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#### Guideline

#### **Homework for Week 01**

Please submit your solutions as a single PDF on Brightspace.

Multiple submissions are allowed before the due time; the last submission will be graded.

## **Grading Criteria**

- Grading will be *highly strict*, with minimal tolerance for mistakes or misconduct.
- Factual grading errors will be corrected, but partial grading decisions will not be negotiable.
- If the solution appears to be plagiarized or Al-generated, the issue will be reported to the instructor.
- Most questions here involve constructing truth tables and drawing a conclusion. If the conclusion is
  incorrect, 75% of the total points will be deducted. If the truth table is incorrect, 1 point to 75% of the
  total points may be deducted, depending on the severity of the errors. The total deduction cannot
  exceed the full score.

## Exercise 0 (5 points)

Indicate whether each statement regarding our class policies is True (T) or False (F).

- 1. Late homework is totally acceptable if the student is busy.
- 2. If a student strolls into class late after the attendance checks have been done, they will still get full attendance credit.
- 3. Actively asking questions during class, or providing constructive feedbacks, can positively impact the student's final grade.
- 4. Copying answers directly from AI tools is acceptable because AI is cool.
- 5. A student's class absence can be excused if they submit a document showing they simply visited a doctor.

# Exercise 1 (20 points)

Check if the two statements below are equivalent using the truth table technique. Your conclusion should be either "equivalent" or "not equivalent."

- $(p \rightarrow q) \land (q \rightarrow r) \land (r \rightarrow p)$
- p∧q∧r

## Exercise 2 (20 points)

Consider the six statement forms (a-f):

- (a) p -> q
- (b) q -> p
- (c) ~p ∨ q
- (d) ~q ∨ p
- (e) ~q -> ~p
- (f) ~p -> ~q
- 1. Find all statement forms that are equivalent to (a), except (a) itself.
- 2. Find all statement forms that are equivalent to (b), except (b) itself.

For this exercise, constructing truth tables is needed.

# Exercise 3 (20 points)

Consider the proposition  $\sim$ P  $\land$  (Q -> P). What can you conclude about P and Q if you know the statement is true? For this exercise, an explanation is not needed. Just show your results using a truth table.

### Exercise 4 (15 points)

A tautology and a contradiction are terms used in logic to describe specific types of propositions.

• A *tautology* is a proposition that is always true, regardless of the truth values of its constituent parts. In other words, a proposition is a tautology if it is true in every row of a truth table. For example, p ∨ ~p. An example in plain language: "It will either rain today or it won't."

A contradiction is a proposition that is always false, regardless of the truth values of its constituent parts.
 In other words, a proposition is a contradiction if it is false in every row of a truth table. For example, p ∧
 ~p. An example in plain language: "I will finish the homework today and I will not."

For each statement form below, determine if it is a tautology, contradiction, or neither. For this exercise, an explanation is not needed. Your answer should be "tautology," "contradiction," or "neither."

- 1.  $(\sim p \lor q) \lor (p \land \sim q)$
- 2.  $(p \land \sim q) \land (\sim p \lor q)$
- 3.  $(p \land q) \lor (\sim p \lor (p \land \sim q))$

#### Exercise 5 (20 points)

Verifying Simple Code with Hoare Logic

Hoare Logic is a formal system for reasoning about the correctness of computer programs. Tony Hoare introduced it in 1969, which contributed to his Turing Award. Hoare Logic helps in verifying that a program does what it is supposed to do. Interested students should read this:

https://amturing.acm.org/award\_winners/hoare\_4622167.cfm

Hoare Logic revolves around the concept of a Hoare Triple, which has the following format:

```
{P} Code {Q}
```

- P is the precondition. It's a proposition about the variables in your program that is true before the code runs.
- Q is the postcondition. It's a proposition that you expect to be true after the code runs.
- Code is the program or part of the program that you're analyzing.

**Examples of correct Hoare Triples:** 

```
{x = 1} y := x + 1 {y = 2 ∧ x = 1}
{x = 1} y := x + 1 {y = 2}
{x = 0} while (x<=10) {x = x + 1} {x = 11}</li>
```

Note: In the above examples, "y = 2" is weaker than " $y = 2 \land x = 1$ ," but it remains correct after y := x + 1 is executed with the precondition "x = 1."

**Examples of incorrect Hoare Triples:** 

```
• \{x = 1\} y := x + 1 \{y - x = 2\}
• \{x > 0\} while \{x < 10\} \{x = x + 1\} \{x = 11\}
```

Note: The second example is incorrect because it claims that if "x > 0," then "x" will equal 11 at the end of the loop. This is flawed for two reasons: (1) If "x" starts as 0.5, then at the end of the loop, "x" will be 10.5, not 11. (2) If "x" starts as a value greater than 10, such as 42, then the loop will terminate without changing the value of "x" at all.

Questions: Determine whether the following Hoare Triple is correct or not. For this exercise, an explanation is not needed. Your answers should be "correct" or "not correct."

1.  $\{x = 3 \land y = 2\}$  Code  $\{x = 2 \land y = 3\}$ , where "Code" refers to the following:

```
x := x + y
y := x - y
x := x - y
```

2.  $\{x > 0\}$  while  $\{x < 10\}$   $\{x = x + 1\}$   $\{x > 10\}$ . Note this one looks similar to, but different from, a piece of code we discussed in class.