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Estimating project and activity duration: a risk management approach using network analysis

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Variations in the durations of activities are commonplace in the construction industry. This is due to the fact that the construction industry is influenced greatly by variations in weather, productivity of labour and plant, and quality of materials. Stochastic network analysis has been used by previous researchers to model variations in activities and produce more effective and reliable project duration estimates. A number of techniques have been developed in previous literature to solve the uncertain nature of networks, these are: PERT (program evaluation and review techniques), PNET (probabilistic network evaluation technique), NRB, (narrow reliability bounds methods) and MCS (Monte Carlo simulation). Although these techniques have proved to be useful in modelling variations in activities, dependence of activity duration is not considered. This can have a severe impact on realistically modelling projects. In this context, the objective of the present research is to develop a methodology that can accurately model activity dependence and realistically predict project duration using a risk management approach. A simulation model has been developed to encapsulate the methodology and run experimental work. In order to achieve this, the following tasks are tackled: identify risk factors that cause activity variations using literature reviews and conducting interviews with contractors; model risk factors and their influence on activity variations through conducting case studies and identifying any dependence between them; develop a computer based simulation model that uses a modified Monte Carlo technique to model activity duration and dependence of risk factors; and run experimental work to validate and verify the model.

Keywords: Network analysis, Monte Carlo simulation, PERT, stochastic analysis

Background

Uncertainty in network analysis has been used by previous researchers in an attempt to model activity duration variations more accurately and produce more effective and reliable project duration estimates. Variations of activity duration do occur due to the exposure of construction projects to numerous uncontrollable risk factors. Several probabilistic methods have been developed to solve the problem of uncertainty in network analysis. Amongst these methods are (Illumoka, 1987; Chapman, 1990): PERT (program evaluation and review technique), PNET (probabilistic network evaluation technique), NRA (narrow reliability

bounds), and MCS (Monte Carlo simulation). Diaz and Hadipriono (1993) found that PERT is the simplest method and yields the most optimistic results, while MCS produces the most conservative results. They used several types of network and the evaluation is based on survival function and computer time. Ranasinghe (1994) has introduced an equation to model the uncertainty in activity duration, and developed a quantification for uncertainty in project duration.

The research in the area of uncertainty in network analysis which has been developed over the last decade has refined the techniques used; however, a number of problems still exist. Uncertainty in analysis is applied with survival of the project in mind, rather than

applying it to projects with the survival of the company as the basis of the decision. Obviously, before the uncertainties of projects can be combined a good understanding of the uncertainties in each project is needed. Furthermore, the techniques used still need enhancing to produce more accurate models of the interactions between uncertainties and activities variations. In this context it is hypothesized in this research that unless some form of dependence between activity variations exist, accurate modelling of uncertainty in networks is unattainable. The objective of this research is to explore a methodology, based on a risk management approach, that models variations in the duration of activities and their dependence on risk factors. It is hypothesized that such a methodology can improve project duration estimates and provide practitioners with a tool for testing several mitigating strategies to counter detrimental events and their influence on project duration.

The following tasks have been performed to achieve the objective. (i) Identify risk factors that cause activity variations using a literature review and conducting interviews with contractors. (ii) Model risk factors and activities' duration variations and identify dependence between them. (iii) Develop a simulation model to encapsulate and test the new methodology. (iv) Run experimental work on case studies to validate the methodology.

Methodology

In this section the proposed methodology of modelling variations in the duration of activities and their dependence on risk factors is discussed. It is assumed

that there are a number of risk factors that might cause variation in activity duration, and their influence can differ from one activity to another. In general, the following are considered to be the risk factors.

- Type of soil and site condition
- Weather conditions
- Material and equipment failure
- Incomplete design scope
- Defective design
- Design changes
- Fluctuation in labour productivity
- Artificial obstruction
- Subcontractors default
- Landslide

Each of the above factors can be modelled using a representative distribution and have a minimum value (0) and a maximum value (1). As in MCS, random numbers for each risk factor are generated from a particular representative distribution. The type of distribution can vary from one activity to another or can be kept fixed for the project once it has been generated. It is proposed that certain risk factors will have the same influence on the project regardless of time, for example, type of soil and site condition, labour productivity, etc. On the other hand, other risk factors might be changed with time and might have different values from one activity to another, for example, weather conditions, equipment failure, incomplete design, design defect, etc. In this case, random numbers will be generated for each activity or for a particular time in the project calendar. Several distributions are used to model risk factors, as shown in Table 1 (Bekr, 1990).

