Compiler Optimizations and Benchmarking

Lecture 02



Overview

Last day...

- Flynn's taxonomy types of parallel architectures
- Dependencies RAW forces sequence, avoid WAR+WAW using renaming
- Amdahl's law make the common case fast, infinite parallelism is doomed
- Gustafson's law if you want more parallelism, increase the problem size
- Readings read upon compiler optimizations
- Mini-assignment try out compiler optimizations on matrix multiply

Today...

- Optimizing your sequential program
 - Compiler optimizations
 - Measuring performance of a single program
 - Summarizing performance distill set of performance results into 1 magic number
- Next week
 - A general introduction to parallel programming
 - Culler text, Chapter 2

Making your program go fast!

- Wikipedia article (lots of links)
 - Follow links for explanations and examples
- Bacon 76-page survey
 - General compiler optimizations for any CPU
- Padua 18-page Optimizations for Supercomputers
 - Describes dependences very well
 - Techniques to find parallelism in loops etc
- Assignment 0
 - Write matrix multiply
 - Try C compiler optimizations: none, -O, -O2, -O3
 - Rewrite matrix multiply with manual optimizations

Gcc compiler options, -O is always safe

-0 -01

Optimize. Optimizing compilation takes somewhat more time, and a lot more memory for a large function.

With -O, the compiler tries to reduce code size and execution time, without performing any optimizations that take a great deal of compilation time.

- -O turns on the following optimization flags:
 - -fauto-inc-dec
 - -fcompare-elim
 - -fcprop-registers
 - -fdce
 - -fdefer-pop
 - -fdelayed-branch
 - -fdse
 - -fguess-branch-probability
 - -fif-conversion2
 - -fif-conversion
 - -fipa-pure-const
 - -fipa-profile
 - -fipa-reference
 - -fmerge-constants
 - -fsplit-wide-types
 - -ftree-bit-ccp
 - -ftree-builtin-call-dce
 - -ftree-ccp
 - -ftree-ch
 - -ftree-copyrename
 - -ftree-dce
 - -ftree-dominator-opts
 - -ftree-dse
 - -ftree-forwprop
 - -ftree-fre
 - -ftree-phiprop
 - -ftree-sra
 - -ftree-pta
 - -ftree-ter
 - -funit-at-a-time

· Gcc compiler options, -O2 is good

-02

Optimize even more. GCC performs nearly all supported optimizations that do not involve a space-speed tradeoff. As compared to -O, this option increases both compilation time and the performance of the generated code.

-O2 turns on all optimization flags specified by -O. It also turns on the following optimization flags:

- -fthread-jumps
- -falign-functions -falign-jumps
- -falign-loops -falign-labels
- -fcaller-saves
- -fcrossjumping
- -fcse-follow-jumps -fcse-skip-blocks
- -fdelete-null-pointer-checks
- -fdevirtualize
- -fexpensive-optimizations
- -fgcse -fgcse-lm
- -finline-small-functions
- -findirect-inlining
- -fipa-sra
- -foptimize-sibling-calls
- -fpartial-inlining
- -fpeephole2
- -fregmove
- -freorder-blocks -freorder-functions
- -frerun-cse-after-loop
- -fsched-interblock -fsched-spec
- -fschedule-insns -fschedule-insns2
- -fstrict-aliasing -fstrict-overflow
- -ftree-switch-conversion
- -ftree-pre
- -ftree-vrp

Gcc compiler options, -O3 is aggressive/unsafe

-O3
Optimize yet more. -O3 turns on all optimizations specified by -O2 and also turns on the -finline-functions, -funswitch-loops, -fpredictive-commoning, -fgcse-after-reload, -ftree-vectorize and -fipa-cp-clone options.

- Lots of gcc optimization options
 - http://gcc.gnu.org/onlinedocs/gcc/Optimize-Options.html
 - These change often -- check the version-specific manual hydra2:~> gcc --version gcc (Ubuntu 4.9.3-13ubuntu2) 4.9.3
- Ask gcc which optimizations are on/off:

Measuring Performance

Evaluating performance of one and many programs!

Benchmarking – SPEC CPU2000 standard suite and others.

Two Fundamental Performance Concepts

1. Throughput (aka bandwidth)

- Total amount of work done in a given time
 - Boeing 747
 - Laundromat with many washers & dryers
 - Important for computer data centres

2. Response time (aka latency)

- Time from start to end of a given task
 - Concorde
 - One fast, modern laundry machine at home
 - Important for personal computers

Which is more important for this course?

- Mostly response time!
- Better response time → usually higher throughput
- Higher throughput != better response time

Evaluating Performance

... of one program!

(aka latency)

MIPS and others...

- MIPS and its relatives...
 - MIPS = Millions of Instructions Per Second
 - Aka Meaningless Indicator of Processor Speed
 - Relative MIPS (VAX 11/780 = 1 MIPS)
 - Someone got it wrong, it is actually 0.5 MIPS! (see Joel Emer)
 - Dhrystone MIPS
 - GIPS
 - MFLOPS, GFLOPS, TFLOPS
 - MOPS, GOPS
- What's wrong with these?

