# Package 'MPAT'

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Type Package

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<b>Description</b> Conduct multiple phenotype genetic association studies based on summary statistics.	
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mports mytnorm	
R topics documented:	
MPAT-package	2
	2
lipids	3
MinP	4
	5
	6
	7
11	8
	9
PC	
PCAQ	_
PCFisher         12           PCLC         13	
PCMinP	
PCO	
SigmaOEstimate	
SigmaXEstimate	
SUM	6
VC	7
Wald	8
WI	8
ndex 20	0

2 **DSUM** 

MPAT-package

Multiple Phenotype Genetic Association Testings by Combining Univariate Testing Summary Statistics.

## **Description**

This package is for conducting multiple phenotype genetic association testings by combining univariate summary statistics for each phentype in GWAS. It contains fourteen methods that can be used in a variety of situations. An overall p-value will be returned for assessing the significance of associations between a SNP and multiple phenotypes. It contains the following functions: PC, PCMinP, PCFisher, PCLC, PCSS, MinP, WI, VC, DSUM, SUM, Wald, mixAda, mixFisher, mix-Tippett, mixVar, mixSD.

#### **Details**

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## Author(s)

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## References

MPAT: an R package for multivariate phenotype association studies.

DSUM

Direct summation of Z-statistics

## **Description**

For SNP, the Z testing statistics for multiple phenotypes are summed together as an overall testing statistic.

#### Usage

DSUM(Z.vec, Sigma)

# **Arguments**

Z.vec Z.vec is a vector representing the Z testing statistics for multiple phenotypes.

Sigma Sigma is the correlation matrix among the Z testing statistics that can be esti-

mated by its sample version over the SNPs.

lipids 3

#### Value

p-value

An overall p-value assessing the association between a genetic variant and multiple phenotypes is returned.

#### Author(s)

Zhonghua Liu <zliu@mail.harvard.edu>

#### References

MPAT: an R package for multivariate phenotype association studies.

## **Examples**

```
data(lipids)
lipids = as.data.frame(lipids)
lipids_zscore = as.matrix(lipids[,c("Zscore.HDL","Zscore.LDL","Zscore.TG","Zscore.TC")])
Sigma = cor(lipids_zscore )
DSUM(Z.vec=lipids_zscore[1,],Sigma) ## p-value for the first SNP
```

lipids

An example data set that contains summary statistics from GWAS studies of four lipids levels.

# Description

This is an example data set that contains summary statistics (Z-scores) for 2000 genetic variants and four lipids levels.

#### Usage

```
data(lipids)
```

#### **Format**

A data frame with 2000 observations on the following 15 variables.

MarkerName SNP names

Allele1 This the allele used as the effect allele

Allele2 This is the "other" allele

W. HDL The sum of the individual study weights (typically, N) for this marker

 ${\tt Zscore.HDL}\ \ Z\ scores\ for\ HDL$ 

Pvalue. HDL P-values for HDL

W.LDL The sum of the individual study weights (typically, N) for this marker

Zscore.LDL Z scores for LDL

Pvalue.LDL P-values for LDL

W. TC The sum of the individual study weights (typically, N) for this marker

Zscore.TC Z scores for TC

Pvalue.TC P-values for TC

4 MinP

```
W. TG The sum of the individual study weights (typically, N) for this marker Zscore. TG Z scores for TG P-value. TG P-values for TG ^{\prime\prime}
```

#### **Source**

http://www.sph.umich.edu/csg/abecasis/public/lipids2010/

#### References

http://www.nature.com/nature/journal/v466/n7307/full/nature09270.html

## **Examples**

```
data(lipids)
head(lipids)
```

MinP

MinP takes the minimum of the p-values for multiple phenotypes as the overall testing statistic.

## **Description**

MinP uses the minimum of the p-values for multiple phenotypes as the overall testing statistic. The p-value of MinP is calculated based on multivariate normal distribution.

## Usage

```
MinP(Z.vec, Sigma)
```

## **Arguments**

 ${\tt Z.vec} \hspace{3em} \hbox{$\tt Z.vec is a vector representing the $\tt Z$ testing statistics for multiple phenotypes.} \\$ 

Sigma is the correlation matrix among the Z testing statistics.

