2020~2021复复函数与联分变换 (多考答集)

- ADBC BCAC BODA

二.解: : $u(x,y) + V(x,y) = y^2 + 2xy - x^2 + 2(x-y)$ 两边对义水偏写可将:

 $U_X + V_X = 2y - 2x + 2 \cdots 0$

西边对了求确寻得:

Ny + Vy = 2y+2x -2 -- 3

图为打到路折,所以以满足一尺方镜

 $U_X = V_y$, $U_y = -V_X$

父入②式两得:

 $U_{\times} - V_{\times} = 2y+2\times-2 \dots 3$

由①③式 Vx=2y···(A), Vx=-2x+2··

对A作解影为 W(X,分)=2X分十个(分), 个(分)特益

2 My=-Vx = 2X-2

RP 4'(y) = -2 $\therefore 2x + \varphi'(y) = 2x - 2$

: q(y) = - 2 + C

:. u(x,y) = 2xy-2y+(

 $V(x,y) = y^2 - x^2 + 2x + C$

C为任务专数.

$$2 + (2) = \frac{1}{2-3} - \frac{1}{2-2}$$

$$\frac{1}{2^{-2}} = \frac{1}{2^{-4+1}} = \frac{1}{\sum_{n=0}^{+\infty} (-1)^n (2^{-4})^n}$$

$$\frac{1}{2^{-2}} = \frac{1}{2^{-4+2}} = \frac{1$$

$$\therefore f(2) = \frac{1}{2-3} - \frac{1}{2-2} = \frac{1}{2} (-1)^{2} \left(1 - \frac{1}{2^{1+1}}\right) (2-4)^{1/2}$$

$$\frac{1}{2-3} = \frac{1}{2-4+1} = \frac{1}{2-4} \frac{1}{1+\frac{1}{2-4}} = \frac{1}{2+4} \frac{\frac{1}{2}}{\frac{1}{2-4}} = \frac{1}{2+4} \frac{\frac{1}{2}}{\frac{1}{2-4}} = \frac{1}{2-4+1} = \frac{$$

$$(+1/2) = \frac{+10}{2} (-1)^n \frac{1}{(2-4)^{n+1}} + \frac{+10}{2} (-1)^n \frac{1}{2^{n+1}} (2-4)^n$$

$$\frac{1}{2-3} = \frac{\frac{1}{2}}{\frac{2}{N=0}} (+)^{N} \frac{1}{(2-4)^{N+1}}$$

$$\frac{1}{2-2} = \frac{1}{2-4+2} = \frac{1}{2-4} \frac{1}{1+\frac{2}{2-4}} = \frac{1}{2-4} \frac{\frac{1}{2}}{N=0} (-2)^{N} \frac{1}{(2-4)^{N}}$$

四.(解结一. 由於所字級公文
唇式 = 2元;
$$\frac{(H_2-e^2)^{(q)}}{9!}\Big|_{2=0} = -\frac{22i}{9!}$$

解法二、由台级计算::+(3)在131=119只有一个的运务点是=0

$$2 \cdot \frac{1}{2} (2) = \frac{1+2-e^2}{2^{10}} = \frac{1}{2^{10}} \left(-\frac{2^1}{2!} - \frac{2^3}{3!} - \cdots - \frac{2^9}{9!} - \cdots \right)$$

:. Res [f(2), 0] = - 1/9!

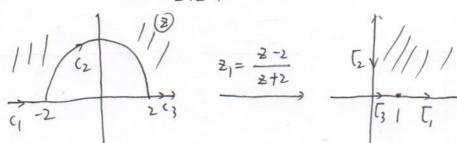
$$\frac{1}{2} \frac{1}{\sqrt{2}} = 22i \left(-\frac{1}{9!}\right) = -\frac{22i}{9!}$$

d.解:: 3数十级= 1-1032 在131=1内只有务点2=0.

又 2=0 为 1-10gzin = 野葵点, 是Sin3265=野夏点

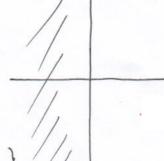
$$= \lim_{z \to 0} \frac{1 - w_3 z}{\sin^2 z} = \lim_{z \to 0} \frac{\sin z}{z \sin z \cos z} = \frac{1}{z}$$

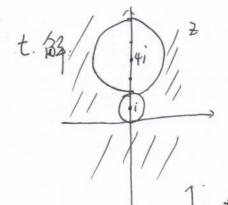
六解· Bey 街 W= i (是-2) 可分解的如下映船的复合 $z_1 = \frac{2-2}{2+2}$ $z_2 = z_1^2$ $\omega = 12$



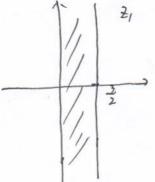
$$\Xi_1 = \frac{2^{-2}}{2+2}$$

$$\frac{2_{\lambda}=\frac{1}{2_{1}}^{2}}{2_{\lambda}}$$





$$Z_1 = \frac{2}{2 - \lambda_1}$$



$$z_{2}=iz_{1}$$
 $z_{3}=\frac{1}{3}z_{2}$

$$w=e^{2s}$$

$$: W = e^{\frac{2}{3}\chi \frac{12}{2-2i}}$$

八.
$$i2 F(s) = & Ef(s) \end{bmatrix}$$
, 好方程而处作程底接%:
$$s^{4}F(s) - s^{3}f(o) - s^{2}f'(o) - sf'(o) - f''(o) - F(s) = \frac{1}{s}$$

$$(s^{4}-1) F(s) = \frac{1}{s} + s + 2 = \frac{(1+s)^{2}}{s}$$

$$\therefore F(s) = \frac{(s+1)^{2}}{(s^{4}+1)s} = \frac{s+1}{(s+1)s \cdot (s+1)}$$

$$= \frac{1}{s+1} - \frac{1}{s^{2}+1} - \frac{1}{s}$$

$$\therefore f(t) = & \frac{1}{s} F(s) = e^{t} - sint -1$$

九、沙啊: 宝岩十(3)的老点,且十(3) 丰。

三、五岁十(3)的一所名点,且不为十(3)的意志

off 38名Fizzi タルコ (2) dを モーのる (14(2) かー所ねた

:. $\text{Res}\left[\frac{+(2)}{2^{2}+(2)} \circ\right] = \lim_{2 \to 0} \frac{+(2)}{2+(2)}$

 $= \lim_{z \to 0} \frac{f'(z)}{f'(z) + 2f''(z)} = \frac{f'(0)}{f'(0)} = 1$

 $7778 = \frac{1}{221} \int_{121} \frac{2+6}{+21} dz$

: 2=0 为被救马额的可考考点

:. I2 =0.

:. I,+ Iz=1. 分起特治。