

**Problem 1**

No, there is no such guarantee. There may be datapoints, which either (1) violate the margin, i.e.  $0 \leq \xi_i \leq 1$  or (2) are on the wrong side of the hyperplane, i.e.  $y_i(w^\top x_i + b) \geq 1 - \xi_i$  does not hold, in this case  $\xi_i > 1$ .

**Problem 2****Problem 3**

We prove that  $K(x, y) = (x^\top y + c)^d$  is a kernel by the construction rules.

- $K_1(x, y) = x^\top y$  is a kernel by Rule 5, where  $B = I$ .
- $K_2(x, y) = c$  is a kernel by Rule 4, where  $\phi(z) = \sqrt{c}$ ,  $\phi : \mathbb{R}^n \rightarrow \mathbb{R}^m$ ,  $m = 1$  and  $K_3(x, y) = x^\top y$
- $K_3(x, y) = K_1(x, y) + K_2(x, y)$  is a kernel by Rule 1
- $K_4(x, y) = K_3(x, y)^d$  is a kernel by recursive application of Rule 3

Thus  $K(x, y) = (x^\top y + c)^d$  is a valid kernel.

**Problem 4****Problem 5****Problem 6****Problem 7**

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