Detailed Performance Equation

CPUTime =
$$\sum_{i}$$
 (InstrCount_i * CPI_i) * CycleTime

- CPUTime total run time of a program
 - Program contains mixture of instruction types
- InstrCount_i count of instructions of type i
- CPI_i cycles per instruction of type i
- CycleTime 1/frequency, eg 1/1GHz = 1ns

Example

InstrType _i	CPI,
<i>i</i> =1	1
<i>i</i> =2	2
<i>i</i> =3	3

Prog	InstrCount _i		
ram:	<i>i</i> =1 <i>i</i> =2		<i>i</i> =3
Α	4	2	4
В	8	2	2

Given

- Same CPU with 3 different instruction types
- CycleTime = 20ns
- Program A, Program B with diff instruction mixes

Find

- Performance of A, B

Example (cont'd)

InstrType _i	CPI,
<i>i</i> =1	1
<i>i</i> =2	2
<i>i</i> =3	3

Prog	InstrCount _i		
ram:	<i>i</i> =1	<i>i</i> =2	<i>i</i> =3
Α	4	2	4
В	8	2	2

CPUTime = \sum_{i} (InstrCount_i * CPI_i) * CycleTime

Program A (total 10 instructions):

$$= [(4*1) + (2*2) + (4*3)] * 20$$

$$= [4+4+12]*20$$

Example (cont'd)

InstrType _i	CPI,
<i>i</i> =1	1
<i>i</i> =2	2
<i>i</i> =3	3

Prog	InstrCount _i		
ram:	<i>i</i> =1	<i>i</i> =2	<i>i</i> =3
Α	4	2	4
В	8	2	2

CPUTime = \sum_{i} (InstrCount_i * CPI_i) * CycleTime

Program B (total 12 instructions):

$$= [(8*1) + (2*2) + (2*3)] * 20$$

= 360 ns/program

Example (cont'd, final)

InstrType _i	CPI,
<i>i</i> =1	1
<i>i</i> =2	2
<i>i</i> =3	3

Prog	InstrCount _i		
ram:	<i>i</i> =1	<i>i</i> =2	<i>i</i> =3
Α	4	2	4
В	8	2	2

Program A (total 10 instructions): 400ns

Program B (total 12 instructions): 360ns

Program B is faster!

(Intuitively, why should we expect this?)

Evaluating Performance

... of many programs!

First.... choose the programs!

You're in engineering and you want to buy a computer....

... which one should you buy?

The **fastest** one of course!

- But you can't trust:
 - MHz/GHz
 - MIPS
 - Or even your friend!

Important: Choose A Realistic Workload

- Best solution: Try it before you buy it!
 - Run your program on the computer
 - Mix and match your most-frequently used programs
 - Quake 3, Google Chrome, Skype, Altera Quartus II (help!)
 - Called a workload
 - Measure the CPUTime (fast stopwatch?)
 - Use <u>TOTAL CPUTime</u> as your metric (?)
- Problem: salesman doesn't want you to try it!
 - Find a new salesman!

- Problem: your programs are not portable!
 - Different OS, different CPU architectures, ...
 - Find a new OS ? A new program?
 - Write tiny version of your program to be portable
 - Toy Benchmarks: Sieve of Erastosthenes, Puzzle, Quicksort
 - Synthetic Benchmarks: Dhrystone (int), Whetstone (fp)
 - Computational Kernels: Livermore Loops, Linpack
- Problem: your program wasn't tuned for this computer
 - Spend an eternity tuning it for each one?
 - Rely upon compiler?
- Benchmarking is problematic!

- Compromise solution: Let somebody else try it!
 - They run their program
 - You trust them
 - Who? 3rd parties, eg: ZDnet? CNET? Tom's Hardware?
 - Who? Manufacturer, eg: IBM? Intel? Dell?
 - Who do you trust?
- SPEC: System Performance Evaluation Cooperative
 - Collect and distribute set of programs: a <u>benchmark suite</u>
 - Benchmark suite represents some typical workload (who's?)
 - Founded by industry (Apollo/HP, DEC, MIPS, and Sun)
 - Note: this is a bit like buying a car from an auto-mechanic...
 "of course, it runs just fine"

SPEC Benchmarks

SPEC Benchmarks

- Measure speed of a <u>system</u>
- System = CPU + memory subsystem + compiler + OS
- Improve any of these => improved performance
- Valuable indicator of <u>system</u> performance!

