

第一题：详见代码和截图

The screenshot displays a ROS environment with three terminal windows and a 3D visualization window.

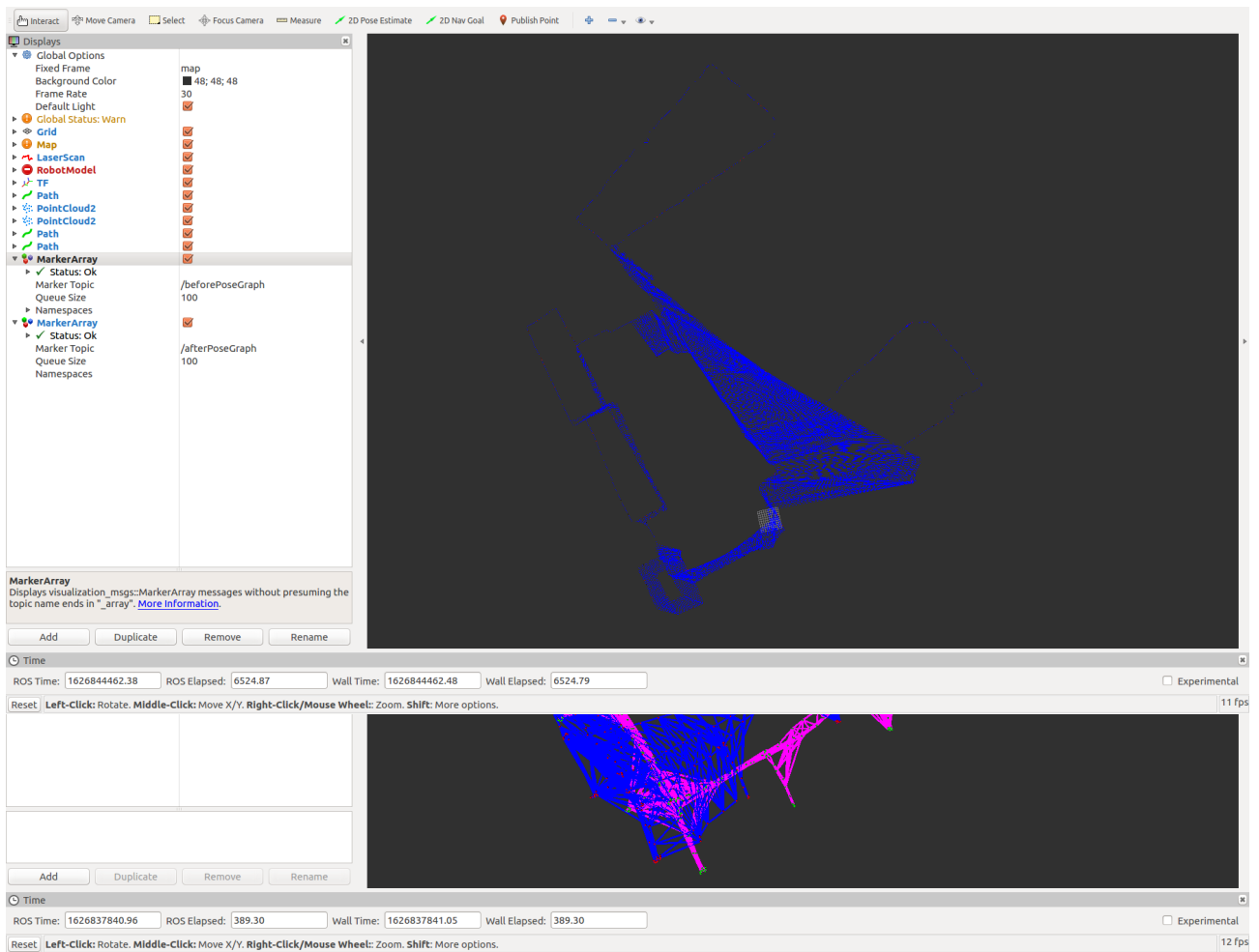
Terminal 1 (top left): Shows the execution of `roscore` and `roslaunch` commands. It logs the start of the `rosout` process and the `roslaunch` server. The output includes the ROS version (1.12.17) and the launch file path.