Table 1 The distributions, their possible use and the parameters required

Name	Use	Parameters	Application
Event	Where there is a risk an event can occur	Outcome and probability	Equipment failure
Rectangle	Where there is an equal chance of outcome between two values	The lower and upper extremes	Design changes and incomplete design scope
Triangle	Where the outcome is between two extremes and the tendency is towards one outcome	The lower and upper and the most likely outcome	Weather condition, labour productivity, materials delay, soil conditions
Trapezium	Where there is a range between which the outcomes are equally likely, and the probability of an outcome beyond that range decreases the further away from it, towards the extreme outcome	The lower and upper extremes and the lower and upper likely outcomes	Weather, subcontractors default

The influence of each risk factor on variations of activity duration should be established. As an example, Table 2 shows a matrix that gives the influence of the risk factors on variations of activity duration. As can be seen, each risk factor has a certain contribution on activity variations (risk factor 1 has 20% influence on duration variations in activity A). The total influence of all factors should be 100% on any given activity. In reality the influence of factors will be assessed judgementally through knowledge elicitation. This will be discussed later in the paper.

Once distribution has been allocated (using a combination of historical data and knowledge of distribution theories) to risk factors and the influence matrix is developed, the remaining task is the calculation of activity duration. In order to achieve this, the following equation is developed:

$$\begin{aligned} \text{Duration of activity A} = & \text{MinTime} + \\ & [\text{MaxTime} - \text{MinTime}] \times \\ & [(\text{RF}_1 \times \text{Random}_1) + \\ & (\text{RF}_2 \times \text{Random}_2) + \\ & (\text{RF}_3 \times \text{Random}_3) + \dots + \\ & (\text{RF}_n \times \text{Random}_n)] \end{aligned}$$

where MinTime is the minimum duration that can be assigned to an activity, MaxTime is the maximum duration that can be assigned to an activity, RF_n is the influence of risk factor n on a particular activity (from activity/risk factor matrix), and Random_n is a random number that should be generated using a representative distribution of risk factor n .

Table 2 Activity/risk factors matrix

Activity	RISK FACTOR						Sum
	1	2	3	4	5	6	
A	20%	20%	40%	0	0	20%	100%
B	0	0	0	50%	40%	10%	100%
C	20%	20%	40%	0	0	20%	100%
D	100%	0	0	0	0	0	100%
E	50%	50%	0	0	0	0	100%

Table 3 An example to illustrate the developed equation for activity A of max duration 20 and min duration 10. Influence factors RF_1 , RF_2 , RF_3 and RF_4 are all 25%.

Run	Rand ₁	Rand ₂	Rand ₃	Rand ₄	Rand ₁ * RF_1	Rand ₂ * RF_2	Rand ₃ * RF_3	Rand ₄ * RF_4	Duration of activity
1	1	1	1	1	0.25	0.25	0.25	0.25	20
2	0	0	0	0	0	0	0	0	10
3	0.5	0.5	0.5	0.5	0.06	0.06	0.06	0.06	12.5
4	1	1	0	0	0.25	0.25	0	0	15

In order to illustrate the above equation, Table 3 shows an example of four runs for activity A. As can be seen, in Run 1 all risk factors have materialized to the very extreme and the duration of the activity is 20, which is the maximum. In Run 2 none of the risk factors has materialized and the duration of the activity is the minimum, 10. Run 3 shows a duration of 12.5 days resulted from 50% materialization of each risk factor. Finally, Run 4 shows the results of having two risk factors, 1 and 2, with 100% materialization. In order to validate the methodology, a simulation model has been developed using the Turbo-Pascal platform. The model encapsulates risk factors, their distribution and influences on each activity and the logic of a given project. The following section introduces a hypothetical case study to illustrate the proposed methodology.

