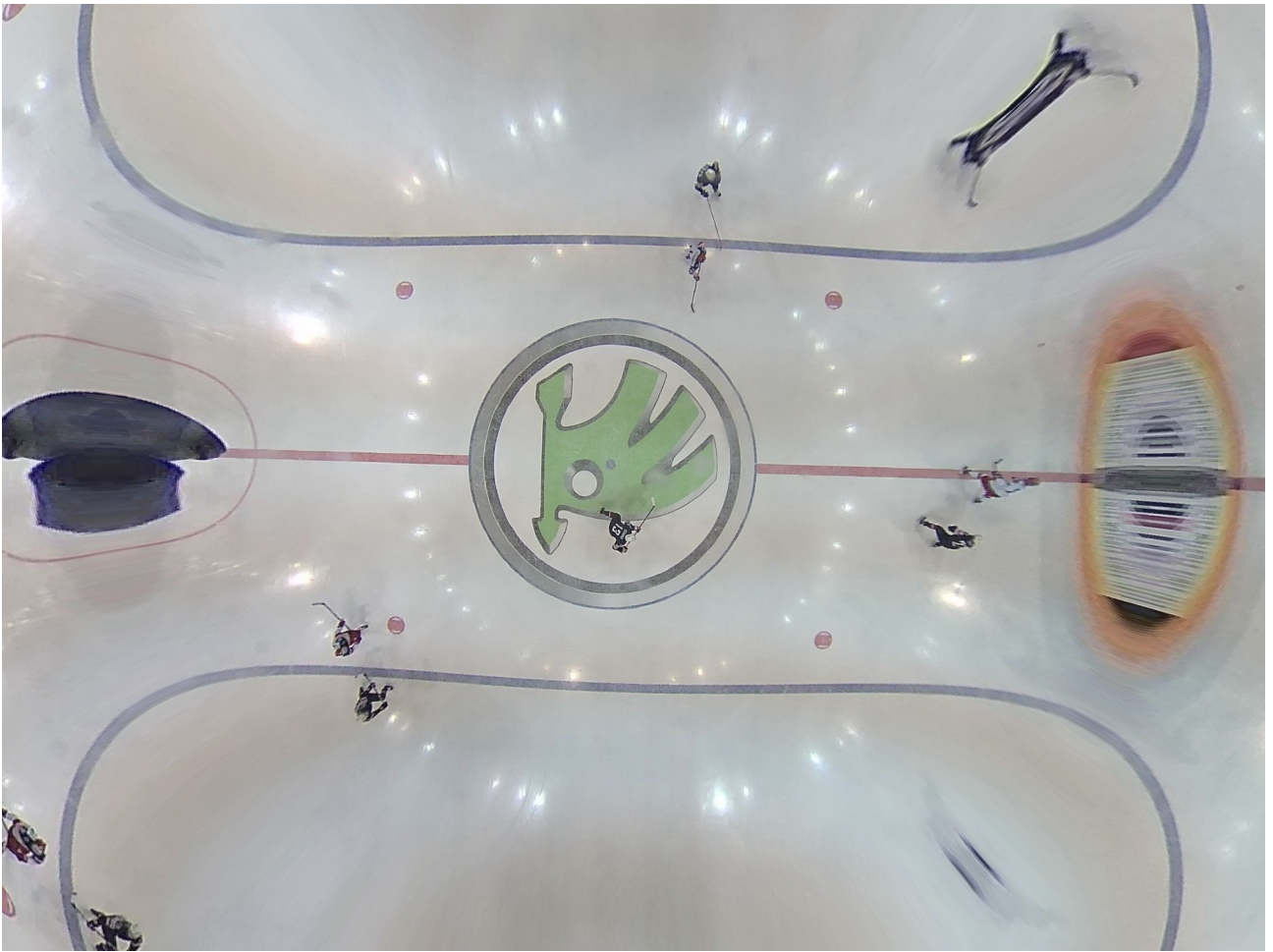


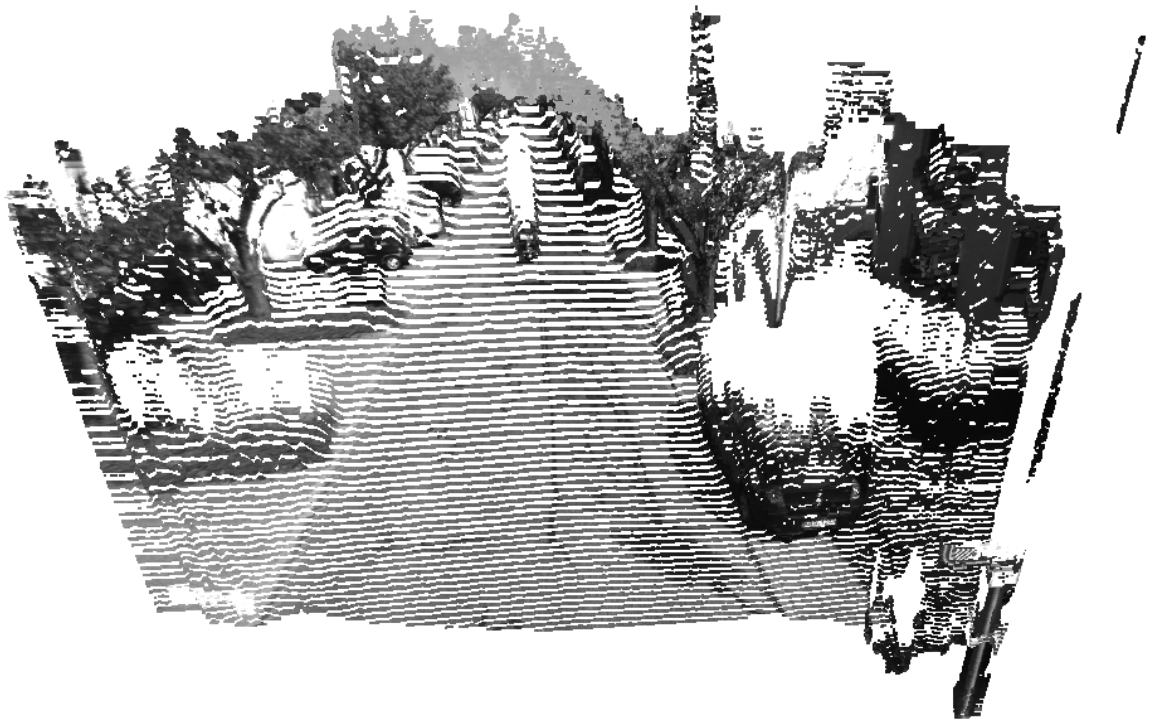


3.1 鱼镜头与普通镜头相比有更大的视野范围

3.2 普通相机成像遵循的是针孔相机模型，在成像过程中实际场景中的直线仍被投影为图像平面上的直线。但是鱼眼相机如果按照针孔相机模型成像的话，投影图像会变得非常大，当相机视场角达到 180° 时，图像甚至会变为无穷大。所以，鱼眼相机的投影模型为了将尽可能大的场景投影到有限的图像平面内，允许了相机畸变的存在。并且由于鱼眼相机的径向畸变非常严重，所以鱼眼相机主要的是考虑径向畸变，而忽略其余类型的畸变。

3.3





$$5.1 \quad \frac{\partial Ax}{\partial x} = \begin{bmatrix} \frac{\partial Ax_1}{\partial x_1} & \frac{\partial Ax_1}{\partial x_2} & \dots & \frac{\partial Ax_1}{\partial x_n} \\ \frac{\partial Ax_2}{\partial x_1} & \frac{\partial Ax_2}{\partial x_2} & \dots & \frac{\partial Ax_2}{\partial x_n} \\ \vdots & \vdots & \ddots & \vdots \\ \frac{\partial Ax_n}{\partial x_1} & \frac{\partial Ax_n}{\partial x_2} & \dots & \frac{\partial Ax_n}{\partial x_n} \end{bmatrix}$$