Terminal 2 (top right): Shows the execution of `roslaunch` for the `ls_slam` package. It logs the start of the `ls_slam` process and the `roslaunch` server. The output includes the ROS version (1.12.17) and the launch file path.

Terminal 3 (bottom left): Shows the execution of `rviz`. It logs the start of the `rviz` process and the `roslaunch` server. The output includes the ROS version (1.12.17) and the launch file path.

3D Visualization Window: Displays a 3D scene with a robot model (red sphere) and a point cloud (blue lines). The robot model is positioned at the origin (0,0,0). The point cloud is a triangular shape. The window includes a toolbar with various tools like Move Camera, Select, Focus Camera, Measure, 2D Pose Estimate, 2D Nav Goal, and Publish Point. The left sidebar shows the Displays panel with a list of displayed elements: Global Options, Fixed Frame, Background Color, Frame Rate, Default Light, Global Status: Warn, Grid, Map, LaserScan, RobotModel, TF, Path, PointCloud2, MarkerArray, and MarkerTopic. The right sidebar shows the Properties panel for the selected element, displaying parameters like map, fixed frame, background color, frame rate, default light, global status, grid, map, laser scan, robot model, tf, path, point cloud 2, marker array, marker topic, queue size, namespaces, and status.

Time Panel: Located at the bottom, it shows the ROS Time (1626835789.05), ROS Elapsed (3699.35), Wall Time (1626835789.08), and Wall Elapsed (3699.31). It also includes a checkbox for Experimental and a Reset button.



第二题:

第一题中求解 $H\Delta x = -b$ 的过程最为耗时，可以通过 g2o 等优化库进行优化，简化计算过程。

第三题:

一阶梯度法，将目标函数在 x 附近进行泰勒展开:

$$\|f(x + \Delta x)\|_2^2 \approx \|f(x)\|_2^2 + J(x)\Delta x + \frac{1}{2}\Delta x^T H \Delta x$$

如果保留一阶梯度，则:

$$\Delta x^* = -J^T(x)$$

二阶梯度法，如果保留二阶梯度，则: $H\Delta x = -J^T$

LM 方法，求解方程:

$$(H + \lambda I)\Delta x = g$$

第四题: 采用 g2o 和 ceres 进行优化，对比发现 ceres 求解时间最快，误差最小

g2o:

```
1: rosrun ls_slam ls_slam
[100%] Built target ls_slam
A touchair-2080T LSSLAMProject --source devel/setup.zsh
A touchair-2080T LSSLAMProject --rosrun ls_slam ls_slam
Inferior: 2.88924e46
Iterations: 0 ch12= 51574.948019 time= 0.279375 cunTime= 0.279375 edges= 3070 schur= 0
Lambda= 0.150732 levenbergiter= 1
ch12= 39827.007231 time= 0.2563 cunTime= 0.535676 edges= 3070 schur= 0
Iterations: 1 ch12= 180488 levenbergiter= 1
ch12= 37926.215906 time= 0.423233 cunTime= 0.958999 edges= 3070 schur= 0
Lambda= 0.535935 levenbergiter= 3
Iterations: 2 ch12= 36132.808805 time= 0.507572 cunTime= 1.46657 edges= 3070 schur= 0
Lambda= 22.866547 levenbergiter= 4
Iterations: 4 ch12= 36132.808805 time= 0.993813 cunTime= 2.46038 edges= 3070 schur= 0
Lambda= 823854168383115392.000000 levenbergiter= 10
finish
FinalError:36132.8
CXX
A touchair-2080T LSSLAMProject --catkin make
Source space: /home/touchair/Downloads/HM6/LSSLAMProject
Build space: /home/touchair/Downloads/HM6/LSSLAMProject/build
Devel space: /home/touchair/Downloads/HM6/LSSLAMProject/devel
Install space: /home/touchair/Downloads/HM6/LSSLAMProject/install
##### Running command: "make cmake_check_build_system" in "/home/touchair/Downloads/HM6/LSSLAMProject/build"
#####
##### Running command: "make -j8 -l8" in "/home/touchair/Downloads/HM6/LSSLAMProject/build"
#####
Scanning dependencies of target ls_slam
25% Building CXX object ls_slam/CMakeFiles/ls_slam.dir/src/main.cpp.o
[ 50%] Linking CXX executable /home/touchair/Downloads/HM6/LSSLAMProject/devel/lib/ls_slam/ls_slam
[100%] Built target ls_slam
A touchair-2080T LSSLAMProject --source devel/setup.zsh
A touchair-2080T LSSLAMProject --rosrun ls_slam ls_slam
Inferior: 251853
Iterations: 0 ch12= 58959.160609 time= 0.000469567 cunTime= 0.000469567 edges= 5 schur= 0
Lambda= 0.883333 levenbergiter= 1
Iterations: 1 ch12= 49457.525924 time= 0.000393021 cunTime= 0.000802588 edges= 5 schur= 0
Lambda= 0.294444 levenbergiter= 1
Iterations: 2 ch12= 49431.181081 time= 0.000372075 cunTime= 0.00123466 edges= 5 schur= 0
Lambda= 0.196296 levenbergiter= 1
Iterations: 3 ch12= 49427.420182 time= 0.000371626 cunTime= 0.00160629 edges= 5 schur= 0
Lambda= 0.130864 levenbergiter= 1
Iterations: 4 ch12= 49421.651841 time= 0.000372119 cunTime= 0.00197841 edges= 5 schur= 0
Lambda= 0.887243 levenbergiter= 1
Iterations: 5 ch12= 49396.529370 time= 0.000371599 cunTime= 0.00235001 edges= 5 schur= 0
Lambda= 0.058102 levenbergiter= 1
Iterations: 6 ch12= 49373.983056 time= 0.000371261 cunTime= 0.00272127 edges= 5 schur= 0
Lambda= 0.338775 levenbergiter= 1
