth floor. No increase has been found for the last

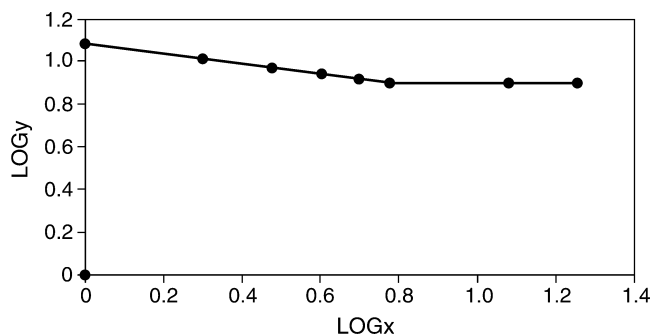


Figure 4 Learning curve - case A

two floors. The basement and the ground floor have not been considered in this process. Results are shown in Table 4 that have a similar shape to the preceding ones. The production value for the sixth floor is abnormally large, possibly due to some management problems.

Table 5 summarizes previous results and furnishes accumulated man-hours for each floor-level. The average man-hour consumption was nine per floor, thus corresponding to a 23% saving when compared to the activity duration of the first floor.

Figures 2 and 3 show that the production planned graphic closely approaches the actual production graphic. For the seventh and eighth floors, the production line is horizontal, which means no additional learning.

The above observations may be confirmed by analysing the learning curve of the project, as illustrated in Table 6 and Figure 4.

Case study B

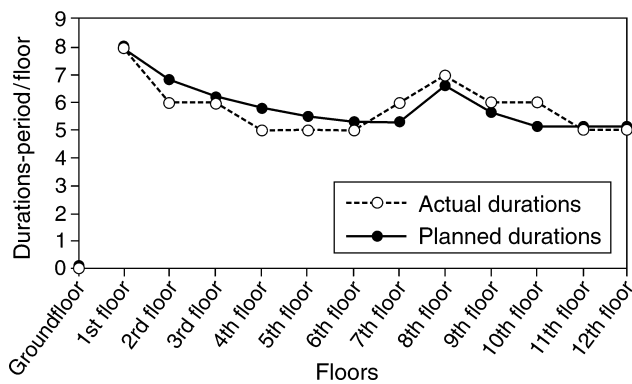
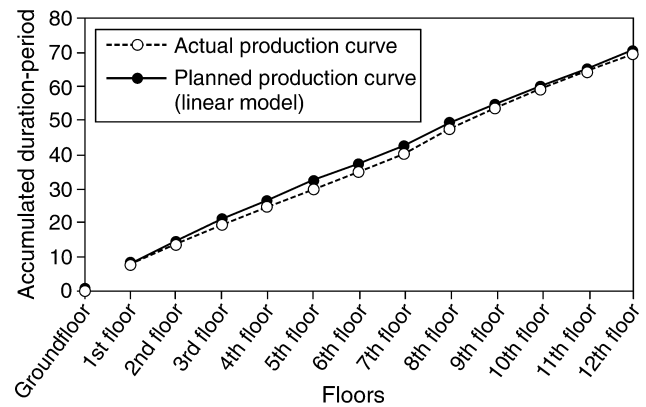
Case Study B is about the construction of a concrete structure for a building of 12 similar floors. A two-stage learning approach has been adopted with identical

Table 6 Calculating the learning curve, case A

	Storeys	X-index	LOGx	Y – time/floor	LOGy	LOGx Accumulated
	Basement	–	–	–	–	–
	Ground floor	–	–	–	–	–
1st Phase	1st floor	1	0.00	12.00	1.08	0.00
	2nd floor	2	0.30	10.20	1.01	0.30
	3rd floor	3	0.48	9.27	0.97	0.48
	4th floor	4	0.60	8.67	0.94	0.60
	5th floor	5	0.70	8.23	0.92	0.70
	6th floor	6	0.78	7.88	0.90	0.78
2nd Phase	7th floor	2	0.30	7.88	0.90	1.08
	8th floor	3	0.48	7.88	0.90	1.26

Table 8 Calculation of duration periods per floor according to the linear model, case B

	Storeys	X-index	Actual duration/floor	Accumulated actual duration	Planned duration/floor	Accumulated planned duration
	Ground floor	—	—	—	—	—
1st Phase	1st floor	1	8	8	8.00	8.00
	2nd floor	2	6	14	6.80	14.80
	3rd floor	3	6	20	6.18	20.98
	4th floor	4	5	25	5.78	26.76
	5th floor	5	5	30	5.49	32.25
2nd Phase	6th floor	6	5	35	5.26	37.50
	7th floor	2	6	41	5.26	42.76
3rd Phase	8th floor	1	7	48	6.63	49.39
	9th floor	2	6	54	5.63	55.02
4th Phase	10th floor	3	6	60	5.12	60.14
	11th floor	2	5	65	5.12	65.27
	12th floor	3	5	70	5.12	70.39

**Figure 5** Variation of the duration-period/floor - case B**Figure 6** Production graphic - case B**Table 9** Calculating the learning curve, case B

	Storeys	X-index	LOGx	Y – time/floor	LOGy	LOGx accumulated
	Ground floor	—	—	—	—	—
1st Phase	1st floor	1	0.00	8.00	0.90	0.00
	2nd floor	2	0.30	6.8	0.83	0.30
	3rd floor	3	0.48	6.18	0.79	0.48
	4th floor	4	0.60	5.78	0.76	0.60
	5th floor	5	0.70	5.49	0.74	0.70
2nd Phase	6th floor	6	0.78	5.26	0.72	0.78
	7th floor	2	0.30	5.26	0.72	1.08
3rd Phase	8th floor	1	0	6.63	0.82	1.08
	9th floor	2	0.30	5.63	0.75	1.38
4th Phase	10th floor	3	0.48	5.12	0.71	1.56
	11th floor	2	0.30	5.12	0.71	1.86
	12th floor	3	0.48	5.12	0.71	2.03

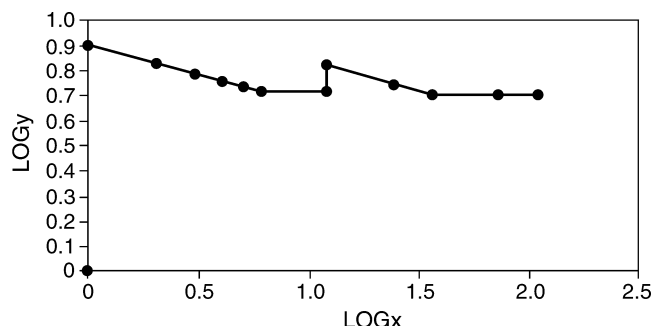


Figure 7 Learning curve - case B

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