#### Value

p-value An overall p-value assessing the association between a genetic variant and mul-

tiple phenotypes is returned.

## Author(s)

Zhonghua Liu <zliu@mail.harvard.edu>

#### References

MPAT: an R package for multivariate phenotype association studies.

mixAda 5

#### **Examples**

```
data(lipids)
lipids = as.data.frame(lipids)
lipids_zscore = as.matrix(lipids[,c("Zscore.HDL","Zscore.LDL","Zscore.TG","Zscore.TC")])
Sigma = cor(lipids_zscore)
MinP(Z.vec=lipids_zscore[1,],Sigma) ## p-value for the first SNP
```

mixAda

Adaptively select optimal combination coefficient of two independents core statistics based on linear mixed effects model.

# Description

mixAda combines the Z testing statistics for multiple phenotypes at a genetic variant in an adaptive fashion to maximize the power.

#### Usage

```
mixAda(Z.vec, Sigma)
```

#### **Arguments**

Sigma is the correlation matrix among the Z testing statistics.

#### Value

p-value An overall p-value assessing the association between a genetic variant and mul-

tiple phenotypes is returned.

# Author(s)

Zhonghua Liu <zliu@mail.harvard.edu>

## References

MPAT: an R package for multivariate phenotype association studies.

```
data(lipids)
lipids = as.data.frame(lipids)
lipids_zscore = as.matrix(lipids[,c("Zscore.HDL","Zscore.LDL","Zscore.TG","Zscore.TC")])
Sigma = cor(lipids_zscore)
mixAda(Z.vec=lipids_zscore[1,],Sigma) ## p-value for the first SNP
```

6 mixFisher

mixFisher	Combine Z-statistics for multiple phenotypes using Fisher's method in a linear mixed effects model.
	33

# Description

Z-statistics for multiple phenotypes are modeled using a linear mixed effects model. Two independent score testing statistics are combined using Fisher's method.

# Usage

```
mixFisher(Z.vec, Sigma, method)
```

# Arguments

Z.vec	Z.vec is a vector representing the Z testing statistics for multiple phenotypes.
Sigma	Sigma is the correlation matrix among the Z testing statistics.
method	The method to compute the p-value which takes three values: davies,liu and liumod .

## Value

p_group	p-value for the group effects of a genetic variant on the multiple phenotypes
p_individual	p-value for the individual effects of a genetic variant on the multiple phenotypes
p_overall	An overall p-value assessing the association between a genetic variant and multiple phenotypes is returned.

# Author(s)

Zhonghua Liu <zliu@mail.harvard.edu>

#### References

MPAT: an R package for multivariate phenotype association studies.

```
data(lipids)
lipids = as.data.frame(lipids)
lipids_zscore = as.matrix(lipids[,c("Zscore.HDL","Zscore.LDL","Zscore.TG","Zscore.TC")])
Sigma = cor(lipids_zscore )
mixFisher(Z.vec=lipids_zscore[1,],Sigma) ## p-value for the first SNP
```

mixSD 7

mixSD	Combine Z-statistics for multiple phenotypes using inverse standard
	deviation weighting method in a linear mixed effects model.

# Description

Z-statistics for multiple phenotypes are modeled using a linear mixed effects model. Two independent score testing statistics are combined using inverse standard deviation weighting method.

# Usage

```
mixSD(Z.vec, Sigma, method)
```

## Arguments

Z.vec	Z.vec is a vector representing the Z testing statistics for multiple phenotypes.
Sigma	Sigma is the correlation matrix among the Z testing statistics.
method	The method to compute the p-value which takes three values: davies,liu and liumod .

#### Value

p-value An overall p-value assessing the association between a genetic variant and multiple phenotypes is returned.