Iterations: 7 ch12= 49369.449696 time= 0.000371666 cunTime= 0.00309293 edges= 5 schur= 0
Lambda= 0.025850 levenbergiter= 1
Iterations: 8 ch12= 49369.449696 time= 0.00145776 cunTime= 0.00450669 edges= 5 schur= 0
Lambda= 931334243928713.250000 levenbergiter= 10
finish
FinalError:49369.5
```

```
1: rosrun ls_slam ls_slam
Iteration: 74 ch12= 10353.654963 time= 0.380878 cunTime= 26.2778 edges= 3995 schur= 0
lambda= 284973.71067 levenbergIter= 2
Iteration: 75 ch12= 10353.654963 time= 0.380538 cunTime= 26.6584 edges= 3995 schur= 0
lambda= 37092.97125 levenbergIter= 1
Iteration: 76 ch12= 10353.654963 time= 0.309677 cunTime= 26.968 edges= 3995 schur= 0
lambda= 253309.983170 levenbergIter= 1
Iteration: 77 ch12= 10353.654963 time= 0.472338 cunTime= 27.4404 edges= 3995 schur= 0
lambda= 120876.97698 levenbergIter= 3
Iteration: 78 ch12= 10353.654963 time= 0.317881 cunTime= 27.7583 edges= 3995 schur= 0
lambda= 900657.717939 levenbergIter= 1
Iteration: 79 ch12= 10353.654963 time= 0.37776 cunTime= 28.136 edges= 3995 schur= 0
lambda= 120876.97698 levenbergIter= 3
Iteration: 80 ch12= 10353.654963 time= 0.387395 cunTime= 28.5234 edges= 3995 schur= 0
lambda= 160169.276336 levenbergIter= 2
Iteration: 81 ch12= 10353.654963 time= 0.499485 cunTime= 29.0229 edges= 3995 schur= 0
lambda= 833469.472191 levenbergIter= 3
Iteration: 82 ch12= 10353.654963 time= 0.294176 cunTime= 29.3171 edges= 3995 schur= 0
lambda= 5693046.315860 levenbergIter= 1
Iteration: 83 ch12= 10353.654963 time= 0.834481 cunTime= 30.1515 edges= 3995 schur= 0
lambda= 709545564.921272 levenbergIter= 7
Iteration: 84 ch12= 10353.654963 time= 0.567477 cunTime= 30.719 edges= 3995 schur= 0
lambda= 8150482580411160.000000 levenbergIter= 4
FinalError:10353.7
CMake
A touchair-2080T LSSLAMProject --catkin make
cat path: /home/touchair/Downloads/HM6/LSSLAMProject
Source space: /home/touchair/Downloads/HM6/LSSLAMProject/src
Build space: /home/touchair/Downloads/HM6/LSSLAMProject/build
Devel space: /home/touchair/Downloads/HM6/LSSLAMProject/devel
Install space: /home/touchair/Downloads/HM6/LSSLAMProject/install
###
### Running command: "make cmake_check_build_system" in "/home/touchair/Downloads/HM6/LSSLAMProject/build"
###
###
### Running command: "make -j8 -l8" in "/home/touchair/Downloads/HM6/LSSLAMProject/build"
###
Scanning dependencies of target ls_slam
[ 25%] Building CXX object ls_slam/CMakeFiles/ls_slam.dir/src/main.cpp.o
[ 58%] Linking CXX executable /home/touchair/Downloads/HM6/LSSLAMProject/devel/lib/ls_slam/ls_slam
[100%] Built target ls_slam
A touchair-2080T LSSLAMProject --source devel/setup.zsh
touchair-2080T LSSLAMProject --rosrun ls_slam ls_slam
Iniferior: 2.05992e+06
Iteration: 0 ch12= 51574.948019 time= 0.279375 cunTime= 0.279375 edges= 3070 schur= 0
