

# **CSE216**

## **Foundations of Computer Science**

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Many slides taken from Prof. YoungMin Kwon. Thanks!

# Plan

## (no change; reminder)

- ~~11.14 Tu~~: Ocaml -
- 11.16 Ocaml ungraded homework; Ocaml in REC
- 11.21 Tu Review Midterm 2 -
- 11.23 **Midterm 2** no homework; C in REC
- 11.28 Tu C C
- 11.30 C C; ungraded homework; Final Review in REC
- 12.05 Tu Final Review -
- 12.07 Final Review - Final Review
- 12.11 Tu Final -

# Midterm2

- Covering lambda calculus and Ocaml
- Same format as midterm1
  - Unlimited physical notes allowed
  - No e-device during the exam
  - Submission to BrightSpace + physical copy

- Today: More on Higher-order functions: Procedure
- Ungraded homework to be announced today
- Next Tuesday will be revision + previous homework

# Procedural Abstraction

# Computing pi with Nilakantha series



$$\pi = 3 + \frac{4}{2 \times 3 \times 4} - \frac{4}{4 \times 5 \times 6} + \frac{4}{6 \times 7 \times 8} - \frac{4}{8 \times 9 \times 10} + \dots$$

# Pseudo-code

$$\pi = 3 + \frac{4}{2 \times 3 \times 4} - \frac{4}{4 \times 5 \times 6} + \frac{4}{6 \times 7 \times 8} - \frac{4}{8 \times 9 \times 10} + \dots$$

- guess = 3
- Loop
  - If guess is good return guess
  - else guess = guess + next\_item
- end loop

# pseudocode -> code v0.1

$$\pi = 3 + \frac{4}{2 \times 3 \times 4} - \frac{4}{4 \times 5 \times 6} + \frac{4}{6 \times 7 \times 8} - \frac{4}{8 \times 9 \times 10} + \dots$$

- guess = 3
- Loop
  - If guess is good return guess
  - else guess = guess + next\_item
- end loop
- let pi\_iter guess =
  - if good\_enough guess then guess
  - else pi\_iter guess+next\_item



# code v0.1 -> v0.2

$$\pi = 3 + \frac{4}{2 \times 3 \times 4} - \frac{4}{4 \times 5 \times 6} + \frac{4}{6 \times 7 \times 8} - \frac{4}{8 \times 9 \times 10} + \dots$$

- let pi\_iter guess =
  - if good\_enough guess then guess
  - else pi\_iter guess+next\_item
- let pi\_iter guess old\_guess tol=
  - if abs(guess-old guess)<tol then guess
  - else pi\_iter guess+next\_item guess tol

# code v0.2 -> v0.3

$$\pi = 3 + \frac{4}{2 \times 3 \times 4} - \frac{4}{4 \times 5 \times 6} + \frac{4}{6 \times 7 \times 8} - \frac{4}{8 \times 9 \times 10} + \dots$$

- let pi\_iter guess old\_guess tol=
  - if abs(guess-old guess)<tol then guess
  - else pi\_iter guess+next\_item guess tol
- let pi\_iter guess old\_guess x sign tol=
  - if abs(guess-old guess)<tol then guess
  - else pi\_iter guess+ sign\*4/(x(x+1)(x+2)) guess tol

# code v0.3 -> v0.4

$$\pi = 3 + \frac{4}{2 \times 3 \times 4} - \frac{4}{4 \times 5 \times 6} + \frac{4}{6 \times 7 \times 8} - \frac{4}{8 \times 9 \times 10} + \dots$$

- let pi\_iter guess old\_guess x sign tol=

```
let good_enough guess old_guess tol =  
  (abs (guess -. old_guess)) <= tol;;
```

- if abs(guess-old guess)<tol then guess

```
let term x sign =  
  sign *. 4. /. (x *. (x +. 1.) *. (x +. 2.))
```

- else pi\_iter guess+ sign\*4/(x(x+1)(x+2)) guess tol

```
let rec pi_iter guess old_guess x sign tol =
```

# code v0.3 -> v0.4 (cont.)

$$\pi = 3 + \frac{4}{2 \times 3 \times 4} - \frac{4}{4 \times 5 \times 6} + \frac{4}{6 \times 7 \times 8} - \frac{4}{8 \times 9 \times 10} + \dots$$

