CSE216 Foundations of Computer Science

State University of New York, Korea

Exercise 1. (points = 25)

Write a function drop: int -> 'a list -> 'a list such that drop n lst returns all but the first n elements of lst.

If lst has fewer than n elements, return the empty list. Here, n can be any integer including negative number.

Problem 2. Ocaml Types (25)

Give the type of the following OCaml expressions:

```
(1) ["Annyeonghaseyo"]
```

(5) let
$$f \times y z = x+y+z$$
 in $f 1$

Give the type of the function defined below:

(6) let
$$f x y = x * . 2.7$$

(7) let
$$f(x,y) = (y,x)$$

$$(8)^{**}$$
 let f x y = x :: y

(9) let
$$f(x, y) = [x; y]$$

(10) let
$$f \times y z = if z$$
 then x else y

Problem 3 (30)

- 1. Write an Ocaml function to calculate the nth Fibonacci number. Note the Fibonacci numbers look like this starting from the first one: 1, 1, 2, 3, 5, 8, 13, 21, 34, 55, 89, 144, 233, 377, 610, 987.
- 2. Write an Ocaml function that takes a list of integers and returns a list of the squares of those integers.

3. Write an Ocaml function compress that eliminates consecutive duplicates of list elements.

```
# compress ["a"; "a"; "a"; "b"; "c"; "c"; "a"; "a"; "d"; "e";
"e"; "e"];;
- : string list = ["a"; "b"; "c"; "a"; "d"; "e"]
```

Problem 4 (20)

Natural numbers are inductively defined as the following grammar

```
n -> Z | S n
```

where Z can be understood as zero, S can be understood the operator that increments by one.

- 1. Create a type nat following this definition of natural number.
- 2. Define a function

```
add : nat-> nat->nat
```

that adds two natural numbers.

3. Define a function

```
mul : nat-> nat->nat
```

that multiplies two natural numbers.