

3. $\vec{E} = -\nabla\phi - \frac{\partial \vec{A}}{\partial t}$

$\vec{B} = \nabla \times \vec{A}$

$\nabla \cdot \vec{B} = \nabla \cdot (\nabla \times \vec{A}) = 0$. 矢量的旋度无源.

$\nabla \times \vec{E} = \nabla \times (-\nabla\phi) - \nabla \times \frac{\partial \vec{A}}{\partial t}$

$= -\nabla \times \frac{\partial \vec{A}}{\partial t} = -\frac{\partial}{\partial t}(\nabla \times \vec{A}) = -\frac{\partial \vec{B}}{\partial t}$

即上述两场均满足 Maxwell 方程组

4. 速率方程组, 稳态时 $\frac{dN_0}{dt} = -RN_0 + \frac{N_1}{\tau_{10}} = 0 \Rightarrow N_1 = \tau_{10}RN_0$

$\frac{dN_1}{dt} = \frac{N_2}{\tau} - \frac{N_1}{\tau_{10}} = 0 \Rightarrow N_2 = \frac{\tau}{\tau_{10}}N_1$

$\frac{dN_2}{dt} = \frac{N_3}{\tau_{32}} - \frac{N_2}{\tau} = 0$

$\frac{dN_3}{dt} = RN_0 - \frac{N_3}{\tau_{32}} = 0$

则 $N_0 = \frac{1}{\tau R}N_2$ $N_1 = \frac{\tau_{10}}{\tau}N_2$

$N_0 + N_1 + N_2 = N \Rightarrow \frac{1}{\tau R}N_2 + \frac{\tau_{10}}{\tau}N_2 + N_2 = N$

$N_2 = \frac{1}{\frac{1}{\tau R} + \frac{\tau_{10}}{\tau} + 1} N = \frac{R}{(\frac{\tau_{10}}{\tau} + 1)R + \frac{1}{\tau}} N$

$N_1 = \frac{\tau_{10}}{\tau}N_2$

$N_2 - N_1 = \frac{(1 - \frac{\tau_{10}}{\tau})R}{(\frac{\tau_{10}}{\tau} + 1)R + \frac{1}{\tau}} N$