lambda= 0.150732 levenbergIter= 1
Iteration: 1 ch12= 3982.007331 time= 0.2563 cunTime= 0.535676 edges= 3070 schur= 0
lambda= 0.104088 levenbergIter= 1
Iteration: 2 ch12= 37926.215906 time= 0.422323 cunTime= 0.958999 edges= 3070 schur= 0
lambda= 0.535935 levenbergIter= 3
Iteration: 3 ch12= 36132.808005 time= 0.507572 cunTime= 1.46657 edges= 3070 schur= 0
lambda= 22.866547 levenbergIter= 4
Iteration: 4 ch12= 36132.808005 time= 0.993813 cunTime= 2.46038 edges= 3070 schur= 0
lambda= 82385416838115392.000000 levenbergIter= 10
FinalError:36132.8
```

```
1/1 + T Ttlbc 默认 2:rviz
t:rosrun ls_slam ls_slam
iteration= 58 ch12= 10353.654977 t1ne= 0.460898 cun1ne= 20.0365 edges= 3995 schur= 0
lambda= 1428.088254 levenbergiter= 2 t1ne= 0.453884 cun1ne= 20.4903 edges= 3995 schur= 0
iteration= 59 ch12= 10353.654969 t1ne= 0.453884 cun1ne= 20.4903 edges= 3995 schur= 0
lambda= 1904.117672 levenbergiter= 2 t1ne= 0.390501 cun1ne= 20.8808 edges= 3995 schur= 0
iteration= 60 ch12= 10353.654966 t1ne= 0.390501 cun1ne= 20.8808 edges= 3995 schur= 0
lambda= 2538.823560 levenbergiter= 2 t1ne= 0.289249 cun1ne= 22.0538 edges= 3995 schur= 0
iteration= 61 ch12= 10353.654965 t1ne= 0.400645 cun1ne= 21.2815 edges= 3995 schur= 0
lambda= 3385.098084 levenbergiter= 2 t1ne= 0.483036 cun1ne= 21.7645 edges= 3995 schur= 0
iteration= 62 ch12= 10353.654964 t1ne= 0.483036 cun1ne= 21.7645 edges= 3995 schur= 0
lambda= 18053.856466 levenbergiter= 3 t1ne= 0.289249 cun1ne= 22.0538 edges= 3995 schur= 0
iteration= 63 ch12= 10353.654964 t1ne= 0.309386 cun1ne= 22.3632 edges= 3995 schur= 0
lambda= 12035.984297 levenbergiter= 1 t1ne= 0.487646 cun1ne= 22.8508 edges= 3995 schur= 0
iteration= 64 ch12= 10353.654963 t1ne= 0.313378 cun1ne= 23.1642 edges= 3995 schur= 0
lambda= 8023.936190 levenbergiter= 1 t1ne= 0.385912 cun1ne= 23.5501 edges= 3995 schur= 0
iteration= 65 ch12= 10353.654963 t1ne= 0.413029 cun1ne= 23.9631 edges= 3995 schur= 0
lambda= 42794.326390 levenbergiter= 3 t1ne= 0.40375 cun1ne= 24.3669 edges= 3995 schur= 0
iteration= 66 ch12= 10353.654963 t1ne= 0.369174 cun1ne= 24.7361 edges= 3995 schur= 0
iteration= 67 ch12= 10353.654963 t1ne= 0.387166 cun1ne= 25.1232 edges= 3995 schur= 0
lambda= 38039.401236 levenbergiter= 2 t1ne= 0.380878 cun1ne= 26.2778 edges= 3995 schur= 0
iteration= 68 ch12= 10353.654963 t1ne= 0.380878 cun1ne= 26.2778 edges= 3995 schur= 0
lambda= 50719.201647 levenbergiter= 2 t1ne= 0.380878 cun1ne= 26.2778 edges= 3995 schur= 0
iteration= 69 ch12= 10353.654963 t1ne= 0.380878 cun1ne= 26.2778 edges= 3995 schur= 0
lambda= 67025.082196 levenbergiter= 2 t1ne= 0.380878 cun1ne= 26.2778 edges= 3995 schur= 0