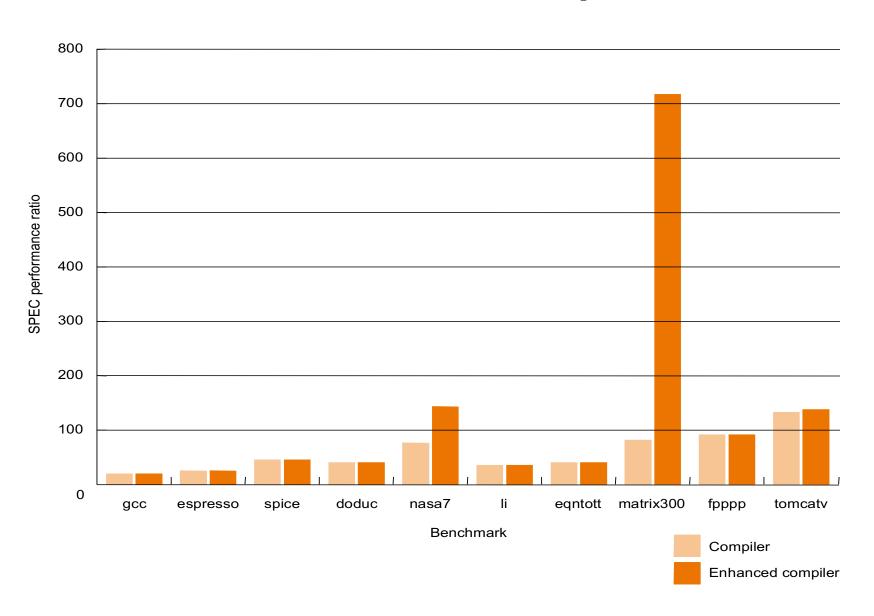
SPEC Rules

- Strict data reporting and collecting standards
- Rules of gameplay (benchmarks can be abused!)
- SPEC is the best we' ve got (so far...)!
- Only possible in last 10-15 years due to portable software (C)

SPEC Periodically Updates Benchmarks...

- 1989, 1992, 1995, 2000, 2006
- Eventually computers get too fast!
- Or nature of the workload changes!
- Or compilers get too smart!

Benchmarks – Compiler Result!



SPEC Benchmark Evolution

SPEC89

- Originally, called "SPEC"
- 4 integer programs, 6 floating-point programs
- One number: geometric mean of speedup relative to VAX 11/780
- Represents a scientific workload (note fp bias)

SPEC92

- 6 integer, 14 floating-point (int, fp results are <u>always</u> separated)
- Eliminates matrix300 from SPEC89
- Called CINT92, CFP92 or SPECint92, SPECfp92
- Each number: <u>geometric mean</u> of speedup relative to VAX 11/780

SPEC95

- 8 integer, 10 floating-point
- Two numbers: SPECint95, SPECfp95, relative to Sun 10/40
- SPEC history http://en.wikipedia.org/wiki/SPEC

SPEC CPU2000 and CPU2006



Lots of workloads!

www.spec.org

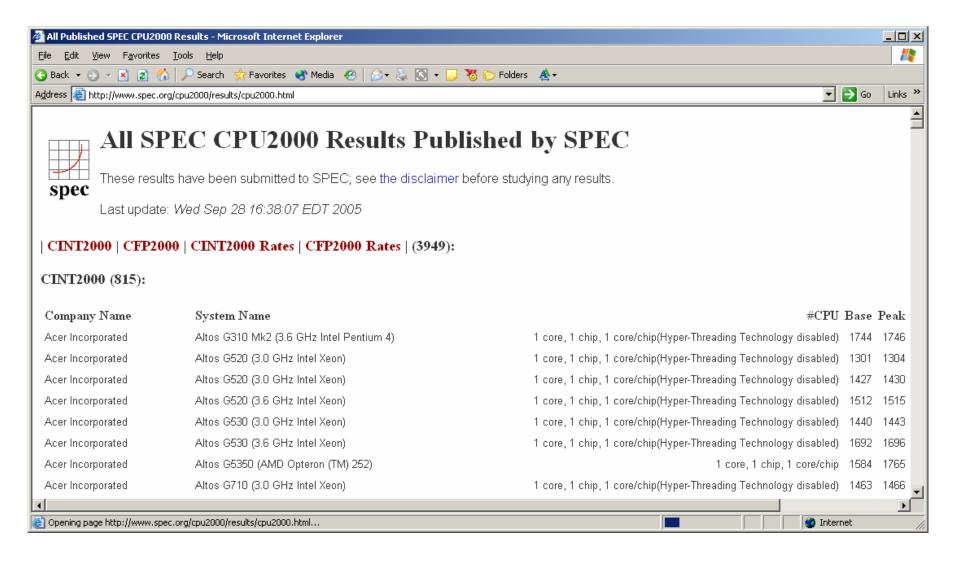
SPEC CPU2000

- Two benchmark sets
 - 12 Integer, 14 Floating-Point
- Two measurement conditions
 - Speed ("response time" or latency)
 - SPECint2000, SPECfp2000
 - Throughput
 - SPECint_rate2000, SPECfp_rate2000
- Why throughput numbers?
 - Computers with multiple CPUs (or multiple cores)
 - Computers with "virtual multiple" CPUs (eg, hyperthreading)
- How to measure throughput?
 - Run N copies of the benchmark, measure completion time
 - Convert execution time into a rate