# Author(s)

Zhonghua Liu <zliu@mail.harvard.edu>

## References

MPAT: an R package for multivariate phenotype association studies.

```
data(lipids)
lipids = as.data.frame(lipids)
lipids_zscore = as.matrix(lipids[,c("Zscore.HDL","Zscore.LDL","Zscore.TG","Zscore.TC")])
Sigma = cor(lipids_zscore)
mixSD(Z.vec=lipids_zscore[1,],Sigma) ## p-value for the first SNP
```

8 mixTippett

mixTippett	Combine Z-statistics for multiple phenotypes using Tippett's method in a linear mixed effects model.

# Description

Z-statistics for multiple phenotypes are modeled using a linear mixed effects model. Two independent score testing statistics are combined using Tippett's method.

# Usage

```
mixTippett(Z.vec, Sigma, method)
```

# Arguments

Z.vec	Z.vec is a vector representing the Z testing statistics for multiple phenotypes.
Sigma	Sigma is the correlation matrix among the Z testing statistics.
method	The method to compute the p-value which takes three values: davies,liu and liumod .

## Value

p_group	p-value for the group effects of a genetic variant on the multiple phenotypes
p_individual	p-value for the individual effects of a genetic variant on the multiple phenotypes
p_overall	An overall p-value assessing the association between a genetic variant and multiple phenotypes is returned.

# Author(s)

Zhonghua Liu <zliu@mail.harvard.edu>

#### References

MPAT: an R package for multivariate phenotype association studies.

```
data(lipids)
lipids = as.data.frame(lipids)
lipids_zscore = as.matrix(lipids[,c("Zscore.HDL","Zscore.LDL","Zscore.TG","Zscore.TC")])
Sigma = cor(lipids_zscore )
mixTippett(Z.vec=lipids_zscore[1,],Sigma) ## p-value for the first SNP
```

mix Var

mixVar	Combine Z-statistics for multiple phenotypes using inverse variance weighting method in a linear mixed effects model.

# Description

Z-statistics for multiple phenotypes are modeled using a linear mixed effects model. Two independent score testing statistics are combined using inverse variance weighting method.

# Usage

```
mixVar(Z.vec, Sigma, method)
```

# Arguments

Z.vec	Z.vec is a vector representing the Z testing statistics for multiple phenotypes.
Sigma	Sigma is the correlation matrix among the Z testing statistics.
method	The method to compute the p-value which takes three values: davies,liu and liumod .

## Value

p-value	An overall p-value assessing the association between a genetic variant and mul-
	tiple phenotypes is returned.

# Author(s)

Zhonghua Liu <zliu@mail.harvard.edu>

## References

MPAT: an R package for multivariate phenotype association studies.

```
data(lipids)
lipids = as.data.frame(lipids)
lipids_zscore = as.matrix(lipids[,c("Zscore.HDL","Zscore.LDL","Zscore.TG","Zscore.TC")])
Sigma = cor(lipids_zscore)
mixVar(Z.vec=lipids_zscore[1,],Sigma) ## p-value for the first SNP
```

10 PC

PC	PC is a function used to combine correlated GWAS summary statistics
	for multiple phenotypes at a genetic locus.

## **Description**

By combining univariate summary statistics for multiple phenotypes, we can obtain an overall association p-value that assess the association between a genetic variant and multiple phenotypes as a whole. PC allows users to conduct dimension reduction by specifying which principal component to use to represent the original multiple summary statistics.

#### Usage

```
PC(Z.vec, Sigma, PCorder)
```

## **Arguments**

Z.vec Z	Livec is a column vector rep	resenting the Wald-typ	e Z testing statistics for mul-
---------	------------------------------	------------------------	---------------------------------

tiple phenotypes.

Sigma is the correlation matrix of the multiple Z testing statistics.

PCorder specifys which principal component to use, it takes integer values. For

example, PCorder=1 means we choose to use the first principal component.

## Value

p-value An overall p-value assessing the association between a genetic variant and mul-

tiple phenotypes is returned.

## Author(s)

Zhonghua Liu <zliu@mail.harvard.edu>

#### References

MPAT: an R package for multivariate phenotype association studies.

```
data(lipids)
lipids = as.data.frame(lipids)
lipids_zscore = as.matrix(lipids[,c("Zscore.HDL","Zscore.LDL","Zscore.TG","Zscore.TC")])
Sigma = cor(lipids_zscore )
PC(Z.vec=lipids_zscore[1,],Sigma,PCorder=1) ## p-value for the first SNP using PC1
```

PCAQ 11

PCAQ	Use PCAQ method to combine Z testing statistics.