$$\frac{\partial Ax_i}{\partial x_k} = \frac{\partial a_{ik}x}{\partial x_k} = a_{ik}$$

$$\frac{\partial Ax}{\partial x} = \begin{bmatrix} a_{11} & a_{12} & \dots & a_{1n} \\ a_{21} & a_{22} & \dots & a_{2n} \\ \vdots & \vdots & \ddots & \vdots \\ a_{n1} & a_{n2} & \dots & a_{nn} \end{bmatrix} = A^T$$

$$5.2 \quad \frac{\partial x^T A x}{\partial x} = \begin{bmatrix} \frac{\partial x^T A x}{\partial x_1} & \frac{\partial x^T A x}{\partial x_2} & \dots & \frac{\partial x^T A x}{\partial x_n} \end{bmatrix}$$

$$\frac{\partial x^T A x}{\partial x_k} = \frac{\partial \sum_{i=1}^n \sum_{j=1}^n x_i A_{ij} x_j}{\partial x_k} = \sum_{i=1}^n A_{ik} x_i + \sum_{j=1}^n A_{kj} x_j$$

$$= A_k^T x + A_k x$$

$$\frac{\partial x^T A x}{\partial x} = A^T x + A x$$

$$5.3 \quad ab^T = \begin{bmatrix} a_1 b_1 & a_1 b_2 & \dots & a_1 b_n \\ a_2 b_1 & a_2 b_2 & \dots & a_2 b_n \\ \vdots & \vdots & \ddots & \vdots \\ a_n b_1 & a_n b_2 & \dots & a_n b_n \end{bmatrix} \quad b^T a = \sum_{i=1}^n a_i b_i \Rightarrow \text{tr}(ab^T) = b^T a$$

$$\sum a = Ax, \quad b = x \Rightarrow \text{tr}(Axx^T) = \text{tr}((Ax)x^T) = x^T Ax$$

6

```
touchair@touchair-2020T:~/下载/视觉SLAM课程/L4/code/build$ ./gaussnewton
total cost: 3.19575e+06
total cost: 376785
total cost: 35673.6
total cost: 2195.01
total cost: 174.853
total cost: 102.78
total cost: 101.937
total cost: 101.937
total cost: 101.937
cost: 101.937, last cost: 101.937
estimated abc = 0.890912, 2.1719, 0.943629
touchair@touchair-2020T:~/下载/视觉SLAM课程/L4/code/build$
```

7

7.1 根据 $v_k = x_k - x_{k-1} + w_k$, $y_k = x_k + u_k$

而 $z = Hx = e \sim N(0, \Sigma)$

$$\Rightarrow H = \begin{bmatrix} -1 & 1 & 0 & 0 \\ 0 & -1 & 1 & 0 \\ 0 & 0 & -1 & 1 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

7.2 $x = \arg \max p(x|z) = \arg \max p(z|x)$

$$= \prod_{k=1}^3 p(v_k | x_{k-1}, x_k) \prod_{k=1}^3 p(y_k | x_k)$$

$$p(v_k | x_{k-1}, x_k) = N(x_k - x_{k-1}, Q), \quad p(y_k | x_k) = N(x_k, R)$$

相移函数取对数 $\Rightarrow \min \sum_{k=1}^3 e^T Q^{-1} e + \sum_{k=1}^3 e^T R^{-1} e$

$$\text{所以 } W = \begin{bmatrix} Q & 0 & 0 & 0 & 0 & 0 \\ 0 & Q & 0 & 0 & 0 & 0 \\ 0 & 0 & Q & 0 & 0 & 0 \\ 0 & 0 & 0 & R & 0 & 0 \\ 0 & 0 & 0 & 0 & R & 0 \\ 0 & 0 & 0 & 0 & 0 & R \end{bmatrix}$$

7.3. H 是 6×4 矩阵, 方程个数大于未知量个数, 是一个超定矩阵
存在唯一解. $x = (H^T H)^{-1} H^T z$