SPEC CPU2000 Benchmarks

	INTEGER		FLOATING-POINT
Name	Description	Name	Туре
gzip vpr gcc mcf crafty parser eon perlbmk gap vortex bzip2 twolf	Compression FPGA circuit placement and routing The GNU C compiler Combinatorial optimization Chess program Word processing program Computer visualization perl application Group theory, interpreter Object-oriented database Compression Place and route simulator	wupwise swim mgrid applu mesa galgel art equake facerec ammp lucas fma3d sixtrack	Quantum chromodynamics Shallow water model Multigrid solver in 3-D potential field Parabolic/elliptical partial differential equation Three-dimensional graphics library Computational fluid dynamics Image recognition using neural networks Seismic wave propagation simulation Image recognition of faces Computational chemistry Primality testing Crash simulation using finite-element method High-energy nuclear physics accelerator design
		apsi	Meterorology: pollutant distribution

SPECint2000 Results



SPEC CPU2000: Base vs Peak

- "Base" results
 - same compiler flags used for all programs, "typical user"
- "Peak" results
 - choose best compiler flags for each program, "power user"
- Base, Peak numbers are normalized "percentage" results
 - Base Machine: Sun ULTRA5-10, 300MHz
 - Each program "problem size" scaled once
 - Runtime ~1000s-3000s on Base Machine
 - Takes ~40hrs to run full suite! (3 passes, CINT + CFP)
 - Base machine Performance defined to be "100%"

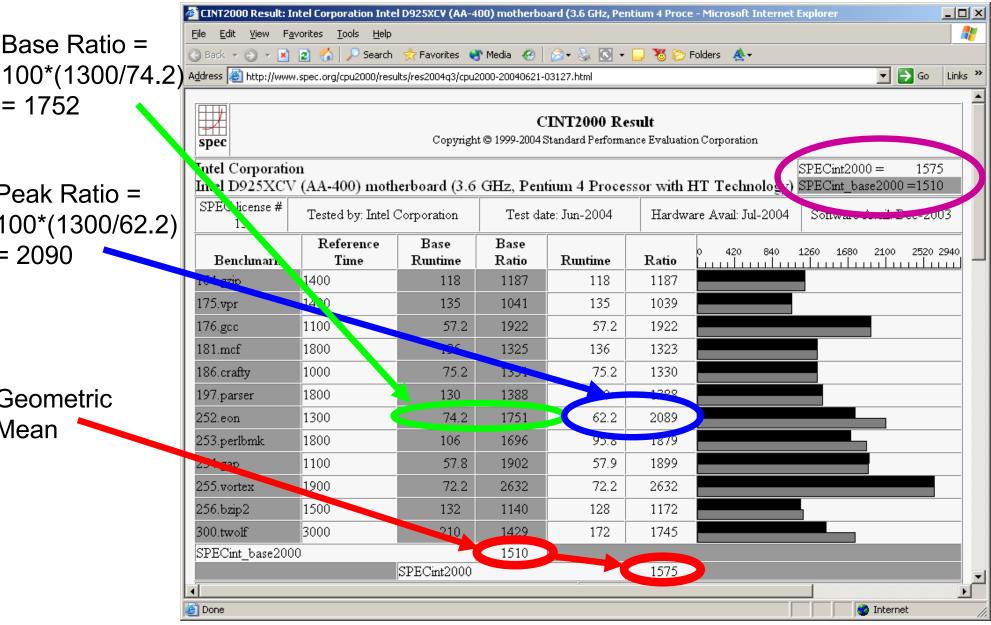
3.6 GHz Pentium 4

Base Ratio = = 1752

Peak Ratio = 100*(1300/62.2)

= 2090

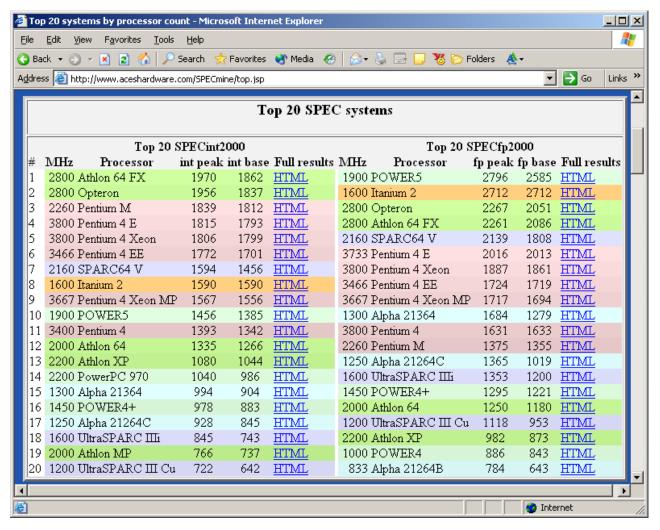
Geometric Mean



SPEC CPU2000 Measurement

- SPECint2000base score of 1510
 - Means "15.10 times faster" than Base Machine
 - This is an average result (how was average computed?)
- Fair measurement requirement
 - Run each program an ODD number of times, report the median execution time
 - Must not create special compiler flags, eg "-spec_cpu2000"
- Reporting requirements
 - Vendor supplies results, SPEC accepts and publishes them
 - Must report which OS, compiler version, all compiler flags used
 - Must report complete system configuration

Top 20 Computer Systems According to SPEC CPU2000 Data



Source: (Sept 27, 2005)

http://www.aceshardware.com/SPECmine/top.jsp

Top 20 Computer Systems 2004 2005

What's

Changed?