# Description

Use PCAQ method to combine Z testing statistics.

# Usage

```
PCAQ(Z.vec, Sigma, SigmaX)
```

# **Arguments**

Z.vec	Z.vec is a vector representing the Z testing statistics for multiple phenotypes.
Sigma	Sigma is the correlation matrix among the Z testing statistics.
SigmaX	The correlation among X which can be estimated by simulation using SigmaX-Estimate.

## Value

p-value	An overall p-value assessing the association between a genetic variant and mul-
	tiple phenotypes is returned.

# Author(s)

Zhonghua Liu <zliu@mail.harvard.edu>

# References

MPAT: an R package for multivariate phenotype association studies.

```
data(lipids)
lipids = as.data.frame(lipids)
lipids_zscore = as.matrix(lipids[,c("Zscore.HDL","Zscore.LDL","Zscore.TG","Zscore.TC")])
Sigma = cor(lipids_zscore )
SigmaX = SigmaXEstimate(Sigma,simNum=1000)
PCAQ(Z.vec=lipids_zscore[1,],Sigma=Sigma,SigmaX=SigmaX) ## p-value for the first SNP
```

PCLC PCLC

ا	PCFisher	Fisher's method to combine principal components based on Z testing statistics

# Description

Z testing statistics for multiple phenotype are orthogonally transformed onto principal component axes and combined using Fisher's method.

#### Usage

```
PCFisher(Z.vec, Sigma)
```

## **Arguments**

Z.vec	Z.vec is a vector representing the Z testing statistics for multiple phenotypes.
Sigma	Sigma is the correlation matrix among the Z testing statistics.

## Value

p-value An overall p-value assessing the association between a genetic variant and mul-

tiple phenotypes is returned.

#### Author(s)

Zhonghua Liu <zliu@mail.harvard.edu>

#### References

MPAT: an R package for multivariate phenotype association studies.

## **Examples**

```
data(lipids)
lipids = as.data.frame(lipids)
lipids_zscore = as.matrix(lipids[,c("Zscore.HDL","Zscore.LDL","Zscore.TG","Zscore.TC")])
Sigma = cor(lipids_zscore )
PCFisher(Z.vec=lipids_zscore[1,],Sigma) ## p-value for the first SNP
```

PCLC

Linear combination of the principal components of the Z testing statistics.

## **Description**

Z testing statistics for multiple phenotype are orthogonally transformed onto principal component axes and combined in a linear fashion.

## Usage

```
PCLC(Z.vec, Sigma)
```

PCMinP 13

#### Arguments

Z.vec is a vector representing the Z testing statistics for multiple phenotypes.

Sigma is the correlation matrix among the Z testing statistics.

Value

p-value An overall p-value assessing the association between a genetic variant and mul-

tiple phenotypes is returned.

## Author(s)

Zhonghua Liu <zliu@mail.harvard.edu>

#### References

MPAT: an R package for multivariate phenotype association studies.

## **Examples**

```
data(lipids)
lipids = as.data.frame(lipids)
lipids_zscore = as.matrix(lipids[,c("Zscore.HDL","Zscore.LDL","Zscore.TG","Zscore.TC")])
Sigma = cor(lipids_zscore)
PCLC(Z.vec=lipids_zscore[1,],Sigma) ## p-value for the first SNP
```

**PCMinP** 

Use the mininum p-value of the principal components of the Z testing statistics as the testing statistic

## **Description**

The p-values using principal components of the Z testing statistics are computed, and the minimum one is taken as the testing statistic.

## Usage

```
PCMinP(Z.vec, Sigma)
```

## **Arguments**

Z.vec is a vector representing the Z testing statistics for multiple phenotypes.

Sigma is the correlation matrix among the Z testing statistics.

## Value

p-value An overall p-value assessing the association between a genetic variant and mul-

tiple phenotypes is returned.