Case study

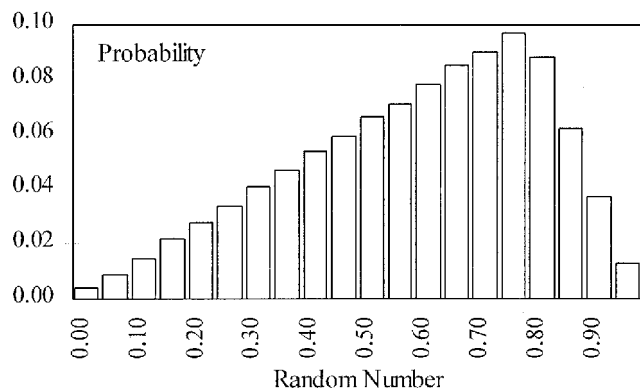
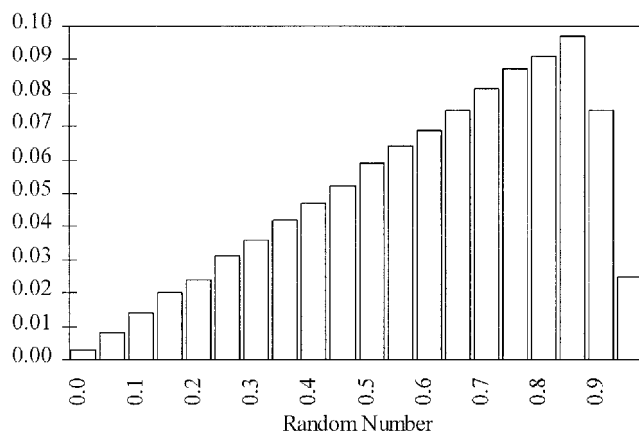
The case study is a small civil engineering project as shown in Table 4. The risk factors that affected each activity in the project and their influence are given in Table 5. The distributions representing the possible outcome of each risk factor are also given in Table 5. A suitable distribution has been allocated to each risk factor using site information and judgement. The quantification of the risk factors has been achieved through selecting a probability distribution which shows the possible outcomes of the variables and the relative likelihood of each possible outcome. Figures 1, 2 and 3 show the distributions of weather, soil and

Table 4 Logic of the project

Activity	Activity No.	Preceded by	Followed by	Min. duration	Max. duration
Start	1	Nil	Pile&Cap E Pile&Cap C Pile&Cap W	0	0
Pile&Cap E	2	Start	SubStr E	18	29
Pile&Cap C	3	Start	SubStr C	13	22
Pile&Cap W	4	Start	SubStr W	4	12
SubStr E	5	Pile&Cap E	Insitu Span	18	29
SubStr C	6	Pile&Cap C	Insitu Span	13	22
SubStr W	7	Pile&Cap W	PC Span	15	25
Insitu Span	8	SubStr E SubStr C	Surface	25	35
PC Span	9	SubStr C SubStr W	Surface	2	8
Surface	10	Insitu Span PC Span	Finishes	2	7
Finishes	11	Surface	End	10	18
End	12	Finishes	Nil	0	0

Table 5 Risk factors influencing the project's activities

Risk factors	Distribution	Mean	STD	Act 2	Act 3	Act 4	Act 5	Act 6	Act 7	Act 8	Act 9	Act 10	Act 11
Weather	Triang (0,0.8,1)	0.59	0.21	0.30	0.30	0.30	0.30	0.30	0.30	0.40	0.10	0.50	0.50
Soil	Triang (0,0.9,1)	0.63	0.22	0.40	0.40	0.40	0.10	0.10	0.10	0.00	0.00	0.00	0.00
Productivity	Triang (0,1)	0.28	0.2	0.15	0.15	0.15	0.30	0.30	0.30	0.30	0.30	0.20	0.20
Equipment	Event (0,0.6,1)	0.53	0.21	0.15	0.15	0.15	0.10	0.10	0.10	0.10	0.20	0.15	0.15
Delay of materials	Triang (0,0.6,1)	0.53	0.21	0.00	0.00	0.00	0.20	0.20	0.20	0.20	0.40	0.15	0.15
Sum				1	1	1	1	1	1	1	1	1	1