MHz Processor

1 3400 Pentium 4 EE

2 2400 Athlon 64 FX

3 2400 Opteron

4 3600 Pentium 4 E

5 3200 Pentium 4 Xeon

6 2000 Pentium M

7 3000 Pentium 4 Xeon

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П	2	2400 Athlon 64 FX	1700	1601	
П	3	2400 Opteron	1655	1566	
П	4	3600 Pentium 4 E	1575	1510	
П	5	3200 Pentium 4 Xeon	1563	1532	
П	6	2000 Pentium M	1541	1528	
П	7	3000 Pentium 4 Xeon MP		1455	
П	8	1900 POWER5	1452	1398	
П	9	1500 Itanium 2	1404	1380	
П	10	3400 Pentium 4	1393	1342	
П	11	1890 SPARC64 V	1345	1174	
П	12	2000 Athlon 64	1335	1266	
	13	2200 Athlon XP	1080	1044	
	14	1300 Alpha 21364	994	904	
П	15	1450 POWER4+	978	883	
	16	1250 Alpha 21264C	928	845	
	17	2000 Athlon MP	766	737	
	18	1200 UltraSPARC III Cu		642	
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2	2800 Opteron	1956	1837
3	2260 Pentium M	1839	1812
4	3800 Pentium 4 E	1815	1793
5	3800 Pentium 4 Xeon	1806	1799
6	3466 Pentium 4 EE	1772	1701
7	2160 SPARC64 V	1594	1456
8	1600 Itanium 2	1590	1590
9	3667 Pentium 4 Xeon MP	1567	1556
10	1900 POWER5	1456	1385
11	3400 Pentium 4	1393	1342
12	2000 Athlon 64	1335	1266
13	2200 Athlon XP	1080	1044
14	2200 PowerPC 970	1040	986
15	1300 Alpha 21364	994	904
16	1450 POWER4+	978	883
17	1250 Alpha 21264C	928	845
18	1600 UltraSPARC IIIi	845	743
19	2000 Athlon MP	766	737
20	1200 UltraSPARC Ⅲ Cu	722	642
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Source: (Oct, 2004)

(Sept 27, 2005)

http://www.aceshardware.com/SPECmine/top.jsp

SPEC CPU2006 Benchmarks

CINT2006 contains 12 benchmarks:

400.perlbench	С	PERL Programming Language
401.bzip2	С	Compression
403.gcc	С	C Compiler
429.mcf	С	Combinatorial Optimization
445.gobmk	С	Artificial Intelligence: go
456.hmmer	С	Search Gene Sequence
458.sjeng	С	Artificial Intelligence: chess
462.libquantum	С	Physics: Quantum Computing
464.h264ref	С	Video Compression
471.omnetpp	C++	Discrete Event Simulation
473.astar	C++	Path-finding Algorithms
483.xalancbmk	C++	XML Processing

SPEC CPU2006 Benchmarks

CFP2006 contains 17 benchmarks:

410.bwaves Fortran Fluid Dynamic	CS
416.gamess Fortran Quantum Che	emistry
433.milc C Physics: Quai	ntum Chromodynamics
434.zeusmp Fortran Physics/CFD	
435.gromacs C/Fortran Biochemistry/	/Molecular Dynamics
436.cactusADM C/Fortran Physics/Gene	eral Relativity
437.leslie3d Fortran Fluid Dynamic	cs
444.namd C++ Biology/Molec	cular Dynamics
447.dealll C++ Finite Elemen	t Analysis
450.soplex C++ Linear Progra	mming, Optimization
453.povray C++ Image Ray-tra	acing
454.calculix C/Fortran Structural Med	chanics
459.GemsFDTD Fortran Computationa	al Electromagnetics
465.tontoFortran Quantum Chemistry	
470.lbm C Fluid Dynamic	cs
481.wrf C/Fortran Weather Pred	iction
482.sphinx3 C Speech recog	nition

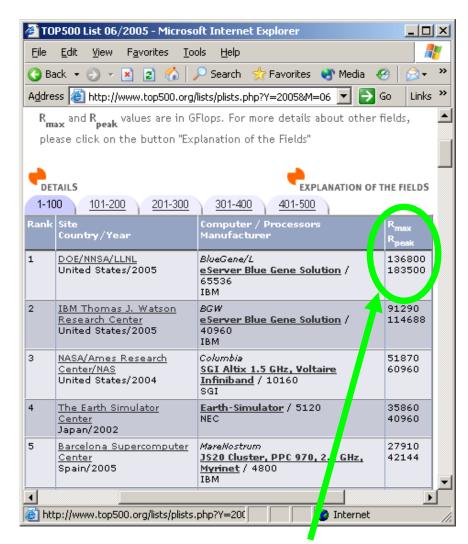
Coming Soon: New SPEC aka "CPUv6"

