## PHYSICS

## Bilevel Optimization for Automated Machine Learning: A New Perspective with Framework and Algorithm

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## **ABSTRACT**

**Keywords:** Automated Machine Learning, Bilevel Optimization, Meta Feature Learning, Neural Architecture Search, Hyperparameter Optimization

Machine Learning (ML) has witnessed an unprecedented evolution in recent years, becoming a key driver of building artificial intelligence system. With cutting-edge technologies such as AlphaGo [1] and ChatGPT [2], the power and versatility of ML have been demonstrated across diverse applications. However, designing effective ML solutions in real-world application scenarios can be challenging and time-consuming, thus paving the way for the emergence of Automated Machine Learning (AutoML). AutoML refers to a set of technologies that streamline the entire process of applying ML to complex problems by automating many of the traditionally manual tasks involved in ML. By doing so, AutoML enables the generation of more powerful ML solutions and extends their scope of applicability [3].

In this perspective, we would like to investigate the intrinsic mechanisms and (re)formulate these different AutoML tasks from a unified optimization perspective. Fig. 1 (a) illustrates how we can view the process of AutoML as addressing the three key issues of ML tasks: "how to extract learning feature", "how to construct learning model", and "how to design learning strategy". These three issues correspond to the main techniques of AutoML, namely Meta Feature Learning (MFL), Neural Architecture Search (NAS), and Hyper-parameter Optimization (HO), respectively.

In essence, MFL enables us to automatically extract relevant features for unseen new tasks [4], NAS helps us to design effective neural network architectures [5], and HO assists in finding optimal hyper-parameters for the model [6].

By automating these key aspects of the ML pipeline, AutoML frees up valuable time and resources for practitioners to focus on other critical tasks. Overall, the techniques of MFL, NAS, and HO play crucial roles in enabling AutoML to efficiently and effectively handle ML tasks. Very recently, Shu et al. [7] provided Simulating Learning Methodology (SLeM), a general paradigm with solid theoretical guarantees for predicting proper hyper-parameter configurations for various AutoML applications.

Bi-Level Optimization (BLO) refers to a category of mathematical tools for hierarchical optimization with two levels of problems: an upper-level problem and a lower-level problem [8]. In the context of AutoML, we actually can utilize BLO to uniformly formulate different kinds of AutoML tasks, such as MFL, NAS and HO.

Specifically, we can observe in Fig. 1 (b) that in the upper-level problem, the goal is to find the best "Methodology", that optimize the performance of the machine learning model (e.g., meta features, network architectures, and tuned hyperparameters). This can be formulated as an optimization problem where the objective function F is the performance of the model on a validation set  $\mathcal{D}_{val}$ , and the variables  $\mathbf{x} \in \mathcal{X}$  are some "meta-parameters" (e.g., corresponding to feature extraction, network architecture, and learning strategy). The constraints can include factors such as computational resources and time limits. In the lower-level problem, the objective is to optimize the machine learning model itself g, given the mate-parameters chosen in the upper level problem. It can be formulated as an

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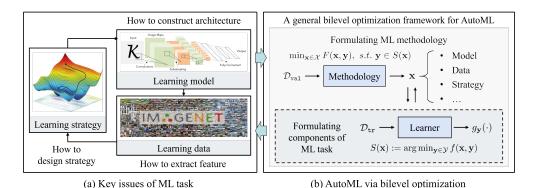


Figure 1. Illustrating key issues of ML task and formulating AutoML paradigm from the perspective of bilevel optimization.

optimization problem where the objective f is the performance of the model on a training set  $\mathcal{D}_{tr}$ , and the variables  $\mathbf{y} \in \mathcal{Y}$  are parameters of the learning model. Therefore, BLO provides a powerful framework for AutoML, enabling automatic selection and optimization of ML models, and making it possible to build high-performing models with minimal manual intervention.