- let pi\_iter guess old\_guess x sign tol =

- if abs(guess-old\_guess)<tol then guess

- else pi\_iter guess+ sign\*4/(x(x+1)(x+2)) guess tol

```
let good_enough guess old_guess tol =  
  (abs (guess -. old_guess)) <= tol;;
```

```
let term x sign =  
  sign *. 4. /. (x *. (x +. 1.) *. (x +. 2.))
```

```
let rec pi_iter guess old_guess x sign tol =  
  if good_enough guess old_guess tol  
  then guess  
  else pi_iter (guess +. (term x sign))  
               guess  
               (x +. 2.)  
               (-. sign)  
               tol
```

# Running the code

```
let rec pi_iter guess old_guess x sign tol =  
  if good_enough guess old_guess tol  
  then guess  
  else pi_iter (guess +. (term x sign))  
               guess  
               (x +. 2.)  
               (-. sign)  
               tol
```

```
let pi tol =  
  pi_iter 3. 0. 2. 1. tol
```

```
let _ = pi 1e-10
```

```
# #use "pi_iter.ml";;
```

```
val good_enough : float -> float -> float -> bool = <fun>  
val term : float -> float -> float = <fun>  
val pi_iter : float -> float -> float -> float -> float -> float..  
val pi : float -> float = <fun>  
- : float = 3.1415926535398846
```

$$\pi = 3 + \frac{4}{2 \times 3 \times 4} - \frac{4}{4 \times 5 \times 6} + \frac{4}{6 \times 7 \times 8} - \frac{4}{8 \times 9 \times 10} + \dots$$

# Expression let...in...

*let* <variable> = <expr1> *in* <expr2>

- *let* binding is equivalent to

( *fun* <variable> -> <expr2> ) <expr1>

```
let foo () =  
  let x = 1 in  
  let y = x + 1 in  
  let z = y + 1 in  
  z + 3
```

# A nicer example

```
let calculate_discounted_price price customer_type =  
  let standard_discount = 0.10 in  
  let premium_discount = 0.20 in  
  let gold_discount = 0.30 in  
  let discount =  
    match customer_type with  
    | "standard" -> standard_discount  
    | "premium" -> premium_discount  
    | "gold" -> gold_discount  
    | _ -> 0.0  
  in  
  let final_price = price -. (price *. discount) in  
  (* Your code to round the final_price to two decimal places *)  
  final_price  
;;
```

**Lab**



- Exercise: Calculate the Area of a Circle
- Define a procedure to calculate the area of a circle. The procedure should take the radius of the circle as an argument and return the area. Use the **let ... in** construct to define a local variable for pi within the procedure.

Consider these functions **double** and **square** on integers:

```
let double x = 2 * x
let square x = x * x
```

```
val double : int -> int = <fun>
```

```
val square : int -> int = <fun>
```

Let's use these functions to write other functions that quadruple and raise a number to the fourth power:

- let quad = (\*todo\*)
- let fourth = (\*todo\*)

There is an obvious similarity between these two functions: what they do is apply a given function twice to a value. By passing in the function to another function `twice` as an argument, we can abstract this functionality:

```
let twice f x = f (f x)
```

```
val twice : ('a -> 'a) -> 'a -> 'a = <fun>
```

The function `twice` is higher-order: its input `f` is a function. And—recalling that all OCaml functions really take only a single argument—its output is technically `fun x -> f (f x)`, so `twice` returns a function hence is also higher-order in that way.

Using `twice`, we can implement `quad` and `fourth` in a uniform way:

- `let quad = (*todo*)`
- `let fourth = (*todo*)`

# Exercise #9

- Pack consecutive duplicates of list elements into sublists.

```
# pack ["a"; "a"; "a"; "a"; "b"; "c"; "c"; "a"; "a"; "d";  
"d"; "e"; "e"; "e"; "e"];;  
- : string list list =  
[["a"; "a"; "a"; "a"]; ["b"]; ["c"; "c"]; ["a"; "a"];  
["d"; "d"];  
["e"; "e"; "e"; "e"]]
```