Top 500 Supercomputers

http://www.top500.org

- Supercomputing
 - 1,000s of processors
 - Specialized programs
 - Nuclear simulations, weather prediction
 - Usually: floating-point operations on dense matrices

Linpack performance



Other Benchmarks

- Banking/database transactions
 - http://www.tpc.org
 (Transaction Processing Performance Council)
- Embedded CPUs
 - http://www.eembc.org (Embedded Microprocessor Benchmark Consortium)
- Multimedia, Network processors
 - http://cares.icsl.ucla.edu (MediaBench, NetBench) (broken link?)
- Supercomputing (Linpack)
 - http://www.netlib.org/benchmark/hpl (linear eqn solving of dense matrices)
- Reconfigurable computing
 - RAW http://cag-www.lcs.mit.edu/raw/benchmark/README.html
 - VersaBench http://cag.csail.mit.edu/versabench/
- Some toy benchmarks or misc benchmarks...
 - http://rib.cs.utk.edu/cgi-bin/catalog.pl?rh=226&term=0!0
 - http://www.netlib.org

Summary: Evaluating Performance

- Performance of one program
 - Execution time, performance equation
 - Instruction counts, CPI, clock cycle time
- Performance of many programs
 - First, choose the benchmark program(s)
 - This is the most critical step !!!
 - Second, compute execution time for each task/program
 - SPEC has strict rules about fair play...
 - Third, summarize performance
 - SPEC computes **geometric average** of normalized performance
 - We'll investigate the rationale behind these rules tomorrow...

Summarizing Performance

Distilling the performance results of many programs into one performance number!

aka .. What the Means Mean!

Summarizing Performance

Given

- Many benchmark programs
- Each has different execution time

Goal

– How to calculate one "performance number" for all programs?

Confusing fact

Problems exist with every possible summary method!

Guiding light

- The summary method you choose should track execution time
- Execution time the only true measure of performance!

Summarizing Performance

Many possible summary methods...

- Arithmetic Mean of ExecutionTime (AMET)
 - Also: Weighted AMET
- Arithmetic Mean of Performance (AMP)
 - Beware AMP != 1 / AMET
- Harmonic Mean of Performance (HMP)
 - Note HMP = 1 / AMET
- Geometric Mean of Performance (GM)
 - Note GM(X)/GM(Y) = GM(X/Y)
- Many problems with each
 - But researchers often use "geometric mean"
 - This lecture will show you why...

Two Arithmetic Means

Two easy summary methods...

- Arithmetic Mean of ExecutionTime (AMET)
 - ET of 3 programs: 1 s, 10 s, 100 s
 - AMET = (1+10+100)/3 = 111/3 = 37 s
- Arithmetic Mean of Performance (AMP)
 - RECALL: Performance = 1 / ExecutionTime
 - Performance of 3 programs: 1 s⁻¹, 0.1 s⁻¹, 0.01 s⁻¹
 - AMP = $(1+0.1+0.01)/3 = 0.37 \text{ s}^{-1}$ • 1 / AMP = 2.7 s
- Beware

AMET != 1 / AMP

Leads to confusion, we'll never use AMP

Probing Further: Problem with Arithmetic Mean of Performance

- Beware
 - AMET != 1 / AMP
- Cannot use Arithmetic Mean of Performance (AMP) to summarize
- Why not??
 - Because Performance is a rate measurement, "programs per second"
- Instead, can sometimes use Harmonic Mean of Performance (HMP) to average rates

Harmonic Mean of Performance

Harmonic Mean

HMP(
$$R_i$$
) = $\frac{N}{1/R_1 + 1/R_2 + ... + 1}/R_N$



- Can use Harmonic Mean of Performance (HMP) to average rates
 - But, it is correct only if "same amount of work" is done
 - What is "work"?
 - "1 program" = 1 unit of work?
 - "1 instruction" = 1 unit of work?
- Example
 - HMP = 3 / (1/1 + 1/0.1 + 1/0.01) = 3/111 = 0.027 s⁻¹
- Harmonic Mean of Performance tracks Arithmetic Mean of ExecutionTime
 - 1 / HMP = 1/0.027 = 37 s
 - HMP is equivalent to:
 - "Convert Performance to ET, take arithmetic mean, convert back to Performance"
- Notice

$$AMET = 1 / HMP$$

Example 1 The Need for Arithmetic...

- You're at home and late for class....
 - Run 10km/h to your car (6 minutes, 1km)
 - Drive 100km/h to school (6 minutes, 10km)
 - Arrive early (whew!)
 - Walk 5km/h to class (6 minutes, 0.5km)
- True Average speed?
 - You travelled 11.5km in 18 min
 - 11.5km / 18min = 38.3 km/h
- Arithmetic Mean for average speed?
 (10km/h + 100km/h + 5km/h)/3 = 38.3 km/h
 - Arithmetic Mean works!
- Harmonic Mean for average speed?

```
HM = 3 * 1/(1/10 + 1/100 + 1/5) = 3 / (0.1 + 0.01 + 0.2) = 3 / 0.31 = 9.68 \text{ km/h}
```

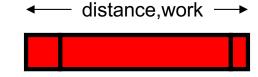
– Harmonic Mean doesn't work!!