In the field of ML/AutoML, there has been a recent surge in developing gradient-based techniques for BLOs. Two main categories of such algorithms have emerged in recent years: gradient with explicit differentiation and implicit differentiation. The key difference between these two categories lies in the way they compute the coupled gradients for BLOs. Very recently, a series of single-loop techniques have also been proposed to reduce the complexity of computing the coupled gradients [9]. For further information on these recent developments in gradient-based BLOs [8].

Despite the substantial amount of literature in the field, fundamental issues still exist in the current algorithms. One of the major challenges is that many of these studies, including both algorithmic design and theoretical investigations, heavily rely on restrictive conditions such as lower-level singleton and convexity. Although there have been a few attempts to address this issue [10], it remains a significant obstacle. Another challenge is the difficulty in providing strict convergence analysis on the approximated schemes used in practical applications, without exact calculation of coupled gradients [5].

VIltimately, the best approach to solving a specific BLO problem will depend on the problem structure, the complexity of the objective functions and constraints, and the computational resources available. Thus it is important to carefully consider the problem formulation and choose an appropriate algorithm or combination of algorithms to efficiently and accurately solve

the problem.

Last but not least, it is necessary to provide some discussions on the challenging and promising directions of BLOs for AutoML in the future:

- Computational acceleration: As the size and complexity of datasets/tasks continue to increase, there is a pressing need for acceleration techniques to BLO algorithms in extremely large-scale and high-dimensional AutoML applications. This includes designing AutoML algorithms that can efficiently search through a large space of architectures, as well as extracting high-dimensional features and optimizing complex training processes. One promising direction is to explore parallel/distributed computing techniques to accelerate the training and evaluation of models.
- Theoretical breakthrough: Existing theories of gradient-based BLOs are mostly relying on strong assumptions (e.g., lower-level singleton and convexity [8]), which limit their applications in real-world scenarios. Thus it is necessary to establish new analyzing tool, that can systematically analyze the properties of the BLO landscape and design efficient algorithms for challenging AutoML tasks (e.g., tackling non-convex and discrete learning).
- Optimization-inspired AutoML: Currently, BLOs are predominantly recognized as solution strategies for practical AutoML applications. Indeed, by delving into the underlying structure of the AutoML paradigm from the perspective of BLO, we can better capture the complex dependencies between different components of the model and thus has the ability to design more efficient and effective AutoML strategies. For example, integrating SLeM mechanism and prompt learning techniques within the BLO framework for improving the generalization capability of fundamental vision-language models.

## **REFERENCES**

- Silver D, Schrittwieser J, Simonyan K et al. Mastering the game of go without human knowledge. Nature 2017; 354– 359
- 2. van Dis EA, Bollen J, Zuidema W *et al.* Chatgpt: five priorities for research. *Nature* 2023; 224–226.
- Feurer M, Klein A, Eggensperger K et al. Efficient and robust automated machine learning. Neural Information Processing Systems (2015) 1145–1153.
- Finn C, Abbeel P and Levine S. Model-agnostic metalearning for fast adaptation of deep networks. *International Conference on Machine Learning* (2017) 1126–1135.
- Liu H, Simonyan K and Yang Y. DARTS: differentiable architecture search. *International Conference on Learning Representations* (2019) 8652–8665.
- Franceschi L, Donini M, Frasconi P et al. Forward and reverse gradient-based hyperparameter optimization. International Conference on Machine Learning (2017) 1165–1173.
- Shu J, Meng D and Xu Z. Learning an explicit hyperparameter prediction function conditioned on tasks. *Journal* of Machine Learning Research 2023; 1–74.
- Liu R, Gao J, Zhang J et al. Investigating bi-level optimization for learning and vision from a unified perspective: A survey and beyond. IEEE Transactions on Pattern Analysis and Machine Intelligence 2021; 10045–10067.
- Liu R, Liu Y, Yao W et al. Averaged method of multipliers for bi-level optimization without lower-level strong convexity. International Conference on Machine Learning (2023) 21839–21866.
- Liu R, Mu P, Yuan X et al. A general descent aggregation framework for gradient-based bi-level optimization. IEEE Transactions on Pattern Analysis and Machine Intelligence 2022; 38–57.