**Figure 1** Distribution of weather**Figure 2** Distribution of soil

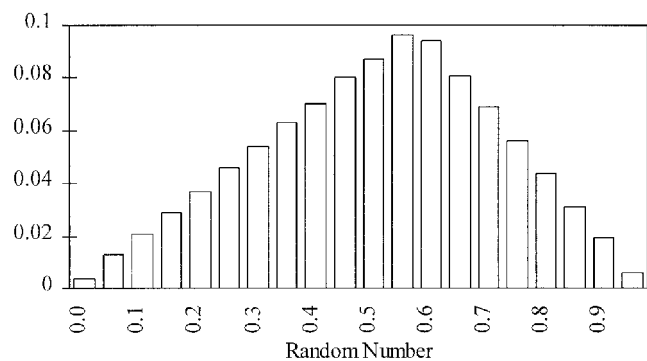


Figure 3 Distribution of reliability of equipment

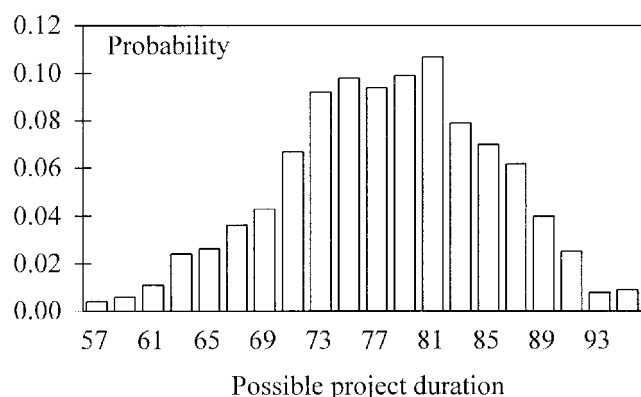


Figure 4 Distribution for the project duration: number of runs 1000, min. value 57 days, max. value 94 days, average 78.7 days, SD 7.5, and skewness -0.115

reliability of equipment, respectively. The influence of each risk factor on the activity duration is assigned. Obviously, the influence of the risk factors should affect the outcome of the project, and a range of experimental work can be designed to investigate the risk factors. It should be mentioned that the objective of this paper is to present the methodology and its operation. Construction managers should be able to use it as a test bench to pinpoint the effect of risk factors on their projects. The distributions that represent the risk factors might differ from project to project and therefore the methodology is designed to accept a wide range of distributions to suit particular applications.

Analysis of the results

Having described and quantified the uncertainty of the risk factors, the next stage is to determine the combined effect of uncertainties on the project duration and to identify the factors which contribute