## Author(s)

Zhonghua Liu <zliu@mail.harvard.edu>

14 PCO

#### References

MPAT: an R package for multivariate phenotype association studies.

## **Examples**

```
data(lipids)
lipids = as.data.frame(lipids)
lipids_zscore = as.matrix(lipids[,c("Zscore.HDL","Zscore.LDL","Zscore.TG","Zscore.TC")])
Sigma = cor(lipids_zscore)
PCMinP(Z.vec=lipids_zscore[1,],Sigma) ## p-value for the first SNP
```

PC0

Use PCO method to combine Z testing statistics.

# **Description**

Use PCO method to combine Z testing statistics.

#### Usage

```
PCO(Z.vec, Sigma, SigmaO)
```

#### **Arguments**

Z.vec	Z.vec is a vector representing the Z testing statistics for multiple phenotypes.
Sigma	Sigma is the correlation matrix among the Z testing statistics.
SigmaO	The correlation among X which can be estimated by simulation using Sig-

maOEstimate.

## Value

p-value An overall p-value assessing the association between a genetic variant and mul-

tiple phenotypes is returned.

# Author(s)

Zhonghua Liu <zliu@mail.harvard.edu>

#### References

MPAT: an R package for multivariate phenotype association studies.

```
data(lipids)
lipids = as.data.frame(lipids)
lipids_zscore = as.matrix(lipids[,c("Zscore.HDL","Zscore.LDL","Zscore.TG","Zscore.TC")])
Sigma = cor(lipids_zscore )
Sigma0 = Sigma0Estimate(Sigma,simNum=1000)
PCO(Z.vec=lipids_zscore[1,],Sigma=Sigma,Sigma0=Sigma0) ## p-value for the first SNP
```

SigmaOEstimate 15

SigmaOEstimate	To estimate the correlation matrix of among X used for PCO
----------------	------------------------------------------------------------

## **Description**

Compute SigmaX which is required for PCO function.

#### Usage

```
SigmaOEstimate(Sigma, simNum)
```

## **Arguments**

Sigma Sigma is the correlation matrix among the Z testing statistics.

simNum The number of simulations to be performed to estimate SigmaX.

#### Value

Sigma0 A correlation matrix among X.

#### Author(s)

Zhonghua Liu <zliu@mail.harvard.edu>

## References

MPAT: an R package for multivariate phenotype association studies.

# **Examples**

```
data(lipids)
lipids = as.data.frame(lipids)
lipids_zscore = as.matrix(lipids[,c("Zscore.HDL","Zscore.LDL","Zscore.TG","Zscore.TC")])
Sigma = cor(lipids_zscore )
SigmaOEstimate(Sigma,simNum=1000)
```

 ${\tt SigmaXEstimate}$ 

To estimate the correlation matrix of among X used for PCAQ

# Description

Compute SigmaX which is required for PCAQ function.

#### Usage

```
SigmaXEstimate(Sigma, simNum)
```

## **Arguments**

Sigma is the correlation matrix among the Z testing statistics.

simNum The number of simulations to be performed to estimate SigmaX.

16 SUM

#### Value

SigmaX A correlation matrix among X.

#### Author(s)

Zhonghua Liu <zliu@mail.harvard.edu>

#### References

MPAT: an R package for multivariate phenotype association studies.

# **Examples**

```
data(lipids)
lipids = as.data.frame(lipids)
lipids_zscore = as.matrix(lipids[,c("Zscore.HDL","Zscore.LDL","Zscore.TG","Zscore.TC")])
Sigma = cor(lipids_zscore )
SigmaXEstimate(Sigma,simNum=1000)
```

SUM

Use SUM method to combine Z testing statistics

## **Description**

The Z testing statistics for multiple phenotypes are combined using SUM method with correlation structures explicitly taken into account.

# Usage

```
SUM(Z.vec, Sigma)
```

# Arguments

Z.vec is a vector representing the Z testing statistics for multiple phenotypes.

Sigma is the correlation matrix among the Z testing statistics.

## Value

p-value An overall p-value assessing the association between a genetic variant and mul-

tiple phenotypes is returned.