iteration= 70 ch12= 10353.654963 t1ne= 0.380878 cun1ne= 26.2778 edges= 3995 schur= 0
lambda= 90167.469595 levenbergiter= 2 t1ne= 0.380878 cun1ne= 26.2778 edges= 3995 schur= 0
iteration= 71 ch12= 10353.654963 t1ne= 0.380878 cun1ne= 26.2778 edges= 3995 schur= 0
lambda= 122223.292794 levenbergiter= 2 t1ne= 0.380878 cun1ne= 26.2778 edges= 3995 schur= 0
iteration= 72 ch12= 10353.654963 t1ne= 0.380878 cun1ne= 26.2778 edges= 3995 schur= 0
lambda= 160297.723725 levenbergiter= 2 t1ne= 0.380878 cun1ne= 26.2778 edges= 3995 schur= 0
iteration= 73 ch12= 10353.654963 t1ne= 0.380878 cun1ne= 26.2778 edges= 3995 schur= 0
lambda= 213730.298308 levenbergiter= 2 t1ne= 0.380878 cun1ne= 26.2778 edges= 3995 schur= 0
iteration= 74 ch12= 10353.654963 t1ne= 0.380878 cun1ne= 26.2778 edges= 3995 schur= 0
lambda= 284973.731067 levenbergiter= 2 t1ne= 0.380878 cun1ne= 26.2778 edges= 3995 schur= 0
iteration= 75 ch12= 10353.654963 t1ne= 0.380878 cun1ne= 26.2778 edges= 3995 schur= 0
lambda= 379964.974753 levenbergiter= 2 t1ne= 0.380878 cun1ne= 26.2778 edges= 3995 schur= 0
iteration= 76 ch12= 10353.654963 t1ne= 0.380878 cun1ne= 26.2778 edges= 3995 schur= 0
lambda= 53309.983170 levenbergiter= 1 t1ne= 0.472338 cun1ne= 27.4404 edges= 3995 schur= 0
iteration= 77 ch12= 10353.654963 t1ne= 0.317881 cun1ne= 27.7583 edges= 3995 schur= 0
lambda= 1350986.576908 levenbergiter= 3 t1ne= 0.37776 cun1ne= 28.136 edges= 3995 schur= 0
iteration= 78 ch12= 10353.654963 t1ne= 0.37776 cun1ne= 28.136 edges= 3995 schur= 0
lambda= 908657.717939 levenbergiter= 1 t1ne= 0.387395 cun1ne= 28.5234 edges= 3995 schur= 0
iteration= 79 ch12= 10353.654963 t1ne= 0.387395 cun1ne= 28.5234 edges= 3995 schur= 0
lambda= 1200876.957252 levenbergiter= 2 t1ne= 0.499485 cun1ne= 29.0229 edges= 3995 schur= 0
iteration= 80 ch12= 10353.654963 t1ne= 0.499485 cun1ne= 29.0229 edges= 3995 schur= 0
lambda= 1601169.276336 levenbergiter= 2 t1ne= 0.294176 cun1ne= 29.3171 edges= 3995 schur= 0
iteration= 81 ch12= 10353.654963 t1ne= 0.294176 cun1ne= 29.3171 edges= 3995 schur= 0
lambda= 853959.473791 levenbergiter= 3 t1ne= 0.834481 cun1ne= 30.1515 edges= 3995 schur= 0
iteration= 82 ch12= 10353.654963 t1ne= 0.834481 cun1ne= 30.1515 edges= 3995 schur= 0
lambda= 5693046.315800 levenbergiter= 1 t1ne= 0.567477 cun1ne= 30.719 edges= 3995 schur= 0
iteration= 83 ch12= 10353.654963 t1ne= 0.567477 cun1ne= 30.719 edges= 3995 schur= 0
lambda= 7959455644932.773438 levenbergiter= 7 t1ne= 0.567477 cun1ne= 30.719 edges= 3995 schur= 0
iteration= 84 ch12= 10353.654963 t1ne= 0.567477 cun1ne= 30.719 edges= 3995 schur= 0
lambda= 8150482580411160.000000 levenbergiter= 4 t1ne= 0.567477 cun1ne= 30.719 edges= 3995 schur= 0
FinalError:10353.7
finish
FinalError:10353.7
```