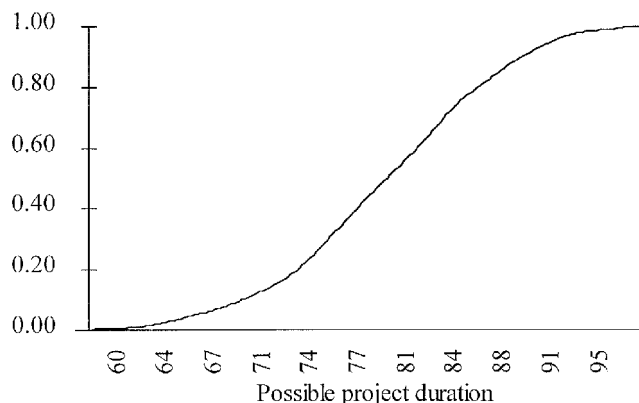


Figure 5 Cumulative distribution for project duration

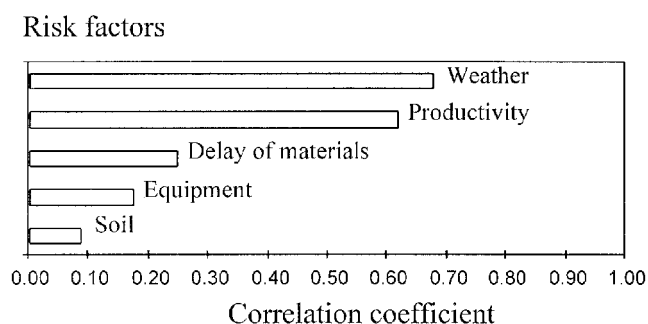


Figure 6 Correlation of the risk factor with project duration

significantly to the total. The results of the runs are compared with Monte Carlo simulation using the Beta distribution to model activity variations. Figure 4 shows the results generated from 1000 iterations of the model; the minimum duration (optimistic) of the project is 57 days and the maximum duration (pessimistic) is 94 days. The mean value of the project duration is 78.7 days with 7.5 standard deviation and -0.115 skewness (i.e. the mean is shifted towards the pessimistic value). The cumulative density function in Figure 5 indicates that around 80% of the results are between 74 and 94 days. In order to identify the influence of the risk factors on the duration of the project, a correlation analysis between the risk factors and project duration is conducted. Figure 6 shows that weather and productivity have a high correlation (0.68 and 0.62, respectively) and this is regarded as a strong influence on the project duration compared with other factors. This type of analysis should help project management on focusing on the risk factors that influence the project duration substantially.

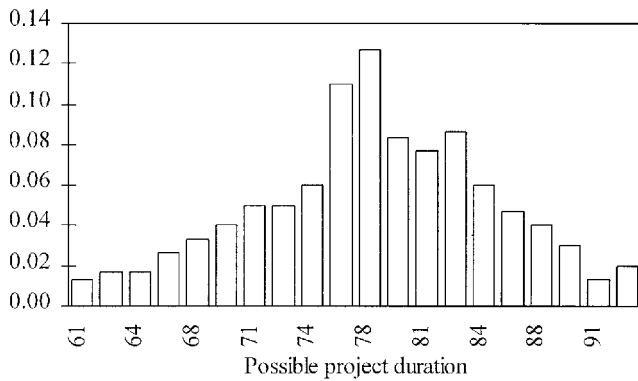


Figure 7 Beta distribution for the project

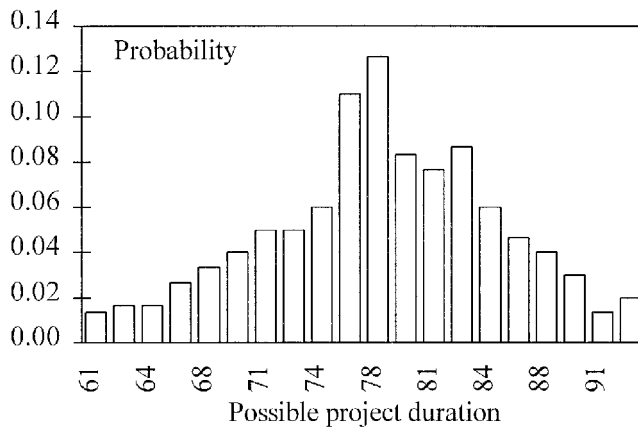


Figure 8 Cumulative distribution for the project: number of runs 1000, min. value 61 days, max. value 94 days, average 78 days, SD 6.9, and skewness -0.21

In order to compare the results generated from the proposed methodology with the traditional PERT approach, the model was allowed to run the same case study using the Beta distribution. The maximum and minimum values for each activity that were used in the Beta distribution are shown in Table 4. Figures 7 and 8 show the results generated from 1000 iterations of the case study, and the results are similar to the proposed methodology; however, the PERT solution has provided a slightly lower standard deviation (6.9) and a higher skewness of (-0.21) . The PERT approach has produced an overall expectation of the project duration without any indication regarding the causes of such wide outcomes in the project duration.

Risk response

Having identified the possible outcomes of the project duration, the management needs to identify the possibility of reducing the variations and minimizing the