Example 2 The Need for Harmony...

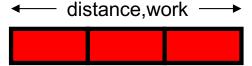
- You're going to an island for a vacation....
 - Drive 100km/h to the ferry (12 minutes, 20km)
 - Boat 30km/h to the island (40 minutes, 20km)
 - Bus 60km/h to the resort (20 minutes, 20km)
- True Average speed?
 - You travelled 60km in 72 minutes
 - 60km/72min = 50 km/h
- Arithmetic Mean for average speed?
 (100km/h + 30km/h + 60km/h)/3 = 63.3 km/h
 - Arithmetic Mean doesn't work!!
- Harmonic Mean for average speed?
 HM = 3 * 1/(1/100 + 1/30 + 1/60) = 3 / (0.01 + 0.033 + 0.0167) = 50 km/h
 - Harmonic Mean works!

Arithmetic vs Harmonic Means

- Averaging speed → speed is a rate
 - Rate is "work per time"
 - Averaging RATES requires some care!
- What's the difference?
 - Example 1



- AM works → each task is performed for same length of time
- HM fails → each task performs different amount of work
 - Work can be "same distance", or "same program"
- Example 2



- AM fails → each task takes different length of time
- HM works → each task performs the same amount of work

Example 3 Correctly Averaging Rates

- Slightly different numbers... note: different time, different work
 - Drive 100km/h to the ferry (6 minutes, 10km)
 - Boat 30km/h to the island (80 minutes, 40km)
 - Bus 60km/h to the resort (20 minutes, 20km)
- True Average speed?

- TrueAvg = TotalDist / TotalTime
- You travelled 70km in 106 minutes
- 70km/106min = 39.6 km/h

(this is the only true answer!)

- Arithmetic Mean for average speed?
 (100km/h + 30km/h + 60km/h)/3 = 63.3 km/h
 - Arithmetic Mean doesn't work!!
- Harmonic Mean for average speed?

```
HM = 3 * 1/(1/100 + 1/30 + 1/60) = 3 / (0.01 + 0.033 + 0.0167) = 50 km/h
```

- Harmonic Mean doesn't work!!
- Lesson
 - Easy to miss-use AMET or HMP and get incorrect results !!

Another Problem with Arithmetic Mean

- Example
 - Three programs: A=1s, B=10000s, C=10000s
 - ArithMeanBefore = 20001 / 3 = 6667s
 - Speed up Program A from 1s to 0.01s (100x!!)
 - ArithMeanAfter = 20000.01 / 3 = 6666.67s
 - Average Speedup = Before/After = 6667/6666.67 ≈ 1.00005
 - But one program was sped up by 100 times !!!
- Arithmetic Mean sometimes hides significant gains in performance
 - Each program is not treated equally
- Proposed Solution: Weighted Arithmetic Mean
 - Make each program "equally significant" in the mean.

Weighted Arithmetic Mean

Weighted Arithmetic Mean

– How to choose the weights? Two main choices:

1. Equalized Weighting

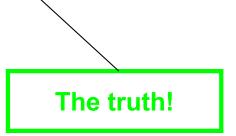
- Fix weights to each program to equalize ExecutionTime of each
 - Weight(A) = 10000, Weight(B) = 1, Weight(C) = 1
 - EQWeightArithMean = (10000*1 + 1*10000 + 1*10000)/3 = 10000s
- Speed up Program A from 1s to 0.01s (100x)
 - EQWeightArithMean = (10000*0.01 + 1*10000 + 1*10000)/3 = 6700s
- Average Speedup = Before/After = 10000/6700 ≈ 1.49
 - Change in EQWeightArithMean now reflects the big improvement to Program A
- What is the Speedup if we improve Program B from 10000s to 100s (also 100x)?

2. Alternate "Unequal" Weighting

- According to your Workload
- Eg, if you run Program B 10 times more often than Programs A or C...

Simple Arithmetic Mean Example

- Arithmetic Mean Example
 - Two computers, X and Y, each run 3 programs A, B, C
 - X: 10s 20s 30s
 - Y: 1s 10s 100s
 - ArithMean(X) = (10s + 20s + 30s)/3 = 20s
 - ArithMean(Y) = (1s + 10s + 100s)/3 = 37s
- Conclusion
 - X is faster than Y

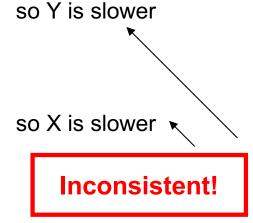


Limits of Arithmetic Mean

- Arithmetic Mean of Normalized results?
 - Normalize to X: ExecTime(Y relative to X) = ExecTime(Y) / ExecTime(X)
- Same Example
 - Two computers, X and Y, each run 3 programs A, B, C
 - X: 10s 20s 30s
 - Y: 1s 10s 100s
 - Conclusion: X is faster than Y

The truth!