#### Author(s)

Zhonghua Liu <zliu@mail.harvard.edu>

#### References

MPAT: an R package for multivariate phenotype association studies.

*VC* 17

#### **Examples**

```
data(lipids)
lipids = as.data.frame(lipids)
lipids_zscore = as.matrix(lipids[,c("Zscore.HDL","Zscore.LDL","Zscore.TG","Zscore.TC")])
Sigma = cor(lipids_zscore )
SUM(Z.vec=lipids_zscore[1,],Sigma) ## p-value for the first SNP
```

۷C

Use variance component test (VC) to combine Z testing statistics

# Description

Use variance component test (VC) to combine Z testing statistics of multiple phenotypes.

## Usage

```
VC(Z.vec, Sigma, method)
```

# Arguments

Sigma is the correlation matrix among the Z testing statistics.

method The method to compute the p-value which takes three values: davies, liu and

liumod.

#### Value

p-value An overall p-value assessing the association between a genetic variant and mul-

tiple phenotypes is returned.

#### Author(s)

Zhonghua Liu <zliu@mail.harvard.edu>

#### References

MPAT: an R package for multivariate phenotype association studies.

```
data(lipids)
lipids = as.data.frame(lipids)
lipids_zscore = as.matrix(lipids[,c("Zscore.HDL","Zscore.LDL","Zscore.TG","Zscore.TC")])
Sigma = cor(lipids_zscore )
VC(Z.vec=lipids_zscore[1,],Sigma) ## p-value for the first SNP
```

18 WI

Wald

Traditional Wald type combination of Z testing statistics

## **Description**

The Z testing statistics for multiple phenotypes are combined using Wald type method.

## Usage

```
Wald(Z.vec, Sigma)
```

## **Arguments**

Z.vec is a vector representing the Z testing statistics for multiple phenotypes.

Sigma is the correlation matrix among the Z testing statistics.

#### Value

p-value An overall p-value assessing the association between a genetic variant and mul-

tiple phenotypes is returned.

## Author(s)

Zhonghua Liu <zliu@mail.harvard.edu>

## References

MPAT: an R package for multivariate phenotype association studies.

# **Examples**

```
data(lipids)
lipids = as.data.frame(lipids)
lipids_zscore = as.matrix(lipids[,c("Zscore.HDL","Zscore.LDL","Zscore.TG","Zscore.TC")])
Sigma = cor(lipids_zscore )
Wald(Z.vec=lipids_zscore[1,],Sigma) ## p-value for the first SNP
```

WI

Use WI method to combine Z testing statistics.

# **Description**

Use WI method to combine Z testing statistics.

# Usage

```
WI(Z.vec, Sigma, method)
```

WI 19

## **Arguments**

Z.vec is a vector representing the Z testing statistics for multiple phenotypes.

Sigma is the correlation matrix among the Z testing statistics.

method The method to compute the p-value which takes three values: davies, liu and

liumod.

## Value

p-value An overall p-value assessing the association between a genetic variant and mul-

tiple phenotypes is returned.

#### Author(s)

Zhonghua Liu <zliu@mail.harvard.edu>

#### References

MPAT: an R package for multivariate phenotype association studies.

```
data(lipids)
lipids = as.data.frame(lipids)
lipids_zscore = as.matrix(lipids[,c("Zscore.HDL","Zscore.LDL","Zscore.TG","Zscore.TC")])
Sigma = cor(lipids_zscore)
WI(Z.vec=lipids_zscore[1,],Sigma,method="liu") ## p-value for the first SNP
```

# **Index**

```
* \\ Topic \ \boldsymbol{datasets}
     lipids, 3
DSUM, 2
lipids, 3
MinP, 4
mixAda, 5
mixFisher, 6
mixSD, 7
mixTippett, 8
mixVar, 9
{\tt MPAT}\ ({\tt MPAT-package}),\, {\tt 2}
MPAT-package, 2
PC, 10
PCAQ, 11
PCFisher, 12
PCLC, 12
PCMinP, 13
PCO, 14
PCSS (Wald), 18
SigmaOEstimate, 15
SigmaXEstimate, 15
SUM, 16
VC, 17
Wald, 18
WI, 18
```