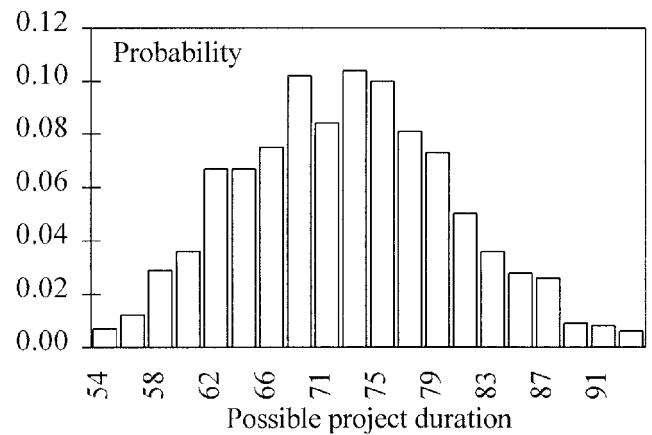


Figure 9 Distribution for the project duration

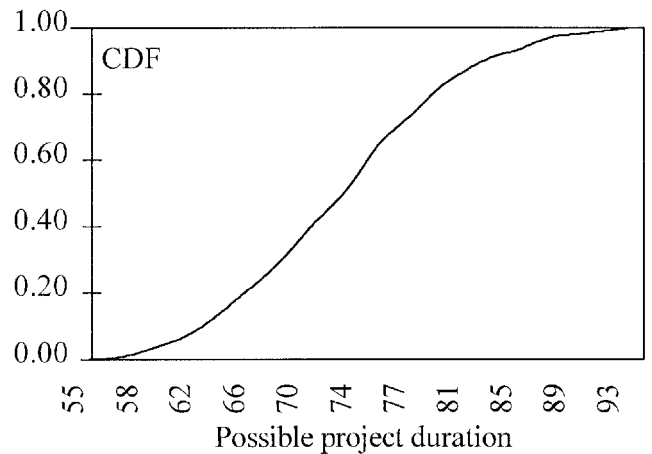


Figure 10 Cumulative distribution for the project duration: number of runs 1000, min. value 54.4 days, max. value 94.661 days, average 72.9 days, SD 7.7, and skewness 0.17

pessimistic part of the project duration. The methodology developed is well suited to targeting the detrimental effect of the risk factors and consequently reducing the impact of such factors. In the case study, it was concluded that the weather and productivity risk factors have a strong impact on the project duration, and the intention is to reduce the effect of these factors. In order to achieve this, it was suggested that the project used in the case study be constructed over the summer; this way, the effect of the weather can be minimized. 1000 iterations were run using the same information presented in Table 4 and changing the mean of the weather distribution to (0.2). Figures 9 and 10 show that the possible project duration has been shifted towards the optimistic part. It can be seen that the mean value is 54 days with skewness of 0.17. More experimental work is under way with the objective of minimizing the detrimental effect of the risk

factor. From Figures 9 and 10 it can be concluded that the detrimental effect of the risk factors can be minimized and a more optimistic duration can be produced. However, the question to be asked is: at what cost can this be achieved? Management should be able to evaluate the cost/benefit of each option. This subject is under investigation.

Figures 11–14 show the results of a set of experiments designed to demonstrate the effect of varying certain risk factors while keeping the rest fixed. The objective is to examine the sensitivity of the projects towards certain risk factors. Figure 11 shows the distribution of the project duration while varying only the weather factor and fixing the rest of the factors. Compared with Figure 4 (varying all risk factors), the

results suggest that the spread of data in Figure 11 is smaller (SD 5.2, min. 64, max. 88), however, the project is still risky, quite sensitive to the influence of weather and needs management attention to counter the uncertainty in the project. Figure 12 shows the distribution of the project duration while varying only the soil risk factors, and the spread of data is reduced further (SD 5.8, min. 75, max. 80) and the uncertainty is minimized. Figure 13 shows the distribution of the project duration while varying only the weather and soil factors, and in Figure 14 all the risk factors except productivity are varied. The figures show that the spread of data is wider than in Figures 11 and 12, and the project is highly uncertain and sensitive to weather and soil factors when they are combined.

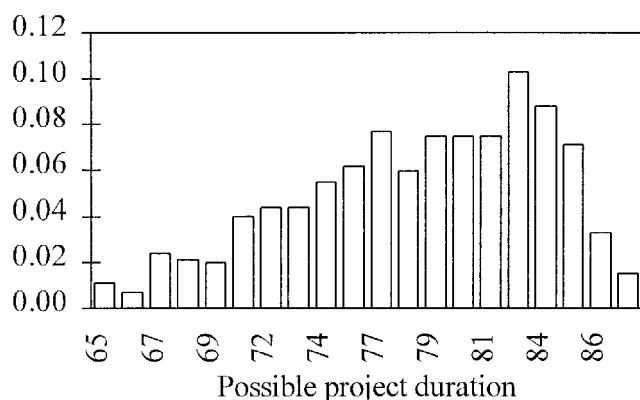


Figure 11 Distribution for the project duration, varying just the weather factor: number of runs 1000, min. value 64 days, max. value 88 days, average 78 days, and SD 5.2

