CSE216
Foundations of Computer Science

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Many slides taken from Prof. YoungMin Kwon. Thanks!

A missing explanation

‘a type

- # max ;;

- - : 'a -> 'a -> 'a = <fun>

if c then e1 else e2

```
# if true then "hello" else 5;;
Error: This expression has type int but an expression was expected of type
         string
# if true then "hello";;
Error: This expression has type string but an expression was expected of type
         unit
       because it is in the result of a conditional with no else branch
# 
```

Ocaml Functions

Function Definitions
(also known as Procedural Abstraction)

```
let <name> <formal parameters> = <body>
```

```
# let square x = x * x;;
val square : int -> int = <fun>
```

name

formal parameter

body

Function Application

```
# square 3;;
-  : int = 9

# square (1+2);;
-  : int = 9

# square (square 3);;
-  : int = 81

# let sum_of_squares x y = square x + square y;;
val sum_of_squares : int -> int -> int = <fun>

# sum_of_squares 3 4;;
- : int = 25
```

square is used as a building block of another procedure

Anonymous functions

fun <formal parameters> -> <body>

```
# fun x -> x * x;;
- : int -> int = <fun>
```

anonymous function

formal parameter

body

```
# let square = fun x -> x * x;;
val square : int -> int = <fun>
```

Recursive function

let ***rec*** *<name> = fun <formal parameters> ->*
<body>

```
# let rec fact = fun x -> if x = 0 then 1 else x * fact (x
- 1);;
val fact : int -> int = <fun>
```

Multi-parameter functions

```
let add x y = x + y
≡ let add = fun x -> fun y -> x + y
≡ let add = fun x -> (fun y -> x + y)

add 2 3
≡ (add 2) 3
```

Tuple parameter function

```
# let add (a, b) = a + b;;
val add : int * int -> int = <fun>
# add (1, 2);;
- : int = 3
```

```
# let add' a b = a + b;;
val add' : int -> int -> int = <fun>
# add' 1 2;;
- : int = 3

# let inc = add' 1;;
val inc : int -> int = <fun>
# inc 2;;
- : int = 3
```

The |> operator

The |> operator represents reverse function application.

You can put the function *after* the value you want to apply it to. This allows building up something that looks like a Unix pipeline:

```
# let ( |> ) x f = f x;;
val ( |> ) : 'a -> ('a -> 'b) -> 'b = <fun>
# 0.0 |> sin |> exp;;
- : float = 1.
```

' a is a *type variable*, and stands for any given type

Lab exercise 1

- Define a function **square** that squares an integer.

- Find different ways to define the function

- Use the **|>** operator to square the number 123456789.

Lab exercise 2

- Write a function hypotenuse of type float->float->float, that takes the lengths of the two shorter sides of a right triangle and returns the length of the hypotenuse.
- Write the function in 3+ different ways
- Calculate the hypotenuse for sides of lengths 3.1 and 4.2
-

Boolean expression

```
# true;;
- : bool = true
# false;;
- : bool = false
```

Structure Comparison

```
# (=);;
- : 'a -> 'a -> bool = <fun>
# (<>);;
- : 'a -> 'a -> bool = <fun>
# (>);;
- : 'a -> 'a -> bool = <fun>

# 2 > 1;;
- : bool = true

# 2. > 1.;;
- : bool = true

# 2 > 1.;;
Characters 4-6:
  2 > 1.;;
      ^^
Error: This expression has
Type float but an expression
was expected of type int
```

```
# int_of_float 1. > 2;;
- : bool = false

# float_of_int 1 > 2.;;
- : bool = false

# float 1 > 2.;;
- : bool = false

# "abc" = "abc";;
- : bool = true

# "abc" <> "abc";;
- : bool = false

# "abc" < "def";;
- : bool = true
```

Structure/address Comparison

```
(* =,  <>: comp. structures,
   ==, !=: comp. addresses *)
# (==);;
- : 'a -> 'a -> bool = <fun>
# (!=);;
- : 'a -> 'a -> bool = <fun>
```

```
# "hello" = "hello";;
- : bool = true

# "hello" <> "hello";;
- : bool = false

# "hello" == "hello";;
- : bool = false

# "hello" != "hello";;
- : bool = true
```

```
# let v = "hello";;
val v : string = "hello"
# v = v;;
- : bool = true
# v <> v;;
- : bool = false
# v == v;;
- : bool = true
# v != v;;
- : bool = false

# let u = v;;
val u : string = "hello"
# u == v;;
- : bool = true
# u != v;;
- : bool = false
```

Logical connectives: &&, ||, not

```
# (&&);;
-  : bool -> bool -> bool = <fun>

# let inside lb ub x = lb <= x && x <= ub;;
val inside : 'a -> 'a -> 'a -> bool = <fun>

# inside 0 10 5;;
-  : bool = true

# let outside lb ub x = not (inside lb ub x);;
val outside : 'a -> 'a -> 'a -> bool = <fun>

# outside 0 10 5;;
- : bool = false
```

Conditional Expression

```
if <predicate> then <consequent>
               else <alternative>
```

```
# let abs x = if x >= 0 then x else - x;;
val abs : int -> int = <fun>

# abs (-3);;
- : int = 3
```

Conditional Expression (2)

- Example: factorial

```
# let rec factorial x =
    if x = 0
    then 1
    else x * factorial (x - 1);;
val factorial : int -> int = <fun>

# factorial 4;;
- : int = 24
```

- To define a *recursive function*, use let rec

Exercises

Exercises 1

- Write down the types of the defined functions in OCaml:
  - a) let double x = 2*x;;
  - b) let square x = x*x;;
  - c) let twice f x = f (f x);;
  - d) let quad = twice double;;
  - e) let fourth = twice square;;