

CSE216

Foundations of Computer Science

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Some slides taken from Cornell's CS3110. Thanks!
https://www.cs.cornell.edu/courses/cs3110/2014fa/lecture_notes.php

Data types

Data type

- Sum Type
- Record type
- Tuple type

Sum type

```
type day = Mon | Tue | Wed | Thu | Fri |  
Sat | Sun
```

- Superficially similar to an enum in Java or C
- Created a one-of type named day
- Created seven constructors from Mon to Sun
- That's effectively how Booleans are defined in OCaml:

```
type bool = false | true
```

Example

```
# type suit = Heart | Diamond | Club | Spade;;  
type suit = Heart | Diamond | Club | Spade
```

```
# Club ;;  
- : suit = Club
```

Example: day_to_int

```
let day_to_int (d : day) =  
  if d=Mon then 1  
  else if d=Tue then 2  
  else if d=Wed then 3  
  else if d=Thu then 4  
  else if d=Fri then 5  
  else if d=Sat then 6  
  else (* d=Sun *) 7
```

Note: Ocaml compiler/interpreter does not see new lines

An alternative (and better) way: Pattern matching

```
let day_to_int (d : day) = match d with  
  | Mon -> 1 (* you can put an “|” in front)  
  | Tue -> 2  
  | Wed -> 3  
  | Thu -> 4  
  | Fri -> 5  
  | Sat -> 6  
  | Sun -> 7
```

Exercise

- Define a sum type shape with constructors for Circle, Rectangle, and Triangle, each carrying appropriate dimensions. Then write a function area to compute the area of a shape

A triangle's shape is uniquely determined by the lengths of the sides, so its metrical properties, including area, can be described in terms of those lengths. By [Heron's formula](#),

$$T = \sqrt{s(s-a)(s-b)(s-c)}$$

where $s = \frac{1}{2}(a+b+c)$ is the [semiperimeter](#), or half of the triangle's perimeter.

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type time = {hour: int; min: int; ampm: string}
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 - order of *fields* doesn't matter; could write

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{hour=10; min=10; ampm="am"}
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{min=10; ampm="am"; hour=10}
```

- To *access* fields of record variable **t**:

```
t.min
```

Exercise

- Which kind of data type, sum type or record type would be better represented with record types rather than sum types?
 - Coins, which can be pennies, nickels, dimes, or quarters
 - Students, who have names and NetIDs
 - A dessert, which has a sauce, a creamy component, and a crunchy component
 - MBTI types, ISTJ, ESTJ etc

Exercise

- Define a record type student with fields name (string), id (int), and grade (float). Create a function pass that checks if a student's grade is at least 60.0.

Pair type

- `type t = int * string`
- `type point = float * float`

Pairs

A **pair** of data: two pieces of data glued together
e.g.,

- $(1, 2)$
- $(\text{true}, \text{"Hello"})$
- $(\text{"cs"}, 3110)$
- Syntax: $(e1, e2)$
- Evaluation:
 - If $e1 \rightarrow v1$ and $e2 \rightarrow v2$
 - Then $(e1, e2) \rightarrow (v1, v2)$
 - A pair of values is itself a value
- Type-checking:
 - If $e1 : t1$ and $e2 : t2$,
 - then $(e1, e2) : t1 * t2$

Accessing Pairs

- **Syntax:** `fst e` and `snd e`
 - *Projection functions*
- **Evaluation:**
 - If `e` \rightarrow (v1, v2)
 - then `fst e` \rightarrow v1
 - and `snd e` \rightarrow v2
- **Type-checking:**
 - If `e` : `ta*tb`,
 - then `fst e` has type `ta`
 - and `snd e` has type `tb`

Tuples

- (e_1, e_2, \dots, e_n)
- $t_1 * t_2 * \dots * t_n$
- $\text{fst } e, \text{ snd } e, ???$

Exercise

- Write a function `distance` that takes a tuple `(x1, y1)` and `(x2, y2)` representing two points and computes the Euclidean distance between them.
- You're given a transformation as a tuple `(shift, scale)` where `shift` is `(dx, dy, dz)` (floats) and `scale` is `(sx, sy, sz)` (floats), and a point `(x, y, z)` (floats). Write a function `transform` that applies the transformation: first scale the point by `(sx, sy, sz)`, then shift by `(dx, dy, dz)`.

Pattern matching tuples

```
let sum_triple (triple:int*int*int) =  
  let (x, y, z) = triple  
  in x + y + z
```

- `(x, y, z)` is a *pattern*
 - because it's on the LHS of equals in `let`

Exercise: Rewrite `sum_triple` using `match ... with ...` syntax

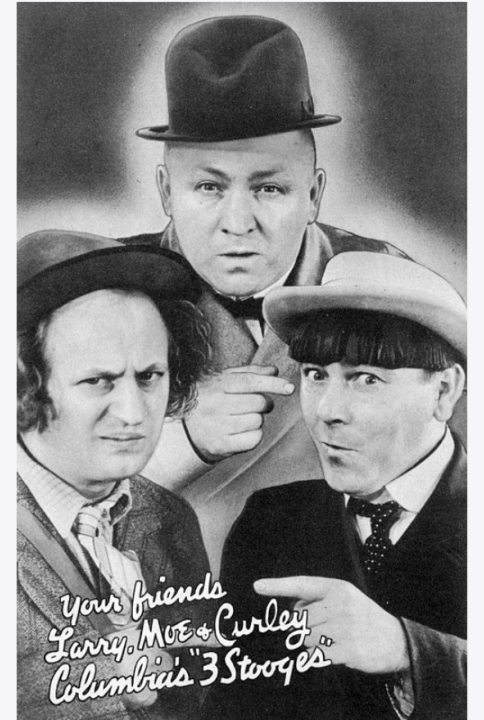
Pattern matching records

The same syntax works for records:

```
type stooges = {larry:int; moe:int; curly:int}

let sum_stooges (s:stooges) =
  let {larry=x; moe=y; curly=z} = s
  in x + y + z
```

The Three Stooges



The Three Stooges in 1937:
(clockwise from left) [Larry Fine](#), [Curly Howard](#),
and [Moe Howard](#)

More Exercises

Exercise 1

1 Define an algebraic datatype **grade** that represents a grade in a course. The datatype should include constructors for an A, B, C, D, and F.

Exercise 2

2 Then, write a function `to_num` that takes a grade as input and returns a numerical equivalent, where A is 4.0, B is 3.0, C is 2.0, D is 1.0, and F is 0.0. Your function should have the following type.

```
val to_num: grade -> float
```


Exercise 3

Define a type, `time`, which holds the hour, minute, and second as separate values.

Exercise 4

Write a function `seconds_since_midnight2` with the following type:

```
val seconds_since_midnight2 : time -> int
```