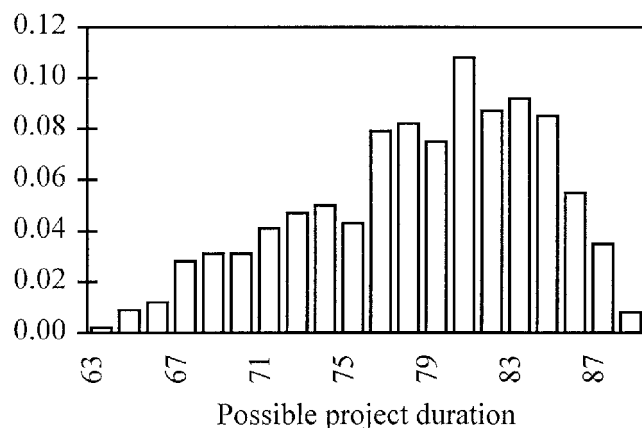


Figure 13 Distribution for the project duration, varying just the weather and soil risk factors: number of runs 1000, min. value 63 days, max. value 69 days, average 78 days, and SD 5.8

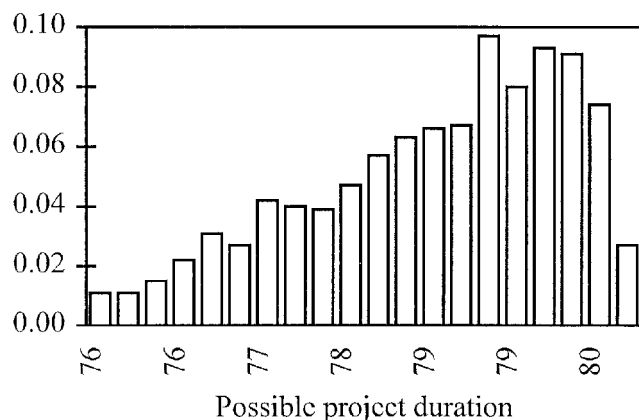


Figure 12 Distribution for project duration, varying just the soil risk factor: number of runs 1000, min. value 75 days, max. value 80 days, average 78 days, and SD 5.8

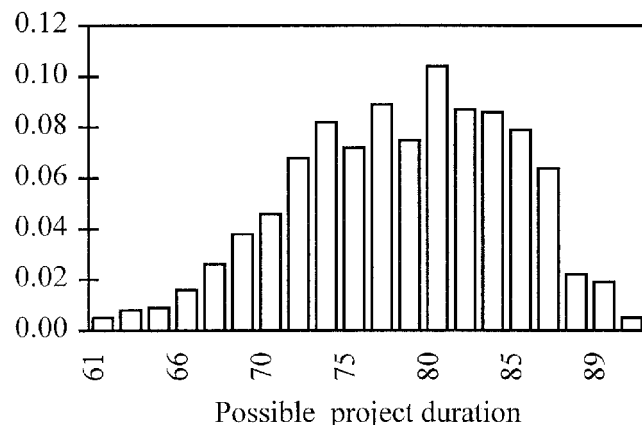


Figure 14 Distribution for the project duration, varying all the risk factors except productivity: number of runs 1000, min. value 60 days, max. value 92 days, average 78 days, and SD 6.1

Conclusions

The objective of this research is to explore a methodology that models variations in the duration of activities and their dependence on risk factors. It is hypothesized that such a methodology can improve project duration estimates and provide practitioners with a tool for testing several mitigating strategies to counter detrimental events and their influence on project duration.

A case study has been used to illustrate the methodology and a simulation model has been developed and used to encapsulate this methodology. It is concluded that the results generated using the methodology are very beneficial to forecasting project duration accurately and estimating the impact of risk factors on project duration. It should be mentioned that the practical application of this method has a number of limitations, e.g.: allocation of the influence of the risk factors on variations of activity duration needs considerable experience and judgement; identifying and modelling risk

factors is highly judgmental and there is room for mistakes; and the methodology is dependent on historical data and most construction companies do not have accurate records of construction sites.

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