- Normalize ExecTime to X (smaller number → Y faster)
 - ArithMean (Y/X) = (0.1 + 0.5 + 3.333) / 3 = 1.311
 - AM of normalized-ET of Y wrt X = 1.311 > 1.0
- Normalize ExecTime to Y (smaller number → X faster)
 - ArithMean (X/Y) = (10 + 2 + 0.3) / 3 = 4.1
 - AM of normalized-ET of X wrt Y = 4.1 > 1.0



Arithmetic Geometric Mean

- When to abandon Arithmetic Mean?
 - Must abandon if we normalize results
 - Get inconsistent answers, depends on choice of baseline
 - Must use Geometric Mean instead
- Geometric Mean

$$GM(R_i) = (R_1 * R_2 * ... * R_N)^{1/N}$$

Multiply N numbers, take Nth root Note – none of the numbers can be zero!!

Geometric Mean of Normalized Numbers

- Normalized numbers...
 - Must abandon Arithmetic Mean (inconsistent)
 - Must use Geometric Mean instead
- Same example
 - Two computers, X and Y, each run 3 programs A, B, C
 - GeoMean(X) = $(10s * 20s * 30s)^{1/3} = 18.17 s$
 - GeoMean(Y) = $(1s * 10s * 100s)^{1/3} = 10 s$
 - GeoMean(X/Y) = $(10 * 2 * 0.3)^{1/3}$ = 1.817
 - GeoMean(Y/X) = $(0.1 * 0.5 * 3.33)^{1/3}$ = 0.55 = 1 / 1.817
 - GeoMean gives consistent answers: Y is faster than X

Geometric Mean Properties

- Useful Properties of Geometric Mean
 - GeoMean(X) / GeoMean(Y) = GeoMean(X/Y)
 - GeoMean(X/Y) = 1 / GeoMean(Y/X)
 - Whether we normalize before computing the mean, or normalize after computing the mean, we get the same answer!
- Homework: prove it!
- Consequences
 - It doesn't matter which machine is used for normalization, we get the same relative answers!
 - Easy to change data if we decide to normalize to a different machine

Normalizing Performance Example

	Computer X	Computer Y
Program A	1s	10s
Program B	1000s	100s
Total Time	1001s	110s

- Which is faster, computer X or Y?
 - X is 10x faster than Y for program A
 - Y is 10x faster than X for program B
 - Confusing! How to summarize?
- Total ExecutionTime says Y is 9.1x faster
 - ArithMean of ExecutionTime says same thing
- OK so far.....

Normalizing Performance Example

			Normalize to X	
	Comp X	Comp Y	X	Υ
Program A	1s	10s	1	10
Program B	1000s	100s	1	0.1
ArithMean	500.5s	55s	1	5.05
GeoMean	31.6s	31.6s	1	1

- Normalize to X…..
 - GeoMean says X and Y are same speed
 - ArithMean says X is 5.05x faster than Y
 - Huh???
- It gets worse
 - Try normalizing to Y...** Beware... it will be confusing...

Normalizing Performance Example

			Normalize to X		Normalize to Y	
	Comp X	Comp Y	X	Y	X	Y
Program A	1s	10s	1	10	0.1	1
Program B	1000s	100s	1	0.1	10	1
ArithMean	500.5s	55s	1	5.05	5.05	1
GeoMean	31.6s	31.6s	1	1	1	1

- Normalize to X....
 - GeoMean says X and Y are same speed
 - ArithMean says X is 5.05x faster than Y
- Normalize to Y....
 - GeoMean still says X and Y are same speed
 - ArithMean says Y is 5.05x faster than X (opposite to before!)

Summarizing Summary

Lessons

- Cannot take Arithmetic Mean of Rates
- Cannot take ArithMean after Normalizing
- 3. Use HarmMean of Rates (if they do same amount of work)
- 4. Use GeoMean after Normalizing
- 5. GeoMean gives consistent answers, but may be misleading
 - Do a sanity check
 - AMET or TotalET sometimes more helpful (Y is 9.1x faster)
 - Would you rather own computer X or Y?

	Comp X	Comp Y
Program A	1s	10s
Program B	1000s	100s
Total Time	1001s	110s

Understanding SPEC CPU2000

- SPEC CPU2000 == standard set of benchmark programs
 - Constantly being updated, eg SPEC2006
- Results are Normalized to Base Machine
 - Base Machine: Sun ULTRA5-10, 300MHz
 - Base Machine Performance defined to be "100%"
- Multiple benchmark programs
 - Report "normalized" performance result of each program
 - Summarize by computing GEOMETRIC MEAN
 - Example
 - SPECint2000 = 1510
 - Means "15.10 times faster" than Base Machine
 - 1510 is a geometric mean of <u>normalized</u> performance for each benchmark
- Fair measurement requirement
 - Run each program ODD # times, report median execution time
 - Why the median? Why not fastest? Why not average?

Homework!

- Do Assignment 0
 - Matrix multiply, done several ways
- Start Assignment 1
 - Instead of matrix multiply, do Gaussian Elimination algorithm
 - Do both forward-elimination only
- Next Week
 - Culler text, Chapter 2, is online under "Lectures Reading"