ceres:

```
1/1 + T Ttlbc 默认 2:rviz
t:rosrun ls_slam ls_slam
A touchair-2080T LSSLAMProject ->rosrun ls_slam ls_slam
initError: 251853

Solver Summary (v.1.14.0-eigen-(3.3.7)-lapack-suitesparse-(4.4.6)-cxsparse-(3.1.4)-eigensparse-openmp-no_tbb)

Parameter blocks      Original      Reduced
Parameters            12            9
Residual blocks        12            9
Residuals              5            5
Residuals              15            15

Minimizer              TRUST_REGION

Sparse linear algebra library  SUITE_SPARSE
Trust region strategy         LEVENBERG_MARQUARDT

Linear solver            SPARSE_NORMAL_CHOLESKY
Threads                  1
Linear solver ordering    AUTOMATIC

Cost:
Initial                  1.259266e+05
Final                    2.467825e+04
Change                   1.012484e+05

Minimizer iterations    3
Successful steps        3
Unsuccessful steps      0

Time (in seconds):
Preprocessor            0.000125
Residual only evaluation 0.000101 (3)
Jacobian & residual evaluation 0.000960 (3)
Linear solver           0.000001 (3)
Minimizer               0.001263

Postprocessor           0.000018
Total                  0.001407

Termination:          CONVERGENCE (Function tolerance reached. |cost_change|/cost: 6.5308
0e-10 <= 1.000000e-06)

finish
FinalError: 49356.5
```

```
1/1 + [ ] [ ] Tilt: 默认
1: roslaunch ls_slam ls_slam
A touchair-2080T LSSLAMProject -> roslaunch ls_slam ls_slam
InitError: 2.05092e+06

Solver Summary (v 1.14.0-eigen-(3.3.7)-lapack-suitesparse-(4.4.6)-cxsparse-(3.1.4)-eigensparse-openmp
-no_tbb)

Parameter blocks          Original      Reduced
Parameters                2187        2184
Residual blocks           3070        3070
Residuals                 9210        9210

Minimizer                  TRUST_REGION

Sparse linear algebra library SUITE_SPARSE
Trust region strategy      LEVENBERG_MARQUARDT

Linear solver              Given          Used
Threads                   1             1
Linear solver ordering     AUTOMATIC     2184

Cost:
Initial                   1.025461e+06
Final                     3.270103e+01
Change                   1.025429e+06

Minimizer iterations       7
Successful steps           7
Unsuccessful steps        0

Time (in seconds):
Preprocessor              0.006626
  Residual only evaluation 0.129995 (7)
  Jacobian & residual evaluation 1.327142 (7)
  Linear solver            0.023077 (7)
  Minimizer                1.493529
Postprocessor              0.004514
Total                     1.504070

Termination:              CONVERGENCE (Function tolerance reached. |cost_change|/cost: 9.0428
01e-08 <= 1.000000e-06)

Finish
FinalError: 65.4021
[ ]
```

```
1/1 + [ ] [ ] Tilt: 默认
1: roslaunch ls_slam ls_slam
#####
##### Running command: "make -j8 -l8" in "/home/touchair/Downloads/HM6/LSSLAMProject/build"
#####
Scanning dependencies of target ls_slam
[ 25%] Building CXX object ls_slam/CMakeFiles/ls_slam.dir/src/main.cpp.o
[ 50%] Linking CXX executable /home/touchair/Downloads/HM6/LSSLAMProject/develop/lib/ls_slam/ls_slam
[100%] Built target ls_slam
A touchair-2080T LSSLAMProject -> source devel/setup.zsh
A touchair-2080T LSSLAMProject -> roslaunch ls_slam ls_slam
InitError: 3.08592e+08

Solver Summary (v 1.14.0-eigen-(3.3.7)-lapack-suitesparse-(4.4.6)-cxsparse-(3.1.4)-eigensparse-openmp
-no_tbb)

Parameter blocks          Original      Reduced
Parameters                5823        5820
Residual blocks           3995        3995
Residuals                 11985       11985

Minimizer                  TRUST_REGION

Sparse linear algebra library SUITE_SPARSE
Trust region strategy      LEVENBERG_MARQUARDT

Linear solver              Given          Used
Threads                   1             1
Linear solver ordering     AUTOMATIC     5820

Cost:
Initial                   1.542960e+08
Final                     5.172337e+03
Change                   1.542909e+08

Minimizer iterations       8
Successful steps           8
Unsuccessful steps        0

Time (in seconds):
Preprocessor              0.014746
  Residual only evaluation 0.242907 (0)
  Jacobian & residual evaluation 2.014007 (0)
  Linear solver            0.034945 (0)
  Minimizer                2.316959
Postprocessor              0.011285
Total                     2.342990

Termination:              CONVERGENCE (Function tolerance reached. |cost_change|/cost: 8.4113
65e-07 <= 1.000000e-06)

Finish
FinalError: 10344.7
[ ]
```

